

# Model Predictive Control Toolbox

For Use with MATLAB®

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- Computation
- Visualization
- Programming

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### *Model Predictive Control Toolbox User's Guide*

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# Introduction

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What Is the Model Predictive Control Toolbox? (p. 1-2)	Toolbox overview
Model Predictive Control of a SISO Plant (p. 1-3)	Toolbox concepts: horizons, constraints, tuning weights
MIMO Plants (p. 1-10)	Extension to plants with multiple inputs and outputs

## What Is the Model Predictive Control Toolbox?

The Model Predictive Control (MPC) Toolbox is a collection of software that helps you design, analyze, and implement an advanced industrial automation algorithm. Like other MATLAB® tools, it provides a convenient graphical user interface (GUI) as well as a flexible command syntax that supports customization.

As its name suggests, MPC automates a target system (the “plant”) by combining a prediction and a control strategy. An approximate, linear plant model provides the prediction. The control strategy compares predicted plant states to a set of objectives, then adjusts available actuators to achieve the objectives while respecting the plant’s *constraints*. Such constraints can include the actuators’ physical limits, boundaries of safe operation, and lower limits for product quality.

MPC’s constraint-tolerance differentiates it from other “optimal control” strategies (e.g., the Linear-Quadratic-Gaussian approach supported in the Control Systems Toolbox). The impetus for this is industrial experience suggesting that the drive for profitability often pushes the plant to one or more constraints. MPC’s explicit consideration of such factors allows it to allocate the available plant resources intelligently as the system evolves over time.

The MPC Toolbox uses the same powerful linear dynamic modeling tools found in the Control Systems and System Identification Toolboxes. You can employ transfer functions, state-space matrices, or a combination of the two. You can also include delays, which are a common feature of industrial plants.

If you don’t have a model but can perform experiments, you can use the System Identification Toolbox to develop a data-based model, then exploit it in the MPC Toolbox.

If you’d rather use Simulink® graphical tools to model your plant, the MPC Toolbox provides a Simulink block for that environment. For example, you can easily linearize a nonlinear Simulink plant, use the linearized model to build an MPC Controller block, and evaluate its control of the nonlinear plant.

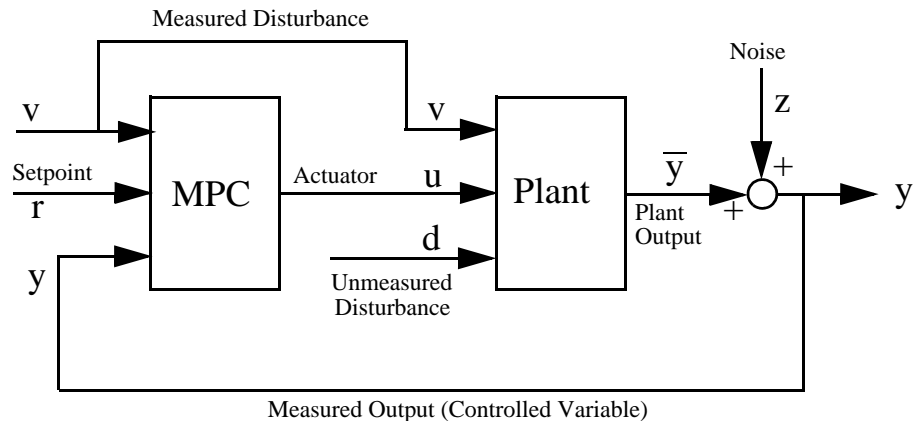
Finally, you can use MPC tools in Simulink to develop and test a control strategy, then implement it in a real plant using the Real Time Workshop.

## Model Predictive Control of a SISO Plant

The usual MPC Toolbox application involves a plant having multiple inputs and multiple outputs (a *MIMO* plant).

Consider instead the simpler application shown in Figure 1-1 (see summary of nomenclature in Table 1-1). This plant could be a manufacturing process, such as a unit operation in an oil refinery, or a device, such as an electric motor. The main objective is to hold a single *output*,  $\bar{y}$ , at a *reference value* (or *setpoint*),  $r$ , by adjusting a single *manipulated variable* (or *actuator*)  $u$ . This is what is generally termed a *SISO* (single-input single-output) plant. The block labeled MPC represents an MPC Toolbox feedback controller designed to achieve the control objective.

The SISO plant actually has multiple inputs, as shown in Figure 1-1. In addition to the manipulated variable input,  $u$ , there may be a measured disturbance,  $v$ , and an unmeasured disturbance,  $d$ .



**Figure 1-1: Block Diagram of a SISO MPC Toolbox Application**

The unmeasured disturbance is always present. As shown in Figure 1-1, it is an *independent* input – not affected by the controller or the plant. It represents all the unknown, unpredictable events that upset plant operation. (In the context of Model Predictive Control, it can also represent unmodeled dynamics.) When such an event occurs, the only indication is its effect on the *measured* output,  $y$ , which is *fed back* to the controller as shown in Figure 1-1.

**Table 1-1: Description of MPC Toolbox Signals**

Symbol	Description
$d$	<i>Unmeasured disturbance</i> . Unknown but for its effect on the plant output. The controller provides <i>feedback</i> compensation for such disturbances.
$r$	<i>Setpoint (or reference)</i> . The target value for the output.
$u$	<i>Manipulated variable (or actuator)</i> . The signal the controller adjusts in order to achieve its objectives.
$v$	<i>Measured disturbance (optional)</i> . The controller provides <i>feedforward</i> compensation for such disturbances as they occur to minimize their impact on the output.
$\bar{y}$	<i>Output (or controlled variable)</i> . The signal to be held at the setpoint. This is the “true” value, uncorrupted by measurement noise.
$y$	<i>Measured output</i> . Used to estimate the true value, $\bar{y}$ .
$z$	<i>Measurement noise</i> . Represents electrical noise, sampling errors, drifting calibration, and other effects that impair measurement precision and accuracy.

Some applications have unmeasured disturbances only. A *measured* disturbance,  $v$ , is another independent input affecting  $\bar{y}$ . In contrast to  $d$ , the controller receives the measured  $v$  directly, as shown in Figure 1-1. This allows the controller to compensate for  $v$ 's impact on  $\bar{y}$  immediately rather than waiting until the effect appears in the  $y$  measurement. This is called *feedforward* control.

In other words, an MPC Toolbox design always provides *feedback* compensation for unmeasured disturbances and *feedforward* compensation for any measured disturbance.

The MPC Toolbox design requires a *model* of the impact that  $v$  and  $u$  have on  $\bar{y}$  (symbolically,  $v \rightarrow \bar{y}$  and  $u \rightarrow \bar{y}$ ). It uses this *plant model* to calculate the  $u$  adjustments needed to keep  $\bar{y}$  at its setpoint.

This calculation considers the effect of any known constraints on the adjustments (typically an actuator upper or lower bound, or a constraint on how rapidly  $u$  can vary). One may also specify bounds on  $\bar{y}$ . These constraint specifications are a distinguishing feature of an MPC Toolbox design and can be particularly valuable when one has multiple control objectives to be achieved *via* multiple adjustments (a MIMO plant). In the context of a SISO system, such constraint handling is often termed an *anti-windup* feature.

If the plant model is accurate, the plant responds quickly to adjustments in  $u$ , and no constraints are encountered, feedforward compensation can counteract the impact of  $v$  perfectly. In reality, model imperfections, physical limitations, and unmeasured disturbances cause the  $y$  to deviate from its setpoint. Therefore, the MPC Toolbox design includes a *disturbance model* ( $d \rightarrow \bar{y}$ ) to *estimate*  $d$  and *predict* its impact on  $\bar{y}$ . It then uses its  $u \rightarrow \bar{y}$  model to calculate appropriate adjustments (feedback). This calculation also considers the known constraints.

Various *noise* effects can corrupt the measurement. The signal  $z$  in Figure 1-1 represents such effects. They could vary randomly with a zero mean, or could exhibit a non-zero, drifting bias. The MPC Toolbox design uses a  $z \rightarrow y$  model in combination with its  $d \rightarrow \bar{y}$  model to remove the estimated noise component (*filtering*).

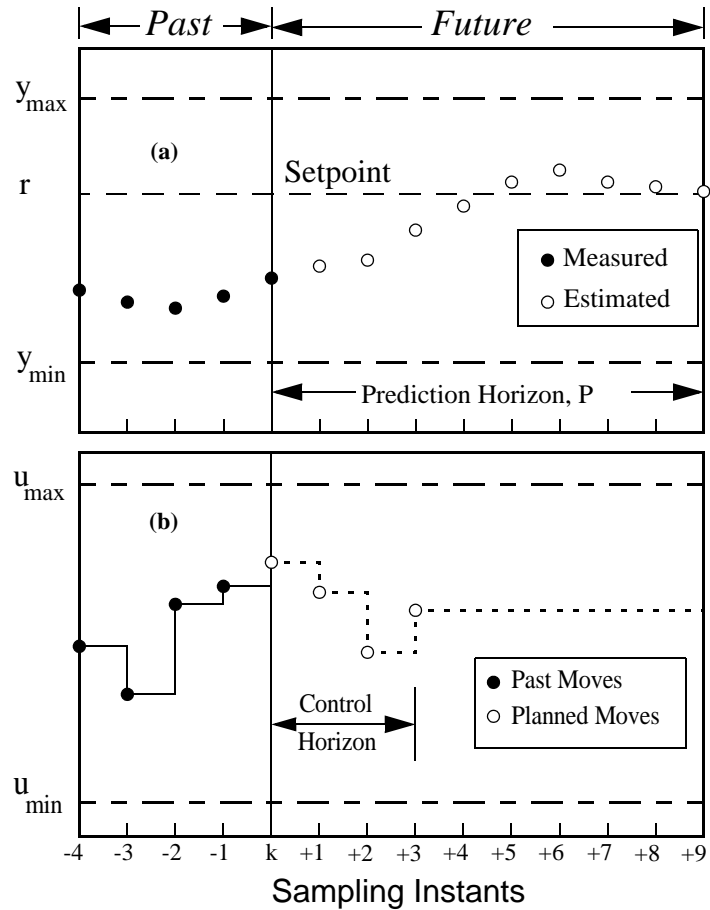
The above feedforward/feedback actions comprise the controller's *regulator* mode. The MPC Toolbox design also provides a *servo* mode, *i.e.*, it adjusts  $u$  such that  $\bar{y}$  tracks a time-varying setpoint.

The tracking accuracy depends on the plant characteristics (including constraints), the accuracy of the  $u \rightarrow \bar{y}$  model, and whether or not future setpoint variations can be *anticipated*, *i.e.*, known in advance. If so, it provides feedforward compensation for these.

## A Typical Sampling Instant

An MPC Toolbox design generates a *discrete-time* controller – one that takes action at regularly-spaced, discrete time instants. The *sampling instants* are the times at which the controller acts. The interval separating successive sampling instants is the *sampling period*,  $\Delta t$  (also called the *control interval*).

This section provides more details on the events occurring at each sampling instant.



**Figure 1-2: Controller State at the  $k$ th Sampling Instant**

Figure 1-2 shows the state of a hypothetical SISO MPC system that has been operating for many sampling instants. Integer  $k$  represents the current instant. The latest measured output,  $y_k$ , and previous measurements,  $y_{k-1}, y_{k-2}, \dots$ , are known and are the filled circles in Figure 1-2(a). If there is a measured disturbance, its current and past values would be known (not shown).

Figure 1-2 (b) shows the controller's previous *moves*,  $u_{k-4}, \dots, u_{k-1}$ , as filled circles. As is usually the case, a *zero-order hold* receives each move from the controller and holds it until the next sampling instant, causing the step-wise variations shown in Figure 1-2 (b).

To calculate its next *move*,  $u_k$  the controller operates in two phases:

- 1 *Estimation*. In order to make an intelligent move, the controller needs to know the current state. This includes the true value of the controlled variable,  $\bar{y}_k$ , and any internal variables that influence the future trend,  $\bar{y}_{k+1}, \dots, \bar{y}_{k+P}$ . To accomplish this, the controller uses all past and current measurements and the models  $u \rightarrow \bar{y}$ ,  $d \rightarrow \bar{y}$ ,  $w \rightarrow \bar{y}$ , and  $z \rightarrow y$ . For details, see "Prediction" and "State Estimation".
- 2 *Optimization*. Values of setpoints, measured disturbances, and constraints are specified over a finite *horizon* of future sampling instants,  $k+1, k+2, \dots, k+P$ , where  $P$  (a finite integer  $\geq 1$ ) is the *prediction horizon* – see Figure 1-2 (a). The controller computes  $M$  moves  $u_k, u_{k+1}, \dots, u_{k+M-1}$ , where  $M$  ( $\geq 1, \leq P$ ) is the *control horizon* – see Figure 1-2 (b). In the hypothetical example shown in the figure,  $P = 9$  and  $M = 4$ . The moves are the solution of a *constrained* optimization problem. For details of the formulation, see Chapter 2, "Optimization Problem".

In the example, the optimal moves are the four open circles in Figure 1-2 (b), and the controller predicts that the resulting output values will be the nine open circles in Figure 1-2 (a). Notice that both are within their *constraints*,  $u_{min} \leq u_{k+j} \leq u_{max}$  and  $y_{min} \leq y_{k+i} \leq y_{max}$ .

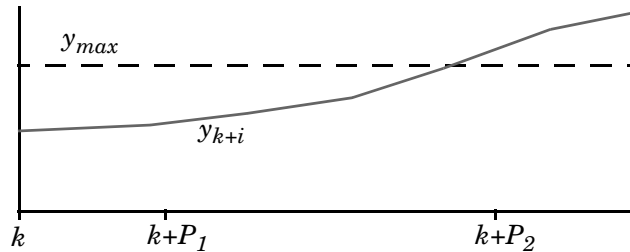
When it's finished calculating, the controller sends move  $u_k$  to the plant. The plant operates with this *constant* input until the next sampling instant,  $\Delta t$  time units later. The controller then obtains new measurements and *totally revises its plan*. This cycle repeats indefinitely.

Reformulation at each sampling instant is essential for good control. The predictions made during the optimization stage are imperfect. Periodic measurement feedback allows the controller to correct for this error and for unexpected disturbances.

## Prediction and Control Horizons

You might wonder why the controller bothers to optimize over  $P$  future sampling periods and calculate  $M$  future moves when it discards all but the first move in each cycle. Indeed, under certain conditions a controller using  $P = M = 1$  would be identical to one using  $P = M = \infty$ . More often, however, the horizon values have an important impact. Some examples follow:

- *Constraints.* Given sufficiently long horizons, the controller can “see” a potential constraint and avoid it – or at least minimize its adverse effects. For example, consider the situation depicted below in which one controller objective is to keep plant output  $y$  below an upper bound  $y_{max}$ . The current sampling instant is  $k$ , and the model predicts the upward trend  $y_{k+i}$ . If the controller were looking  $P_1$  steps ahead, it wouldn’t be concerned by the constraint until more time had elapsed. If the prediction horizon were  $P_2$ , it would begin to take corrective action immediately.



- *Plant delays.* Suppose that the plant includes a pure time delay equivalent to  $D$  sampling instants. In other words, the controller’s current move,  $u_k$ , has no effect until  $y_{k+D+1}$ . In this situation it is essential that  $P \gg D$  and  $M \ll P - D$ , as this forces the controller to consider the full effect of each move. For example, suppose  $D = 5$ ,  $P = 7$ ,  $M = 3$ , the current time instant is  $k$ , and the three moves to be calculated are  $u_k$ ,  $u_{k+1}$ , and  $u_{k+2}$ . Moves  $u_k$ ,  $u_{k+1}$  would have some impact within the prediction horizon, but move  $u_{k+2}$  would have none until  $y_{k+8}$ , which is outside. Thus,  $u_{k+2}$  is indeterminant. Setting  $P = 8$  (or  $M = 2$ ) would allow a unique value to be determined. It would be better to increase  $P$  even more.
- *Other nonminimum phase plants.* Consider a SISO plant with an inverse-response, i.e., a plant with a short-term response in one direction,



but a longer term response in the opposite direction. The optimization should focus primarily on the longer-term behavior. Otherwise, the controller would move in the wrong direction.

Most designers choose  $P$  and  $M$  such that controller performance is insensitive to small adjustments in these horizons. Here are typical rules of thumb for a lag-dominant, stable process:

- 1** Choose the control interval such that the plant's open-loop settling time is approximately 20-30 sampling periods (i.e., the sampling period is approximately one fifth of the dominant time constant).
- 2** Choose prediction horizon  $P$  to be the number of sampling periods used in step 1.
- 3** Use a relatively small control horizon  $M$ , e.g., 3-5.

If performance is poor, you should examine other aspects of the optimization problem and/or check for inaccurate controller predictions.

## MIMO Plants

One advantage of an MPC Toolbox design (relative to classical multi-loop control) is that it generalizes directly to plants having multiple inputs and outputs. Moreover, the plant can be *non-square*, i.e., having an unequal number of actuators and outputs. Industrial applications involving hundreds of actuators and controller outputs have been reported.

The main challenge is to tune the controller to achieve multiple objectives. For example, if there are several outputs to be controlled, it might be necessary to prioritize so that the controller provides accurate setpoint tracking for the most important output, sacrificing others when necessary, e.g., when it encounters constraints. The MPC Toolbox features support such prioritization.

### Optimization and Constraints

As discussed in more detail in Chapter 2, “Optimization Problem”, the MPC Toolbox controller solves an optimization problem much like the LQG optimal control described in the Control System Toolbox. The main difference is that the MPC Toolbox optimization problem includes explicit *constraints* on  $u$  and  $y$ .

### Setpoint Tracking

Consider first a case with no constraints. A primary control objective is to force the plant outputs to track their setpoints.

Specifically, the controller predicts how much each output will deviate from its setpoint within the prediction horizon. It multiplies each deviation by the output’s weight, and computes the weighted sum of squared deviations,  $S_y(k)$ , as follows:

$$S_y(k) = \sum_{i=1}^P \sum_{j=1}^{n_y} \left\{ w_j^y [r_j(k+i) - y_j(k+i)] \right\}^2$$

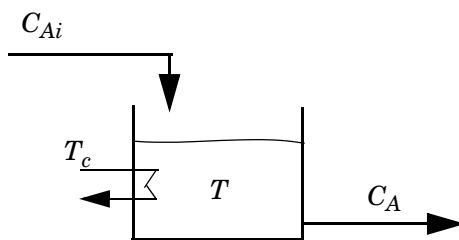
where  $k$  is the current sampling interval,  $k+i$  is a future sampling interval (within the prediction horizon),  $P$  is the prediction horizon,  $n_y$  is the number of plant outputs,  $w_j^y$  is the *weight* for output  $j$ , and  $[r_j(k+i) - y_j(k+i)]$  is the predicted deviation at future instant  $k+i$ .

If  $w_j^y \gg w_{i \neq j}^y$  the controller does its best to track  $r_j$ , sacrificing  $r_i$  tracking if necessary. If  $w_j^y = 0$ , on the other hand, the controller completely ignores deviations  $r_j - y_j$ .

Choosing the weights is a critical step. You will usually need to tune your controller, varying the weights to achieve the desired behavior.

As an example, consider Figure 1-3, which depicts a type of chemical reactor (a CSTR). Feed enters continuously with reactant concentration  $C_{Ai}$ . A reaction takes place inside the vessel at temperature  $T$ . Product exits continuously, and contains residual reactant at concentration  $C_A$  ( $< C_{Ai}$ ).

The reaction liberates heat. A coolant having temperature  $T_c$  flows through coils immersed in the reactor to remove excess heat.



**Figure 1-3: CSTR Schematic**

From the MPC Toolbox point of view,  $T$  and  $C_A$  would be plant outputs, and  $C_{Ai}$  and  $T_c$  would be inputs. More specifically,  $C_{Ai}$  would be an independent disturbance input, and  $T_c$  would be a manipulated variable (actuator).

There is one manipulated variable (the coolant temperature), so it's impossible to hold both  $T$  and  $C_A$  at setpoints. Controlling  $T$  would usually be a high priority. Thus, you might set the output weight for  $T$  much larger than that for  $C_A$ . In fact, you might set the  $C_A$  weight to zero, allowing  $C_A$  to float within an *acceptable operating region* (to be defined by constraints).

### Move Suppression

If the controller focuses exclusively on setpoint tracking, it might choose to make large manipulated-variable adjustments. These could be impossible to achieve. They could also accelerate equipment wear or lead to control system instability.

Thus, the MPC Toolbox controller also monitors a weighted sum of controller adjustments, calculated according to the following equation:

$$S_{\Delta u}(k) = \sum_{i=1}^M \sum_{j=1}^{n_{mv}} \left\{ w_j^{\Delta u} \Delta u_j(k+i-1) \right\}^2$$

where  $M$  is the control horizon,  $n_{mv}$  is the number of manipulated variables,  $\Delta u_j(k+i-1)$  is the predicted adjustment (i.e., *move*) in manipulated variable  $j$  at future (or current) sampling interval  $k+i-1$ , and  $w_j^{\Delta u}$  is a weight, which must be zero or positive. Increasing  $w_j^{\Delta u}$  forces the controller to make smaller, more cautious  $\Delta u_j$  moves. In many cases (but not all) this will have the following effects:

- The controller’s setpoint tracking will degrade
- The controller will be less sensitive to prediction inaccuracies (i.e., more *robust*)

### Setpoints on Manipulated Variables

In most applications, the controller’s manipulated variables (MVs) should move freely (within a constrained region) to compensate for disturbances and setpoint changes. An attempt to hold an MV at a point within the region would degrade output setpoint tracking.

On the other hand, some plants have more MVs than output setpoints. In such a plant, if all manipulated variables were allowed to move freely, the MV values needed to achieve a particular setpoint or to reject a particular disturbance would be non-unique. Thus, the MVs would drift within the operating space.

A common approach is to define setpoints for “extra” MVs. These setpoints usually represent operating conditions that improve safety, economic return, etc. The MPC Toolbox design includes an additional term to accommodate such cases, as follows:

$$S_u(k) = \sum_{i=1}^M \sum_{j=1}^{n_{mv}} \left\{ w_j^u [\bar{u}_j - u_j(k+i-1)] \right\}$$

where  $\bar{u}_j$  is the manipulated variable setpoint (nominal value) for the  $j^{\text{th}}$  MV, and  $w_j^u$  is the corresponding weight.

## Constraints

Constraints may be either *hard* or *soft*. A hard constraint must not be violated. Unfortunately, under some conditions a constraint violation might be unavoidable (e.g., an unexpected, large disturbance), and a realistic controller must allow for this.

The MPC Toolbox does so by *softening* each constraint, making a violation mathematically acceptable, though discouraged. The designer may specify the degree of softness in each case, making selected constraints less likely to be violated than others. See “Optimization Problem” on page 2-5 for the mathematical details.

Briefly, you specify a *tolerance band* for each constraint. If the tolerance band is zero, the constraint is hard (no violation allowed). Increasing the tolerance band softens the constraint.

The tolerance band *is not* a limit on the constraint violation, however. (If it were, you would still have a hard constraint.) You need to view it relative to other constraints.

For example, suppose you have two constraints, one on a temperature and the other on a flow rate. You specify a tolerance band of 2 degrees on the temperature constraint, and 20 kg/s on the flow rate constraint. The MPC Toolbox controller interprets this to mean that violations of these magnitudes are of *equal concern*, and should be handled accordingly.

## State Estimation

At the beginning of each sampling instant the controller estimates the current plant state. Accurate knowledge of the state improves prediction accuracy, which, in turn, improves controller performance.

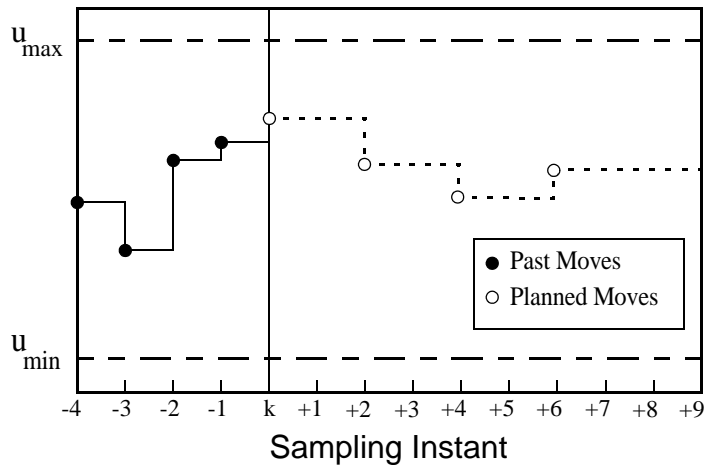
If all plant states were measured, the state estimation problem would be relatively simple, requiring consideration of measurement noise effects only. Unfortunately, the internal workings of a typical plant are unmeasured, and the controller must estimate their current values from the available measurements. It also estimate the values of any sustained, unmeasured disturbances.

The MPC Toolbox provides a default state estimation strategy, which the designer may customize. For details, see “State Estimation” on page 2-8.

## Blocking

In Figure 1-2 (b),  $M = 4$  and  $P = 9$ , and the controller is optimizing the first  $M$  moves of the prediction horizon, after which the manipulated variable remains constant for the remaining  $P - M = 5$  sampling instants.

Figure 1-4 shows an alternative *blocked* strategy – again with 4 planned moves – in which the first occurs at sampling instant  $k$ , the next at  $k+2$ , the next at  $k+4$ , and the final at  $k+6$ . A *block* is one or more successive sampling periods during which the manipulated variable is constant. The *block durations* are the number of sampling periods in each block. In Figure 1-4 the block durations are 2, 2, 2, and 3. (Their sum must equal  $P$ .)



**Figure 1-4: Blocking Example with 4 Moves**

As for the default (unblocked) mode, only the current move,  $u_k$ , actually goes to the plant. Thus, as shown in Figure 1-4, the controller has made a plant adjustment at each sampling instant.

So why use blocking? When  $P \gg M$  (as is generally recommended), and all  $M$  moves are at the beginning of the horizon, the moves tend to be larger (because all but the final move last just one sampling period). Blocking often leads to smoother adjustments, all other things being equal.

See the subsequent case study examples and the literature for more discussion and MIMO design guidelines.





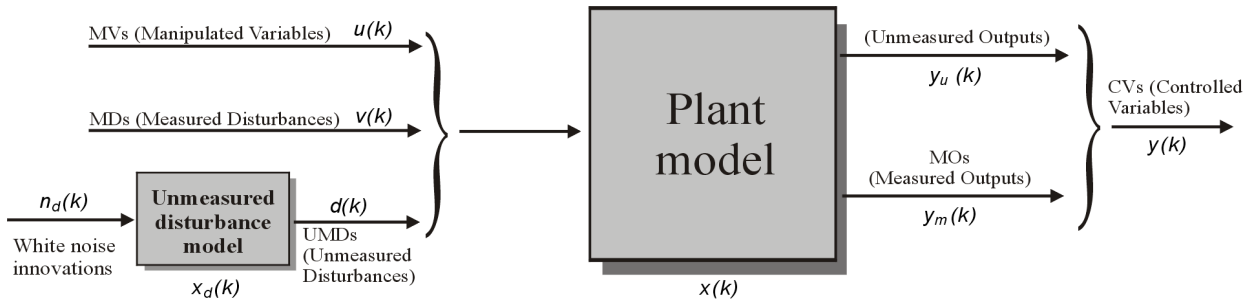
# MPC Problem Setup

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Prediction Model (p. 2-2)	A discussion of the prediction model used by the controller to estimate hypothetical future outputs over the prediction horizon.
Optimization Problem (p. 2-5)	A mathematical description of the cost function used by the controller to optimize control moves over the control horizon.
State Estimation (p. 2-8)	A state-space model is used to represent the combination of the plant model, noise model, and disturbance model.
QP Matrices (p. 2-12)	A brief discussion of the mathematical structure of matrices associated with the optimization problem.
MPC Computation (p. 2-18)	A discussion of the algorithms used for constrained and unconstrained model predictive control.
Using Identified Models (p. 2-19)	A description of the way identified models are handled

## Prediction Model

The linear model used in the MPC Toolbox for prediction and optimization is depicted in Figure 2-1.



**Figure 2-1: Model Used for Optimization**

The model consists of

- A model of the *plant* to be controlled, whose inputs are the manipulated variables, the measured disturbances, and the unmeasured disturbances
- A model generating the unmeasured *disturbances*

---

**Note** When defining an MPC controller, you must specify a plant model. You do not need to specify a model generating the disturbances, as the controller setup assumes by default that unmeasured disturbances are generated by integrators driven by white noise (see “Output Disturbance Model” on page 2-9 and `setindist` on page 6-38)

---

The model of the plant is a linear time-invariant system described by the equations

$$x(k+1) = Ax(k) + B_u u(k) + B_v v(k) + B_d d(k)$$

$$y_m(k) = C_m x(k) + D_{vm} v(k) + D_{dm} d(k)$$

$$y_u(k) = C_u x(k) + D_{vu} v(k) + D_{du} d(k) + D_{uu} u(k)$$

where  $x(k)$  is the  $n_x$ -dimensional state vector of the plant,  $u(k)$  is the  $n_u$ -dimensional vector of manipulated variables (MV), i.e., the command inputs,  $v(k)$  is the  $n_v$ -dimensional vector of measured disturbances (MD),  $d(k)$  is the  $n_d$ -dimensional vector of unmeasured disturbances (UD) entering the plant,  $y_m(k)$  is the vector of measured outputs (MO), and  $y_u(k)$  is the vector of unmeasured outputs (UO). The overall output vector  $y(k)$  collects  $y_m(k)$  and  $y_u(k)$ .

The Model Predictive Control Toolbox accepts both plant models specified as LTI objects, and models obtained from input/output data using the System Identification Toolbox (IDMODEL objects), see Using Identified Models (p. 2-19).

In the above equations  $d(k)$  collects both state disturbances ( $B_d \neq 0$ ) and output disturbances ( $D_d \neq 0$ ).

---

**Note** A valid plant model for the MPC Toolbox cannot have direct feedthrough of manipulated variables  $u(k)$  on the measured output vector  $y_m(k)$ .

---

The unmeasured disturbance  $d(k)$  is modeled as the output of the linear time invariant system

$$x_d(k+1) = \bar{A}x_d(k) + \bar{B}n_d(k) \quad (2-1)$$

$$d(k) = \bar{C}x_d(k) + \bar{D}n_d(k). \quad (2-2)$$

The system described by the above equations is driven by the random Gaussian noise  $n_d(k)$ , having zero mean and unit covariance matrix. For instance, a step-like unmeasured disturbance is modeled as the output of an integrator. Input disturbance models as in the equations above can be manipulated by using the methods `getindist` on page 6-14 and `setindist` on page 6-38.

---

**Note** If continuous-time models are supplied, they are internally sampled with the controller's sampling time.

---

## Offsets

In many practical applications, the matrices  $A, B, C, D$  of the model representing the process to control are obtained by linearizing a nonlinear dynamical system, such as

$$x' = f(x, u, v, d)$$

$$y = h(x, u, v, d),$$

at some nominal value  $x=x_0, u=u_0, v=v_0, d=d_0$ . In these equations  $x'$  denotes either the time derivative (continuous time model) or the successor  $x(k+1)$  (discrete time model). As an example,  $x_0, u_0, v_0, d_0$  may be obtained by using TRIM on a simulink model describing the nonlinear dynamical equations, and  $A, B, C, D$  by using LINMOD. The linearized model has the form

$$x' \cong f(x_0, u_0, v_0, d_0) + \nabla_x f(x_0, u_0, v_0, d_0)(x - x_0) + \nabla_u f(x_0, u_0, v_0, d_0)(u - u_0) + \nabla_v f(x_0, u_0, v_0, d_0)(v - v_0) + \nabla_d f(x_0, u_0, v_0, d_0)(d - d_0)$$

$$y \cong h(x_0, u_0, v_0, d_0) + \nabla_x h(x_0, u_0, v_0, d_0)(x - x_0) + \nabla_u h(x_0, u_0, v_0, d_0)(u - u_0) + \nabla_v h(x_0, u_0, v_0, d_0)(v - v_0) + \nabla_d h(x_0, u_0, v_0, d_0)(d - d_0)$$

The matrices  $A, B, C, D$  of the model are readily obtained from the Jacobian matrices appearing in the equations above.

The linearized dynamics are affected by the constant terms  $F=f(x_0, u_0, v_0, d_0)$  and  $H=h(x_0, u_0, v_0, d_0)$ . For this reason the MPC algorithm internally adds a measured disturbance  $v=1$ , so that  $F$  and  $H$  can be embedded into  $B_v$  and  $D_v$ , respectively, as additional columns.

---

**Note** Nonzero offset values  $d_0$  for unmeasured disturbances, while relevant for obtaining the linearized model matrices, are not relevant for the MPC problem setup. In fact, only  $d-d_0$  can be estimated from output measurements.

---

## Optimization Problem

Assume that the estimates of  $x(k)$ ,  $x_d(k)$  are available at time  $k$  (for state estimation see “State Estimation” on page 2-8). The MPC control action at time  $k$  is obtained by solving the optimization problem

$$\begin{aligned} \min_{\Delta u(k|k), \dots, \Delta u(m-1+k|k), \varepsilon} & \left\{ \sum_{i=0}^{p-1} \left( \sum_{j=1}^{n_y} \left| w_{i+1,j}^y (y_j(k+i+1|k) - r_j(k+i+1)) \right|^2 \right. \right. \\ & \left. \left. + \sum_{j=1}^{n_u} \left| w_{i,j}^{\Delta u} \Delta u_j(k+i|k) \right|^2 + \sum_{j=1}^{n_u} \left| w_{i,j}^u (u_j(k+i|k) - u_{j\text{target}}(k+i)) \right|^2 \right) + \rho_\varepsilon \varepsilon^2 \right\} \end{aligned} \quad (2-3)$$

where the subscript “ $(\cdot)_j$ ” denotes the  $j$ -th component of a vector, “ $(k+i|k)$ ” denotes the value predicted for time  $k+i$  based on the information available at time  $k$ ;  $r(k)$  is the current sample of the output reference, subject to

$$\begin{aligned} u_{j\min}(i) - \varepsilon V_j^u \min(i) &\leq u_j(k+i|k) \leq u_{j\max}(i) + \varepsilon V_j^u \max(i) \\ \Delta u_{j\min}(i) - \varepsilon V_j^{\Delta u} \min(i) &\leq \Delta u_j(k+i|k) \leq \Delta u_{j\max}(i) + \varepsilon V_j^{\Delta u} \max(i) \\ y_{j\min}(i) - \varepsilon V_j^y \min(i) &\leq y_j(k+i+1|k) \leq y_{j\max}(i) + \varepsilon V_j^y \max(i) \\ \Delta u(k+h|k) &= 0, h = m, \dots, p-1 \\ \varepsilon &\geq 0 \end{aligned} \quad i = 0, \dots, p-1 \quad (2-4)$$

with respect to the sequence of input increments  $\{\Delta u(k|k), \dots, \Delta u(m-1+k|k)\}$  and to the slack variable  $\varepsilon$ , and by setting  $u(k) = u(k-1) + \Delta u(k|k)^*$ , where  $\Delta u(k|k)^*$  is the first element of the optimal sequence.

---

**Note** Although only the measured output vector  $y_m(k)$  is fed back to the MPC controller,  $r(k)$  is a reference for *all* the outputs (measured and unmeasured).

---

When the reference  $r$  is not known in advance, the current reference  $r(k)$  is used over the whole prediction horizon, namely  $r(k+i+1) = r(k)$  in Equation 2-3. In model predictive control the exploitation of future references is referred to as *anticipative action* (or *look-ahead* or *preview*). A similar anticipative action can

be performed with respect to measured disturbances  $v(k)$ , namely  $v(k+i)=v(k)$  if the measured disturbance is not known in advance (e.g. is coming from a Simulink block) or  $v(k+i)$  is obtained from the workspace. In the prediction,  $d(k+i)$  is instead obtained by setting  $n_d(k+i)=0$  in Figure 2-1 and Figure 2-2.

$w_{i,j}^{\Delta u}$ ,  $w_{i,j}^u$ ,  $w_{i,j}^y$  are nonnegative weights for the corresponding variable. The smaller  $w$ , the less important is the behavior of the corresponding variable to the overall performance index.

$u_{j,min}$ ,  $u_{j,max}$ ,  $\Delta u_{j,min}$ ,  $\Delta u_{j,max}$ ,  $y_{j,min}$ ,  $y_{j,max}$  are lower/upper bounds on the corresponding variables. In Equation 2-4, the constraints on  $u$ ,  $\Delta u$ , and  $y$  are relaxed by introducing the slack variable  $\epsilon \geq 0$ . The weight  $\rho_\epsilon$  on the slack variable  $\epsilon$  penalizes the violation of the constraints. The larger  $\rho_\epsilon$  with respect to input and output weights, the more the constraint violation is penalized. The Equal Concern for the Relaxation (ECR) vectors  $V_{min}^u$ ,  $V_{max}^u$ ,  $V_{min}^{\Delta u}$ ,  $V_{max}^{\Delta u}$ ,  $V_{min}^y$ ,  $V_{max}^y$  have nonnegative entries which represent the concern for relaxing the corresponding constraint; the larger  $V$ , the *softer* the constraint.  $V=0$  means that the constraint is a *hard* one that cannot be violated. By default, all input constraints are hard ( $V_{min}^u=V_{max}^u=V_{min}^{\Delta u}=V_{max}^{\Delta u}=0$ ) and all output constraints are soft ( $V_{min}^y=V_{max}^y=1$ ). As hard output constraints may cause infeasibility of the optimization problem (for instance, because of unpredicted disturbances, model mismatch, or just because of numerical round off), a warning message is produced if  $V_{min}^y$ ,  $V_{max}^y$  are smaller than a given small value and automatically adjusted at that value. By default,

$$\rho_\epsilon = 10^5 \max \left\{ w_{i,j}^{\Delta u}, w_{i,j}^u, w_{i,j}^y \right\} \quad (2-5)$$

Note that also ECRs can be time varying.

Vector  $u_{target}(k+i)$  is a setpoint for the input vector. One typically uses  $u_{target}$  if the number of inputs is greater than the number of outputs, as a sort of lower-priority setpoint.

As mentioned earlier, only  $\Delta u(k|k)$  is actually used to compute  $u(k)$ . The remaining samples  $\Delta u(k+i|k)$  are discarded, and a new optimization problem based on  $y_m(k+1)$  is solved at the next sampling step  $k+1$ .

The algorithm implemented in the Toolbox uses different procedures depending on the presence of constraints. If all the bounds are infinite, then the slack variable  $\epsilon$  is removed, and the problem in Equation 2-3 and Equation 2-4 is solved analytically. Otherwise a Quadratic Programming (QP) solver is used.

---

The matrices associated with the quadratic optimization problem are described in “QP Matrices” on page 2-12.

Since output constraints are always soft, the QP problem is never infeasible. If for numerical reasons the QP problem becomes infeasible, the second sample from the previous optimal sequence is applied, i.e.  $u(k)=u(k-1)+\Delta^* u(k | k-1)$ .

---

**Note** For reasons of numerical robustness, for constrained MPC problems the default value  $\Delta u_{j,min}$  for unbounded input rates is -10 and the maximum allowed lower bound is -1e5. The default value for unconstrained problems is minus infinity.

---

## State Estimation

As the states  $x(k)$ ,  $x_d(k)$  are not directly measurable, predictions are obtained from a state estimator. In order to provide more flexibility, the estimator is based on the model depicted in Figure 2-2.

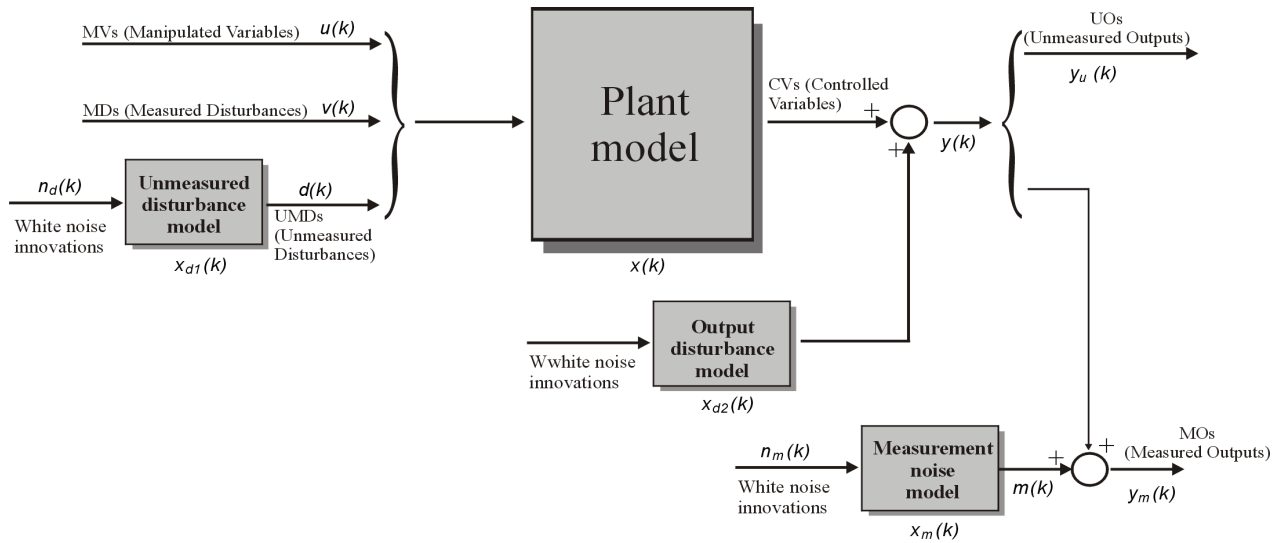


Figure 2-2: Model Used for State Estimation

### Measurement Noise Model

We assume that the measured output vector  $y_m(k)$  is corrupted by a measurement noise  $m(k)$ . The measurement noise  $m(t)$  is the output of the linear time-invariant system

$$x_m(k+1) = \tilde{A}x_m(k) + \tilde{B}n_m(k)$$

$$m(k) = \tilde{C}x_m(k) + \tilde{D}n_m(k).$$

The system described by these equations is driven by the random Gaussian noise  $n_m(k)$ , having zero mean and unit covariance matrix.



---

**Note** The objective of the MPC controller is to bring  $y_u(k)$  and  $[y_m(k)-m(k)]$  as close as possible to the reference vector  $r(k)$ . For this reason, the measurement noise model producing  $m(k)$  is not needed in the prediction model used for optimization described in “Prediction Model” on page 2-2.

---

## Output Disturbance Model

In order to guarantee asymptotic rejection of output disturbances, the overall model is augmented by an output disturbance model. By default, in order to reject constant disturbances due for instance to gain nonlinearities, the output disturbance model is a collection of integrators driven by white noise on measured outputs. Output integrators are added according to the following rule:

- 1 Measured outputs are ordered by decreasing output weight (in case of time-varying weights, the sum of the absolute values over time is considered for each output channel, and in case of equal output weight the order within the output vector is followed)
- 2 By following such order, an output integrator is added per measured outputs, unless there is a violation of observability, or the corresponding weight is zero, or the user forces it (through the `OutputVariables`. Integrators property described in “OutputVariables” on page 8-5).

An arbitrary output disturbance model can be specified through the function `setoutdist` on page 6-43. See also `setoutdist` on page 6-43 for ways to remove the default output integrators.

## State Observer

The state observer is designed to provide estimates of  $x(k)$ ,  $x_d(k)$ ,  $x_m(k)$ , where  $x(k)$  is the state of the plant model,  $x_d(k)$  is the overall state of the input and output disturbance model,  $x_m(k)$  is the state of the measurement noise model. The estimates are computed from the measured output  $y_m(k)$  by the linear state observer

$$\begin{bmatrix} \hat{x}(k|k) \\ \hat{x}_d(k|k) \\ \hat{x}_m(k|k) \end{bmatrix} = \begin{bmatrix} \hat{x}(k|k-1) \\ \hat{x}_d(k|k-1) \\ \hat{x}_m(k|k-1) \end{bmatrix} + M(y_m(k) - \hat{y}_m(k))$$

$$\begin{bmatrix} \hat{x}(k+1|k) \\ \hat{x}_d(k+1|k) \\ \hat{x}_m(k+1|k) \end{bmatrix} = \begin{bmatrix} A\hat{x}(k|k) + B_u u(k) + B_v v(k) + B_d \bar{C} \hat{x}_d(k|k) \\ \bar{A} \hat{x}_d(k|k) \\ \tilde{A} \hat{x}_m(k|k) \end{bmatrix}$$

$$\hat{y}_m(k) = C_m \hat{x}(k|k-1) + D_{vm} v(k) + D_{dm} \bar{C} \hat{x}_d(k|k-1) + \tilde{C} \hat{x}_m(k|k-1)$$

where “ $m$ ” denotes the rows of  $C, D$  corresponding to measured outputs.

To prevent numerical difficulties in the absence of unmeasured disturbances, the gain  $M$  is designed using Kalman filtering techniques (see the function `KALMAN` in the Control System Toolbox) on the extended model

$$\begin{bmatrix} x(k+1) \\ x_d(k+1) \\ x_m(k+1) \end{bmatrix} = \begin{bmatrix} A & B_d \bar{C} & 0 \\ 0 & \bar{A} & 0 \\ 0 & 0 & \tilde{A} \end{bmatrix} \begin{bmatrix} x(k) \\ x_d(k) \\ x_m(k) \end{bmatrix} + \begin{bmatrix} B_u \\ 0 \\ 0 \end{bmatrix} u(k) + \begin{bmatrix} B_v \\ 0 \\ 0 \end{bmatrix} v(k) + \begin{bmatrix} B_d \bar{D} & 0 & B_u & B_v \\ \bar{B} & 0 & 0 & 0 \\ 0 & \tilde{B} & 0 & 0 \end{bmatrix} \begin{bmatrix} n_d(k) \\ n_m(k) \\ n_u(k) \\ n_v(k) \end{bmatrix}$$

$$y_m(k) = \begin{bmatrix} C_m & D_{dm} \bar{C} & \tilde{C} \end{bmatrix} \begin{bmatrix} x(k) \\ x_d(k) \\ x_m(k) \end{bmatrix} + D_{vm} v(k) + \begin{bmatrix} \bar{D}_m & \tilde{D} & 0 & 0 \end{bmatrix} \begin{bmatrix} n_d(k) \\ n_m(k) \\ n_u(k) \\ n_v(k) \end{bmatrix} \quad \mathbf{(2-6)}$$

where  $n_u(k)$  and  $n_v(k)$  are additional unmeasured white noise disturbances having unit covariance matrix and zero mean, that are added on the vector of manipulated variables and the vector of measured disturbances, respectively, to ease the solvability of the Kalman filter design.

---

**Note** The overall state-space realization of the combination of plant and disturbance models must be observable for the state estimation design to succeed. The MPC Toolbox first checks for observability of the plant, provided that this is given in state-space form. After all models have been converted to discrete-time, delay-free, state-space form and combined together, observability of the overall extended model is checked (see the note on page 6-37 and “Construction and Initialization” on page 8-12).

Note also that observability is only checked numerically. Hence, for large models of badly conditioned system matrices, unobservability may be reported by the MPC Toolbox even if the system is observable.

---

See also `getestim` on page 6-11 and `setestim` on page 6-36 for details on the methods that you can use to access and modify properties of the state estimator.

## QP Matrices

This section describes the matrices associated with the MPC optimization problem described in “Optimization Problem” on page 2-5.

### Prediction

Assume for simplicity that the disturbance model in Equation 2-1 and Equation 2-2 is a unit gain (i.e.,  $d(k)=n_d(k)$  is a white Gaussian noise). For simplicity, denote by

$$x \leftarrow \begin{bmatrix} x \\ x_d \end{bmatrix}, A \leftarrow \begin{bmatrix} A & B_d \bar{C} \\ 0 & \bar{A} \end{bmatrix}, B_u \leftarrow \begin{bmatrix} B_u \\ 0 \end{bmatrix}, B_v \leftarrow \begin{bmatrix} B_v \\ 0 \end{bmatrix}, B_d \leftarrow \begin{bmatrix} B_d \bar{D} \\ \bar{B} \end{bmatrix}, C \leftarrow \begin{bmatrix} C & D_d \bar{C} \end{bmatrix}$$

Then, the prediction model given by

$$x(k+1) = Ax(k) + B_u u(k) + B_v v(k) + B_d n_d(k)$$

$$y(k) = Cx(k) + D_v v(k) + D_d n_d(k).$$

Consider for simplicity the prediction of the future trajectories of the model performed at time  $k=0$ . We set  $n_d(i)=0$  for all prediction instants  $i$ , and obtain

$$y(i|0) = C \left[ A^i x(0) + \sum_{h=0}^{i-1} \left( A^{i-1-h} B_u \left( u(-1) + \sum_{j=0}^h \Delta u(j) \right) + B_v v(h) \right) \right] + D_v v(i)$$

which gives

$$\begin{bmatrix} y(1) \\ \dots \\ y(p) \end{bmatrix} = S_x x(0) + S_{u1} u(-1) + S_u \begin{bmatrix} \Delta u(0) \\ \dots \\ \Delta u(p-1) \end{bmatrix} + H_v \begin{bmatrix} v(0) \\ \dots \\ v(p) \end{bmatrix}$$

where

$$S_x = \begin{bmatrix} CA \\ CA^2 \\ \dots \\ CA^p \end{bmatrix} \in \mathfrak{R}^{pn_y \times n_x}, S_{u1} = \begin{bmatrix} CB_u \\ CB_u + CAB_u \\ \dots \\ \sum_{h=0}^{p-1} CA^h B_u \end{bmatrix} \in \mathfrak{R}^{pn_y \times n_u}$$

$$S_u = \begin{bmatrix} CB_u & 0 & \dots & 0 \\ CB_u + CAB_u & CB_u & \dots & 0 \\ \dots & \dots & \dots & \dots \\ \sum_{h=0}^{p-1} CA^h B_u & \sum_{h=0}^{p-2} CA^h B_u & \dots & CB_u \end{bmatrix} \in \mathfrak{R}^{pn_y \times pn_u}$$

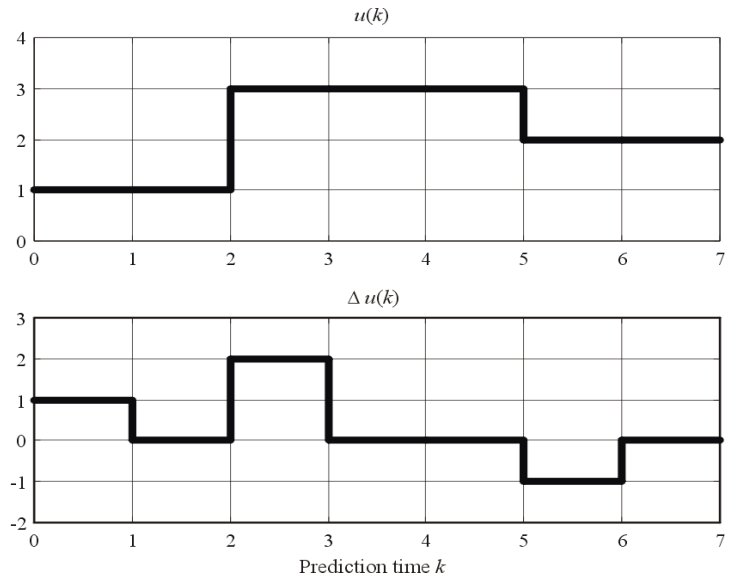
$$H_v = \begin{bmatrix} CB_v & D_v & 0 & \dots & 0 \\ CAB_v & CB_v & D_v & \dots & 0 \\ \dots & \dots & \dots & \dots & \dots \\ CA^{p-1}B_v & CA^{p-2}B_v & CA^{p-3}B_v & \dots & D_v \end{bmatrix} \in \mathfrak{R}^{pn_y \times (p+1)n_v}$$

## Optimization Variables

Let  $m$  be the number of free control moves and denote by  $z = [z_0; \dots; z_{m-1}]$ . Then,

$$\begin{bmatrix} \Delta u(0) \\ \dots \\ \Delta u(p-1) \end{bmatrix} = J_M \begin{bmatrix} z_0 \\ \dots \\ z_{m-1} \end{bmatrix} \quad (2-7)$$

where  $J_M$  depends on the choice of blocking moves. Together with the slack variable  $\epsilon$ , vectors  $z_0, \dots, z_{m-1}$  constitute the free optimization variables of the optimization problem (in case of systems with a single manipulated variables,  $z_0, \dots, z_{m-1}$  are scalars).



**Figure 2-3: Blocking Moves: Inputs and Input increments for moves=[2 3 2]**

Consider for instance the blocking moves depicted in Figure 2-3, which corresponds to the choice moves=[2 3 2], or, equivalently,

$$u(0)=u(1), \quad u(2)=u(3)=u(4), \quad u(5)=u(6), \quad \Delta u(0)=z_0, \quad \Delta u(2)=z_1, \quad \Delta u(5)=z_2, \quad \Delta u(1)=\Delta u(3)=\Delta u(4)=\Delta u(6)=0.$$

Then, the corresponding matrix  $J_M$  is

$$J_M = \begin{bmatrix} I & 0 & 0 \\ 0 & 0 & 0 \\ 0 & I & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & I \\ 0 & 0 & 0 \end{bmatrix}$$

## Cost Function

The function to be optimized is

$$\begin{aligned}
 J(z, \varepsilon) = & \left( \begin{bmatrix} u(0) \\ \dots \\ u(p-1) \end{bmatrix} - \begin{bmatrix} u_{\text{target}}(0) \\ \dots \\ u_{\text{target}}(p-1) \end{bmatrix} \right)^T W_u^2 + \left( \begin{bmatrix} u(0) \\ \dots \\ u(p-1) \end{bmatrix} - \begin{bmatrix} u_{\text{target}}(0) \\ \dots \\ u_{\text{target}}(p-1) \end{bmatrix} \right) \\
 & + \begin{bmatrix} \Delta u(0) \\ \dots \\ \Delta u(p-1) \end{bmatrix}^T W_{\Delta u}^2 \begin{bmatrix} \Delta u(0) \\ \dots \\ \Delta u(p-1) \end{bmatrix} \\
 & + \left( \begin{bmatrix} y(1) \\ \dots \\ y(p) \end{bmatrix} - \begin{bmatrix} r(1) \\ \dots \\ r(p) \end{bmatrix} \right)^T W_y^2 \left( \begin{bmatrix} y(1) \\ \dots \\ y(p) \end{bmatrix} - \begin{bmatrix} r(1) \\ \dots \\ r(p) \end{bmatrix} \right) + \rho_\varepsilon \varepsilon^2
 \end{aligned}$$

where

$$\begin{aligned}
 W_u &= \text{diag}(w_{0,1}^u, w_{0,2}^u, \dots, w_{0,n_u}^u, \dots, w_{p-1,1}^u, w_{p-1,2}^u, \dots, w_{p-1,n_u}^u) \\
 W_{\Delta u} &= \text{diag}(w_{0,1}^{\Delta u}, w_{0,2}^{\Delta u}, \dots, w_{0,n_u}^{\Delta u}, \dots, w_{p-1,1}^{\Delta u}, w_{p-1,2}^{\Delta u}, \dots, w_{p-1,n_u}^{\Delta u}) \\
 W_y &= \text{diag}(w_{1,1}^y, w_{1,2}^y, \dots, w_{1,n_y}^y, \dots, w_{p,1}^y, w_{p,2}^y, \dots, w_{p,n_y}^y)
 \end{aligned}$$

Finally, after substituting  $u(k)$ ,  $\Delta u(k)$ ,  $y(k)$ ,  $J(z)$  can be rewritten as

$$\begin{aligned}
 J(z, \varepsilon) = & \rho_\varepsilon \varepsilon^2 + z^T K_{\Delta u} z + 2 \left( \begin{bmatrix} r(1) \\ \dots \\ r(p) \end{bmatrix}^T K_r + \begin{bmatrix} v(0) \\ \dots \\ v(p) \end{bmatrix} K_v + u(-1)^T K_u \right. \\
 & \left. + \begin{bmatrix} u_{\text{target}}(0) \\ \dots \\ u_{\text{target}}(p-1) \end{bmatrix}^T K_{ut} + x(0)^T K_x \right) z + \text{constant}
 \end{aligned} \tag{2-8}$$

---

**Note** In order to keep the QP problem always strictly convex, if the condition number of the Hessian matrix  $K_{\Delta U}$  is larger than  $10^{12}$ , the quantity  $10 \cdot \sqrt{\epsilon}$  is added on each diagonal term. This may only occur when all input rates are not weighted ( $W^{\Delta u}=0$ ) (see note on page 8-8)

---

## Constraints

Let us now consider the limits on inputs, input increments, and outputs along with the constraint  $\epsilon \geq 0$

$$\begin{bmatrix} y_{min}(1) - \epsilon V^y_{min}(1) \\ \dots \\ y_{min}(p) - \epsilon V^y_{min}(p) \\ u_{min}(0) - \epsilon V^u_{min}(0) \\ \dots \\ u_{min}(p-1) - \epsilon V^u_{min}(p-1) \\ \Delta u_{min}(0) - \epsilon V^{\Delta u}_{min}(0) \\ \dots \\ \Delta u_{min}(p-1) - \epsilon V^{\Delta u}_{min}(p-1) \end{bmatrix} \leq \begin{bmatrix} y(1) \\ \dots \\ y(p) \\ u(0) \\ \dots \\ u(p-1) \\ \Delta u(0) \\ \dots \\ \Delta u(p-1) \end{bmatrix} \leq \begin{bmatrix} y_{max}(1) + \epsilon V^y_{max}(1) \\ \dots \\ y_{max}(p) + \epsilon V^y_{max}(p) \\ u_{max}(0) + \epsilon V^u_{max}(0) \\ \dots \\ u_{max}(p-1) + \epsilon V^u_{max}(p-1) \\ \Delta u_{max}(0) + \epsilon V^{\Delta u}_{max}(0) \\ \dots \\ \Delta u_{max}(p-1) + \epsilon V^{\Delta u}_{max}(p-1) \end{bmatrix}$$

---

**Note** Upper and lower bounds that are not finite are removed, as well as the input and input-increment bounds over blocked moves.

---

Similarly to what was done for the cost function, we can substitute  $u(k)$ ,  $\Delta u(k)$ ,  $y(k)$ , and obtain

$$M_z z + M_\epsilon \epsilon \leq M_{lim} + M_v \begin{bmatrix} v(0) \\ \dots \\ v(p) \end{bmatrix} + M_u u(-1) + M_x x(0) \quad (2-9)$$



where matrices  $M_z, M_\varepsilon, M_{\text{lim}}, M_v, M_u, M_x$  are obtained from the upper and lower bounds and ECR values.

The matrices of the QP problem are built in function `mpc_buildmat`.

## MPC Computation

This section describes how the MPC optimization problem is solved at each time step  $k$  (in `mpcmove`, `mpc_sfun.dll`, and `mpcloop_engine.dll`) by using the matrices built at initialization described in “QP Matrices” on page 2-12.

### Unconstrained MPC

The optimal solution is computed analytically:

$$z^* = -K^{-1} \Delta u \left( \begin{bmatrix} r(1) \\ \dots \\ r(p) \end{bmatrix}^T K_r + \begin{bmatrix} v(0) \\ \dots \\ v(p) \end{bmatrix} K_v + u(-1)^T K_u + \begin{bmatrix} u_{\text{target}}(0) \\ \dots \\ u_{\text{target}}(p-1) \end{bmatrix}^T K_{ut} + x(0)^T K_x \right)^T$$

and the MPC controller sets  $\Delta u(k)=z^*_0$ ,  $u(k)=u(k-1)+\Delta u(k)$ .

### Constrained MPC

The optimal solution  $z^*$ ,  $\epsilon^*$  is computed by solving the quadratic program described in Equation 2-8 and Equation 2-9, using the QP solver coded in the `qp solver.dll` function (see `qp dantz` on page 6-33 for more details).

## Using Identified Models

The MPC Toolbox is able to handle plant models generated by the System Identification Toolbox from input/output measurements.

The MPC Toolbox labels control input signals as ‘Manipulated’, measured input disturbances as ‘Measured’, and unmeasured input disturbances as ‘Unmeasured’. On the other hand, the System Identification Toolbox has a different naming rule, as it calls ‘Measured’ the inputs that are measurable quantities, and ‘Noise’ those that are not.

When you specify an identified model in the MPC constructor as the plant model, the MPC Toolbox treats ‘Noise’ signals as ‘Unmeasured’ input signals, and ‘Measured’ signals as ‘Manipulated’ signals, assuming that all measured inputs are also manipulated variables. You can later change later signal types, for instance to specify that some measured inputs are measured disturbances, rather than manipulated variables (See `setname` on page 6-42).

The MPC Toolbox internally converts the identified model you have provided as a plant model into the classical (A,B,C,D) state-space format. The columns of the B matrix originally related to ‘Noise’ channels are treated as the effect of unmeasured input disturbances on the state of the plant. On the other hand, the columns of the D matrix related to ‘Noise’ channels as treated as the effect of measurement noise superimposed on the output signal. Accordingly, the MPC Toolbox treats as the plant model the state-space model obtained from (A,B,C,D) by zeroing the columns of D related to ‘Noise’ channels. Those columns are instead used as a static noise model, or cascaded to an existing noise model if you have specified one. A unit static gain is assumed as the disturbance model, unless you have specified another one.



# MPC Simulink Library

---

MPC Controller Block (p. 3-2)

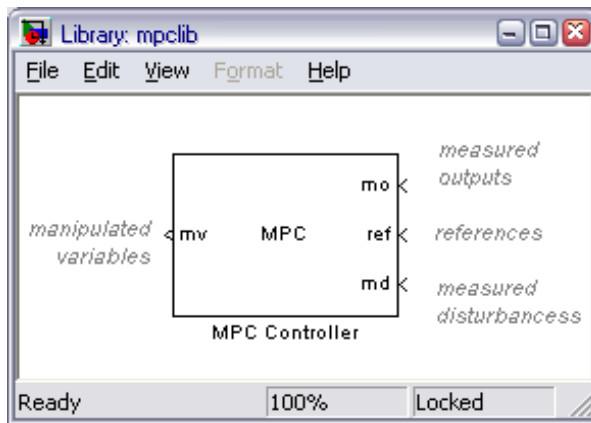
A discussion of the Simulink block representing an MPC controller as defined by an MPC object.

## MPC Controller Block

### Opening the Library

The MPC Simulink Library provides a single block representing the MPC controller.

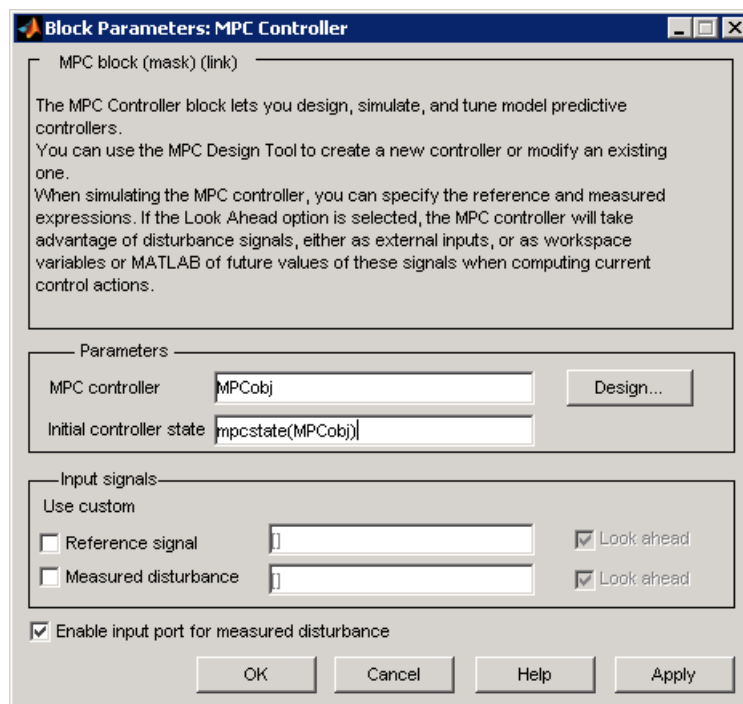
The library can be opened from the main Simulink library or by typing `mpclib` from the command prompt.



**Figure 3-1: MPC Simulink Library**

After copying the MPC Controller block in your diagram, you can double-click on the block and open the mask window.

## MPC Controller Block Mask



**Figure 3-2: MPC Controller Block Mask**

The mask requires that you specify a valid MPC controller object. There are three ways of providing an MPC controller object:

- 1** In the **MPC controller** edit box, enter the name of an MPC object that exists in the workspace
- 2** Enter the name of an MPC object that exists in the workspace and then click the **Design** button to open the MPC Design Tool and design the MPC controller object there.
- 3** Click the **Design** button without specifying an MPC controller object. The MPC Controller block prompts you to enter the number of manipulated variables then will automatically to construct a default MPC controller by

linearizing the plant model from the Simulink diagram. This option requires Simulink Control Design. See “Importing a Plant Model” on page 5-9 for more information about creating linearized plant models with the MPC Toolbox. Refer to the Simulink Control Design documentation for more information about the linearization process.

---

**Note** Closed-loop simulations can be run while the MPC controller is edited in the MPC Design Tool. In this case, the controller parameters used for simulating the Simulink diagram are those currently specified in the MPC Design Tool, so that the parameters of the controller can be more easily tuned. Once the MPC Design Tool is closed, the designed controller must be exported as an MPC object to the workspace in order to be used in simulation.

---

## Look Ahead and Signals from the Workspace

Reference and measured disturbance signals, by default, are taken from the Simulink diagram. They can be taken instead from the workspace. In this case, store the signal in a structure having the same format as used in the Simulink **From Workspace** and **To Workspace** blocks. This requires two fields: `time` and `signals`.

For example, to specify the sinusoidal reference signal  $\sin(t)$  over a time horizon of 10 seconds, assuming an MPC controller’s sampling time  $T_s$ , use

```
time=(0:Ts:10);  
ref.time=time;  
ref.signals.values=sin(time);
```

An alternative would be to run a separate Simulink simulation to create the stored signal. Use the blocks required to define the signal (e.g., **Sine** in the above example), and store the result using a **To Workspace** block.

The **Look ahead** check box enables an anticipative action on the corresponding signal. It can only be enabled if the signal comes from the workspace.

See the demo `mpcpreview` for an illustrative example of enabling preview and reading signals from the workspace.



## Initialization

The initial controller state must be a valid `mpcstate` object. See “MPC State Object” on page 8-13.

## Using the MPC Toolbox with Real-Time Workshop®

The C sources of the S-function executing the MPC Controller Block code are available in the `mpcutils/src` directory. You can build a real-time executable by pressing **Ctrl+B** on your Simulink diagram to invoke Real-Time Workshop and build the model.

In some cases, it is necessary to copy the source files (`mpc_sfun.c`, `mpc_sfun.h`, `mpc_common.c`, `mat_macros.h`, `dantzgmp.h`, `dantzgmp_solver.c`) to a visible directory, such as the current directory '.', or 'C:\MATLAB\rtw\c\src'.

The MPC Controller Block can be also used to produce real-time executables that run under xPC Target.



# Case-Study Examples

---

This chapter describes some typical MPC applications. Familiarity with LTI models (from the Control System Toolbox) and Simulink block diagrams will make the examples easier to understand, but you can skip the modeling details if you wish.

The first example designs a servomechanism controller. The specifications require a fast servo response despite constraints on a plant input and a plant output.

The second example controls a paper machine headbox. The process is nonlinear, and has three outputs, two manipulated inputs, and two disturbance inputs, one of which is measured for feedforward control.

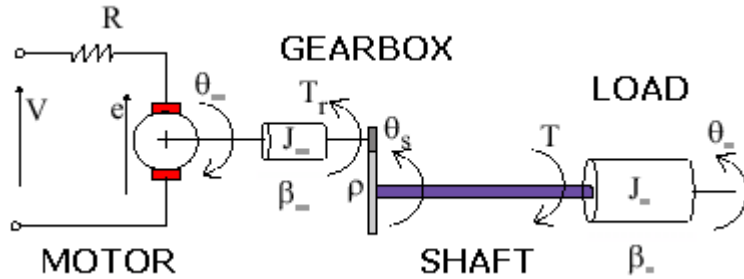
Servomechanism Controller (p. 4-2)

MPC Toolbox design of a servomechanism. Uses MPCTOOL GUI and commands.

Paper Machine Process Control  
(p. 4-30)

Application to a paper machine headbox. Involves multiple signals. Illustrates use of MPCTOOL GUI and Simulink.

## Servomechanism Controller



**Figure 4-1: Position Servomechanism Schematic**

### System Model

A position servomechanism consists of a DC motor, gearbox, elastic shaft, and a load (see Figure 4-1). The differential equations representing this system are

$$\dot{\omega}_L = -\frac{k_\theta}{J_L} \left( \theta_L - \frac{\theta_M}{\rho} \right) - \frac{\beta_L}{J_L} \omega_L$$

$$\dot{\omega}_M = \frac{k_T}{J_M} \left( \frac{V - k_T \omega_M}{R} \right) - \frac{\beta_M \omega_M}{J_M} + \frac{k_\theta}{\rho J_M} \left( \theta_L - \frac{\theta_M}{\rho} \right)$$

where  $V$  is the applied voltage,  $T$  is the torque acting on the load,  $\omega_L = \dot{\theta}_L$  is the load's angular velocity,  $\omega_M = \dot{\theta}_M$  is the motor shaft's angular velocity, and the other symbols represent constant parameters (see Table 4-1 for more information on these).

If we define the state variables as  $x_p = [\theta_L \ \omega_L \ \theta_M \ \omega_M]^T$ , we can convert the above model to an LTI state-space form:

$$\dot{x}_p = \begin{bmatrix} 0 & 1 & 0 & 0 \\ \frac{k_\theta}{J_L} & \frac{\beta_L}{J_L} & \frac{k_\theta}{\rho J_L} & 0 \\ 0 & 0 & 0 & 1 \\ \frac{k_\theta}{\rho J_M} & 0 & -\frac{k_\theta}{\rho^2 J_M} & -\frac{\beta_M + k_T^2/R}{J_M} \end{bmatrix} x_p + \begin{bmatrix} 0 \\ 0 \\ 0 \\ \frac{k_T}{R J_M} \end{bmatrix} V$$

$$\theta_L = [1 \ 0 \ 0 \ 0] x_p$$

$$T = \left[ k_\theta \ 0 \ -\frac{k_\theta}{\rho} \ 0 \right] x_p$$

**Table 4-1: Parameters Used in the Servomechanism Model**

Symbol	Value (SI units)	Definition
$k_\theta$	1280.2	Torsional rigidity
$k_T$	10	Motor constant
$J_M$	0.5	Motor inertia
$J_L$	$50J_M$	Nominal load inertia
$\rho$	20	Gear ratio
$\beta_M$	0.1	Motor viscous friction coefficient
$\beta_L$	25	Load viscous friction coefficient
$R$	20	Armature resistance

## Control Objectives and Constraints

The controller must set the load's angular position,  $\theta_L$ , at a desired value by adjusting the applied voltage,  $V$ . The only measurement available for feedback is  $\theta_L$ .

The elastic shaft has a finite shear strength, so the torque,  $T$ , must stay within specified limits

$$|T| \leq 78.5 \text{ Nm}$$

Also, the applied voltage must stay within the range

$$|V| \leq 220 \text{ V}$$

From an input/output viewpoint, the plant has a single input,  $V$ , which is manipulated by the controller. It has two outputs, one measured and fed back to the controller,  $\theta_L$ , and one unmeasured,  $T$ .

## Defining the Plant Model

The first step in a design is to define the plant model. The following commands are from the mpcdemos file `motor_model.m`, which you can run instead of entering the commands manually.

```
% DC-motor with elastic shaft
%
%Parameters (MKS)
%-----
Lshaft=1.0;      %Shaft length
dshaft=0.02;    %Shaft diameter
shaftrho=7850;  %Shaft specific weight (Carbon steel)
G=81500*1e6;    %Modulus of rigidity
tauam=50*1e6;  %Shear strength
Mmotor=100;     %Rotor mass
Rmotor=.1;      %Rotor radius
Jmotor=.5*Mmotor*Rmotor^2; %Rotor axial moment of inertia
Bmotor=0.1;     %Rotor viscous friction coefficient (A CASO)
R=20;           %Resistance of armature
Kt=10;          %Motor constant
```

```

gear=20;           %Gear ratio
Jload=50*Jmotor;  %Load NOMINAL moment of inertia
Bload=25;         %Load NOMINAL viscous friction coefficient
Ip=pi/32*dshaft^4;           %Polar momentum of shaft
(circular) section
Kth=G*Ip/Lshaft;           %Torsional rigidity
(Torque/angle)
Vshaft=pi*(dshaft^2)/4*Lshaft; %Shaft volume
Mshaft=shaftrho*Vshaft;    %Shaft mass
Jshaft=Mshaft*.5*(dshaft^2/4); %Shaft moment of inertia
JM=Jmotor;
JL=Jload+Jshaft;
Vmax=tauam*pi*dshaft^3/16; %Maximum admissible torque
Vmin=-Vmax;

%Input/State/Output continuous time form
%-----
%-----
AA=[0           1           0           0;
    -Kth/JL     -Bload/JL    Kth/(gear*JL)  0;
     0           0           0           1;
     Kth/(JM*gear)  0         -Kth/(JM*gear^2)
    -(Bmotor+Kt^2/R)/JM];

BB=[0;0;0;Kt/(R*JM)];
Hyd=[1 0 0 0];
Hvd=[Kth 0 -Kth/gear 0];
Dyd=0;
Dvd=0;

% Define the LTI state-space model
sys=ss(AA,BB,[Hyd;Hvd],[Dyd;Dvd]);

```

## Controller Design Using MPCTOOL

The servomechanism model is linear, so you can use the MPC Toolbox design tool (`mpctool`) to configure a controller and test it.

---

**Note** To follow this example on your own system, first create the servomechanism model as explained above. This defines the variable `sys` in your MATLAB workspace.

---

### Opening MPCTOOL and Importing a Model

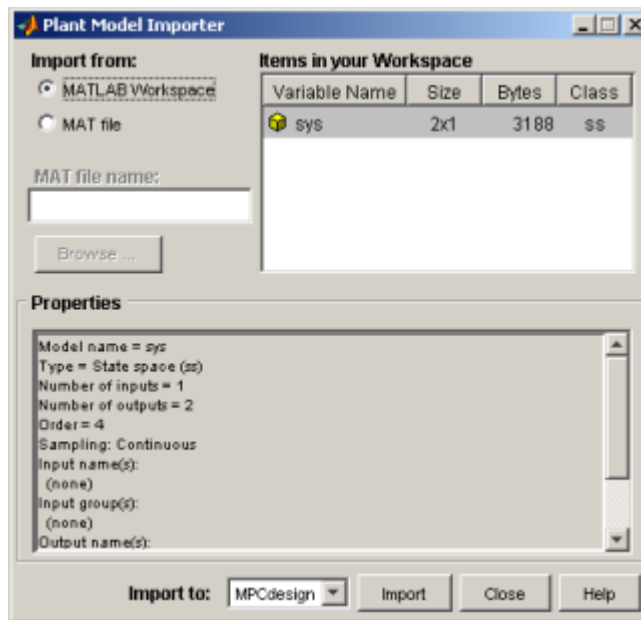
To begin, open the design tool by typing the following at the MATLAB prompt:

```
mpctool
```

Once the design tool has appeared, click the **Import Plant** button. The **Plant Model Importer** will appear (see Figure 4-2).

By default, the **Import from** radio buttons are set to import from the MATLAB workspace, and the box at the upper right lists all LTI models defined there. In Figure 4-2, `sys` is the only available model, and it is selected. The **Properties** window lists the selected model's key attributes.



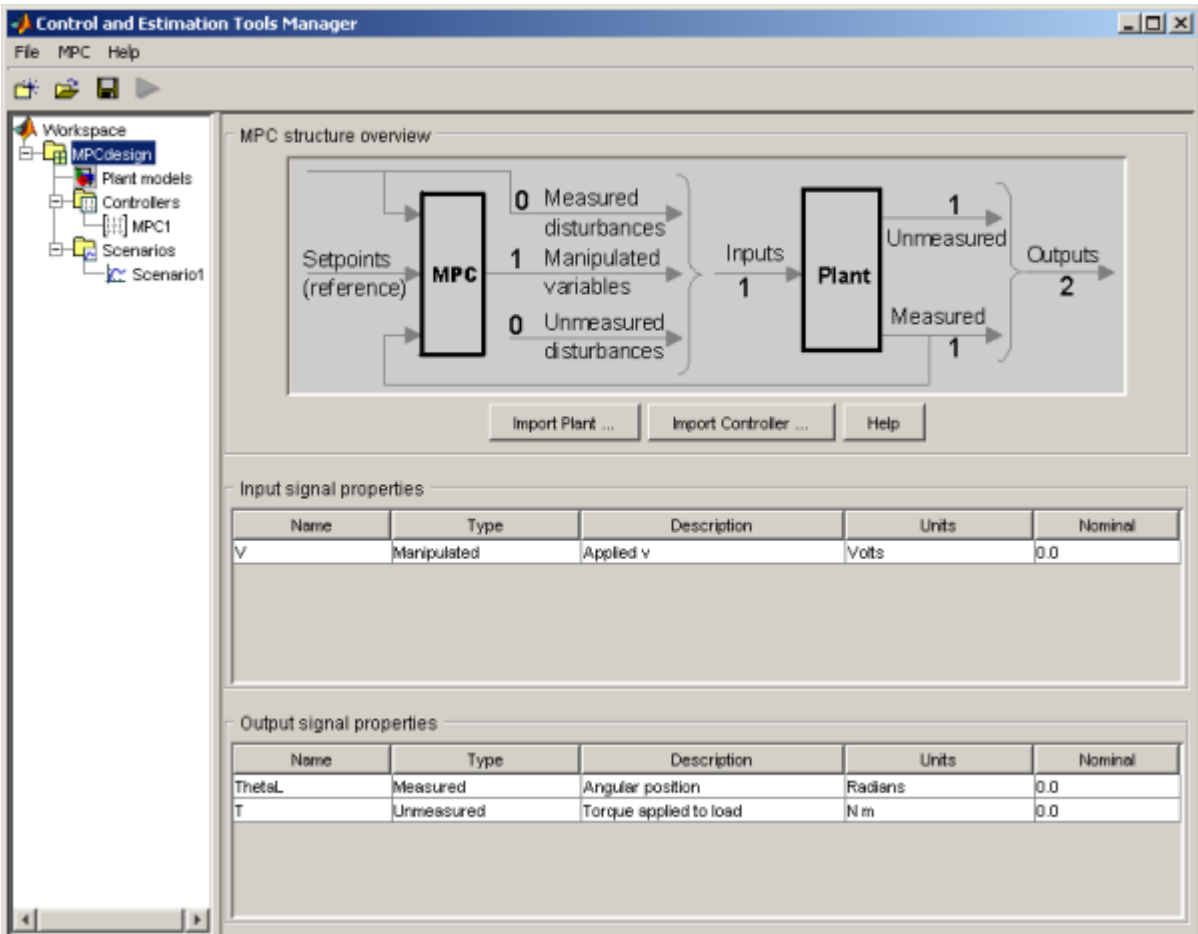


**Figure 4-2: Import Dialog with the Servomechanism Model Selected**

Make sure your servomechanism model, `sys`, is selected. Then click the **Import** button. Your model loads, and tables appear in the design tool's main window (see Figure 4-3). The diagram at the top shows the number of inputs and outputs in your model.

### Specifying Signal Properties

It's essential to specify *signal types* before going on. By default, the design tool assumes all plant inputs are manipulated, which is correct in this case. But it also assumes all outputs are measured, which is not. Specify that the second output is unmeasured by clicking on the appropriate table cell and selecting the **Unmeasured** option.



**Figure 4-3: Design Tool After Importing the Plant Model and Specifying Signal Properties**

You also have the option to change the default signal names (In1, Out1, Out2) to something more meaningful (e.g., V, ThetaL, T), enter descriptive information in the blank **Description** and **Units** columns, and specify a nominal initial value for each signal (the default is zero).

After you've entered all your changes, you should see a view similar to Figure 4-3. Notice that the graphic shows the effect of designating one output as measured, the other unmeasured.

### Navigation Using the Tree View

Now consider the design tool's left-hand frame. This *tree* is an ordered arrangement of *nodes*. By default, the *root* node is named **MPCdesign**, and is selected when the design tool starts. Whenever you select the root node, the starting view shown in Figure 4-3 reappears.

The **Plant models** node is next in the hierarchy. Click on it to list the plant models being used in your design. (Each model name is editable.) The middle section displays the selected model's properties. There is also a space to enter notes describing the model's special features. Buttons allow you to import a new model or delete one you no longer need.

The next node is **Controllers**. You might see a + sign to its left, indicating that it contains subnodes. If so, click on the + sign to expand the tree (as shown in Figure 4-3). All the controllers in your design will appear here. By default, you have one: **MPC1**. In general, you might opt to design and test several alternatives.

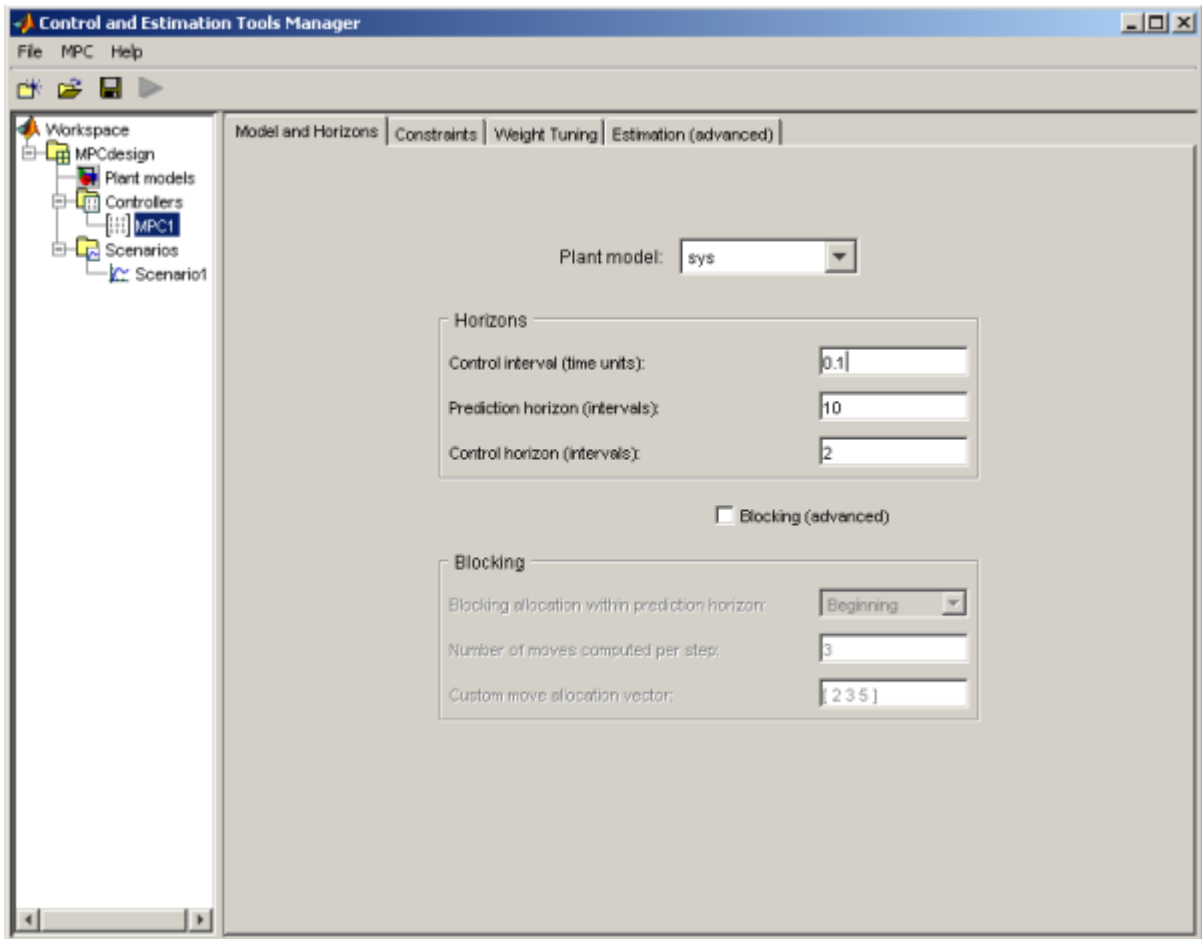
Select **Controllers** to see a list of all controllers, similar to the **Plant models** view. The table columns show important controller settings: the plant model being used, the controller sampling period, and the prediction and control horizons. All are editable. For now, leave them at their default values.

The buttons on the **Controllers** view allow you to:

- **Import** a controller designed previously and stored either in your workspace or in a MAT-file
- **Export** the selected controller to your workspace
- Create a **New** controller, which will be initialized to the MPC Toolbox defaults
- **Copy** the selected controller to create a duplicate that you can modify
- **Delete** the selected controller

## Specifying Controller Properties

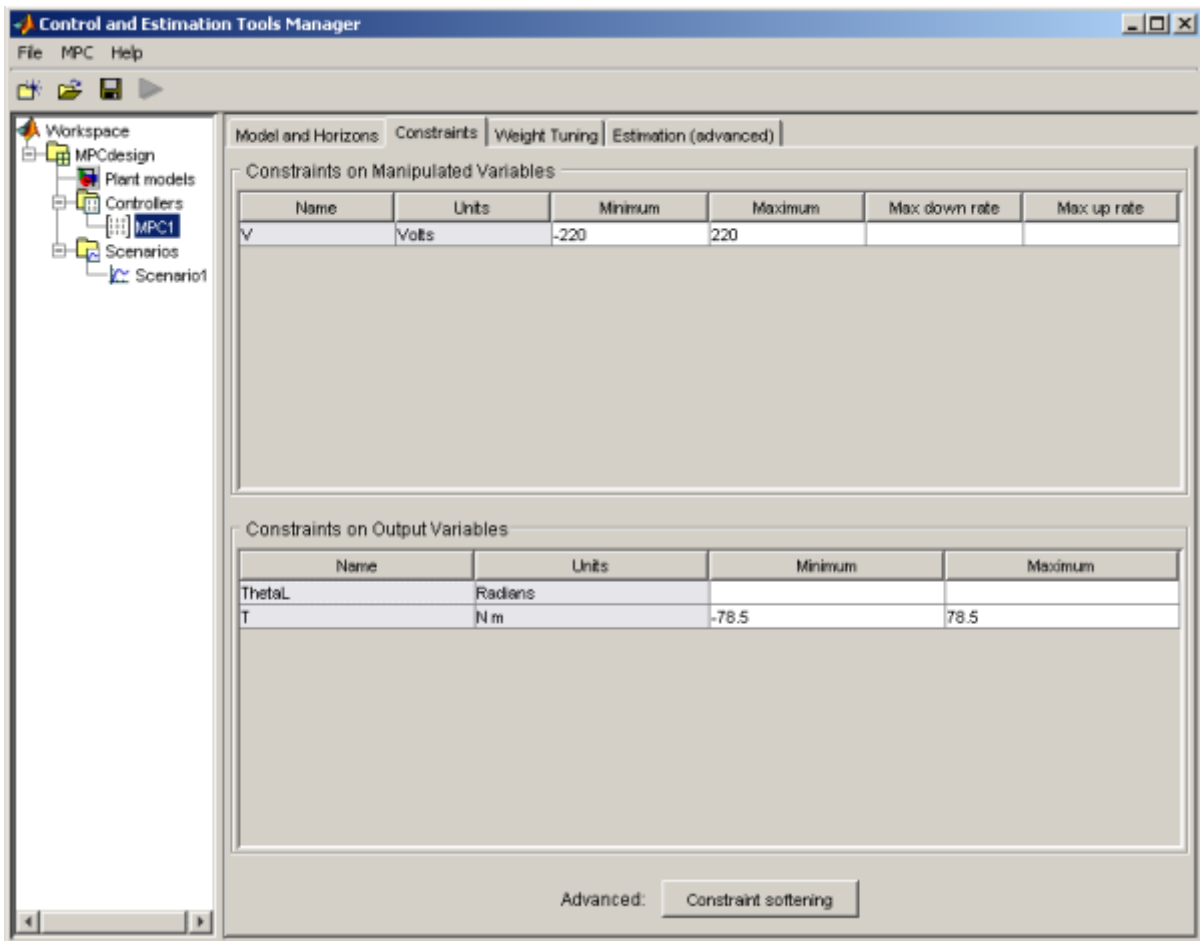
Select the **MPC1** subnode. The main panel should change to the MPC design view shown in Figure 4-4.



**Figure 4-4: Controller Design View, Models and Horizons Pane**

If the selected **Prediction model** is continuous-time, as in this example, the **Control interval** (sampling period) defaults to 1. You need to change this to an

application-appropriate value. Set it to 0.1 seconds (as shown in Figure 4-4). Leave the other values at their defaults for now.



**Figure 4-5: Controller Design View, Constraints Pane**

### Specifying Constraints

Next, select the **Constraints** tab. The view shown in Figure 4-5 appears. Enter the appropriate constraint values. Leaving a field blank implies that there is no constraint.

In general, it's good practice to include all known manipulated variable constraints, but it's unwise to enter constraints on outputs unless they are an essential aspect of your application. The limit on applied torque is such a constraint, as are the limits on applied voltage. The angular position has physical limits, the controller shouldn't attempt to enforce them, so you should leave the corresponding fields blank (see Figure 4-5)

The **Max down rate** should be nonpositive (or blank). It limits the amount a manipulated variable can decrease in a single control interval. Similarly, the **Max up rate** should be nonnegative. It limits the increasing rate. Leave both unconstrained (i.e., blank).

The shaded columns can't be edited. If you want to change this descriptive information, select the root node view and edit its tables. (Such changes apply to all controllers in the design.)

### Weight Tuning

Next, select the **Weight Tuning** tab to obtain a view like that shown in Figure 4-6.

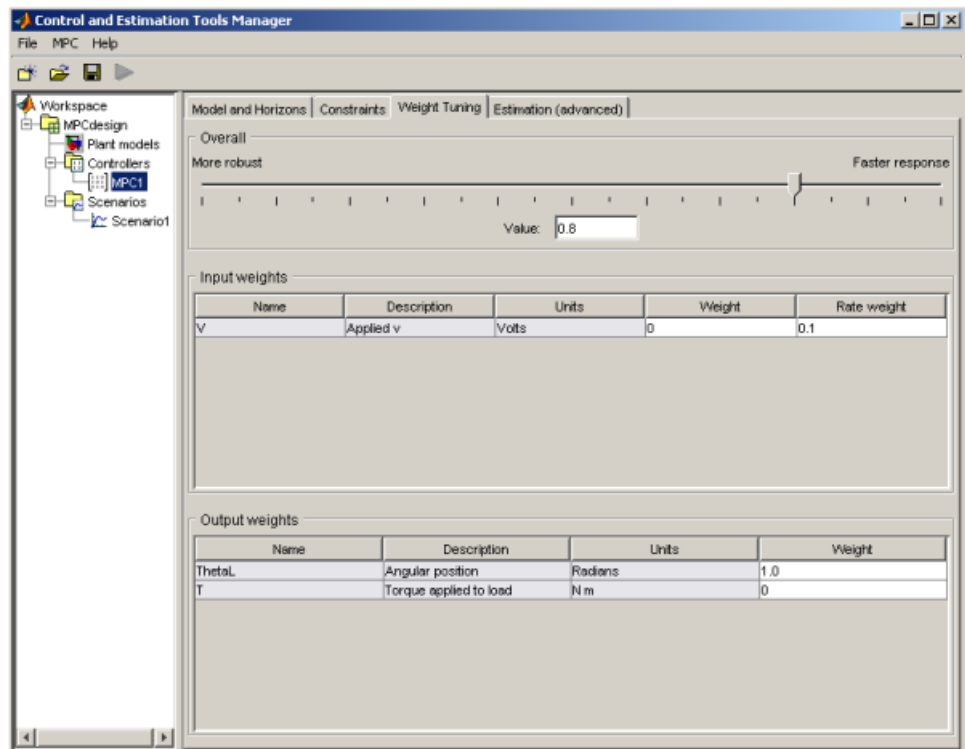
The *weights* specify trade-offs in the controller design. First consider the **Output weights**. The controller will try to minimize the deviation of each output from its *setpoint* or *reference* value. For each sampling instant in the prediction horizon, the controller multiplies predicted deviations for each output by the output's weight, squares the result, and sums over all sampling instants and all outputs. One of the controller's objectives is to minimize this sum, *i.e.*, to provide good *setpoint tracking* (See "Optimization Problem" on page 2-5 for more details.)

Here, the angular position should track its setpoint, but the applied torque can vary, provided that it stays within the specified constraints. Therefore, set the torque's weight to zero, which tells the controller that setpoint tracking is unnecessary for this output.

Similarly, it's acceptable for the applied voltage to deviate from nominal (it must in order to change the angular position!). Its weight should be zero (the default for manipulated variables). On the other hand, it's probably

undesirable for the controller to make drastic changes in the applied voltage. The **Rate weight** penalizes such changes. Use the default, 0.1.

When setting the rates, the relative magnitudes are more important than the absolute values, and you must account for differences in the measurement scales of each variable. For example, if a deviation of 0.1 units in variable A is just as important as a deviation of 100 units in variable B, variable A's weight must be 1000 times larger than that for variable B.

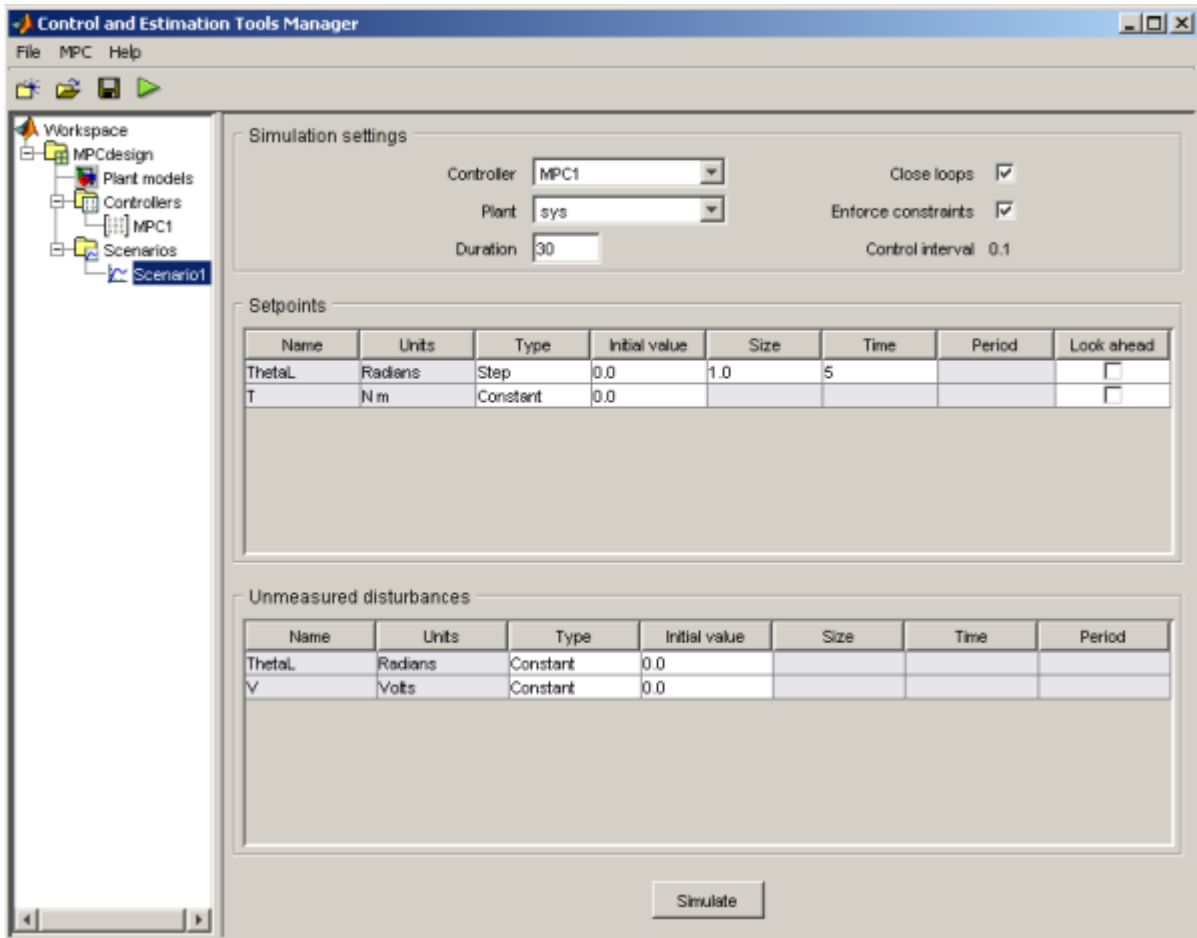


**Figure 4-6: Controller Design View, Weight Tuning Pane**

The tables allow you to weight individual variables. The slider at the top adjusts an overall trade-off between controller action and setpoint tracking. Moving the slider to the left places a larger overall penalty on manipulated

variable changes. This usually increases controller robustness, but setpoint tracking becomes more sluggish.

The **Estimation** tab allows you to adjust the controller’s response to unmeasured disturbances (not used in this example).



**Figure 4-7: Simulation Settings View for “Scenario1”**



### Defining a Simulation Scenario

If you haven't already done so, expand the **Scenarios** node to show the **Scenario1** subnode (see Figure 4-3). Select **Scenario1** to obtain the view shown in Figure 4-7.

A *scenario* is a set of simulation conditions. As shown in Figure 4-7, you choose the controller to be used (from among controllers in your design), the model to act as the plant, and the simulation duration.

You must also specify all setpoints and disturbance inputs.

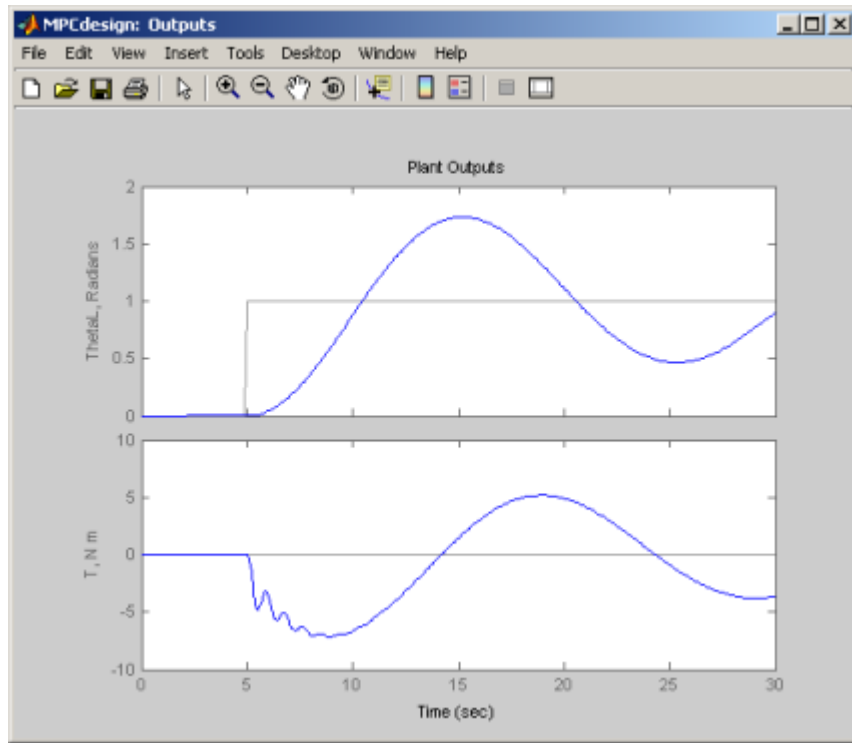
Duplicate the settings shown in Figure 4-7, which will test the controller's servo response to a unit-step change in the angular position setpoint. All other inputs are being held constant at their nominal values.

---

**Note** The **ThetaL** and **V** unmeasured disturbances allow you to simulate additive disturbances to these variables. By default, these disturbances are turned off, i.e., zero.

---

The **Look ahead** option designates that all future setpoint variations are known. In that case, the controller can adjust the manipulated variable(s) in advance to improve setpoint tracking. This would be unusual in practice, and is not being used here.



**Figure 4-8: Response to Unit Step in the Angular Position Setpoint**

### Running a Simulation

Once you're ready to run the scenario, click the **Simulate** button or the green arrow on the tool bar.

---

**Note** The green arrow tool is available from any view once you've defined at least one scenario. It runs the *active scenario*, i.e., the one most recently selected or modified.

---

We obtain the results shown in Figure 4-8. The blue curves are the output signals, and the gray curves are the corresponding setpoints. The response is very sluggish, and hasn't settled within the 30 second simulation period.

---

**Note** The plot shown in Figure 4-8 provides many of the customization features available in the Control System Toolbox `ltiview` and `sisotool` displays. Try clicking on a curve to obtain the numerical characteristics of the selected point, or right-clicking in the plot area to obtain a customization menu.

---

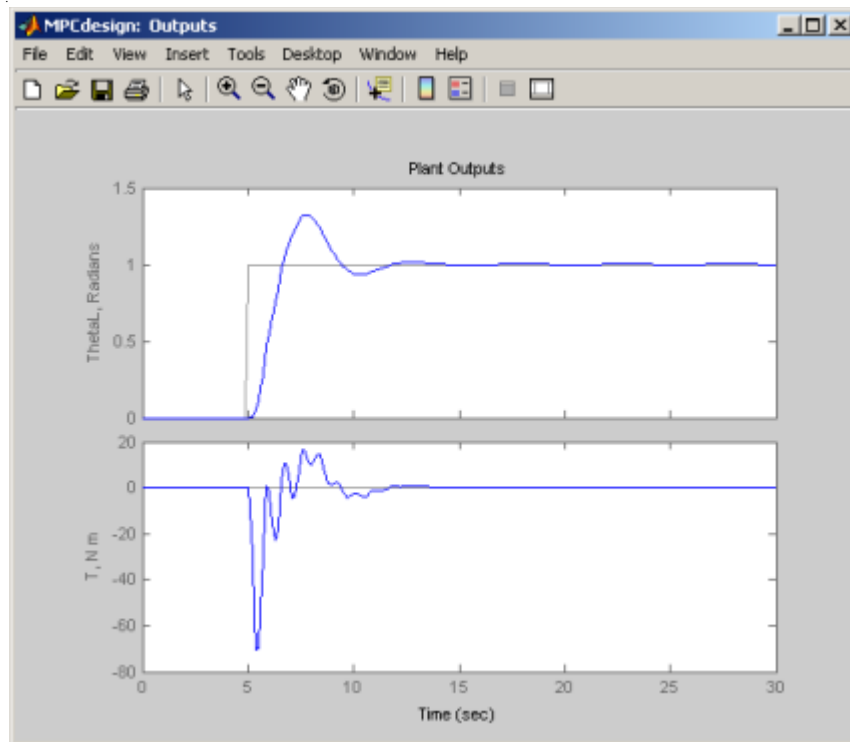
The corresponding applied voltage adjustments appear in a separate window (not shown) and are also very sluggish.

On the positive side, the applied torque stays well within bounds, as does the applied voltage.

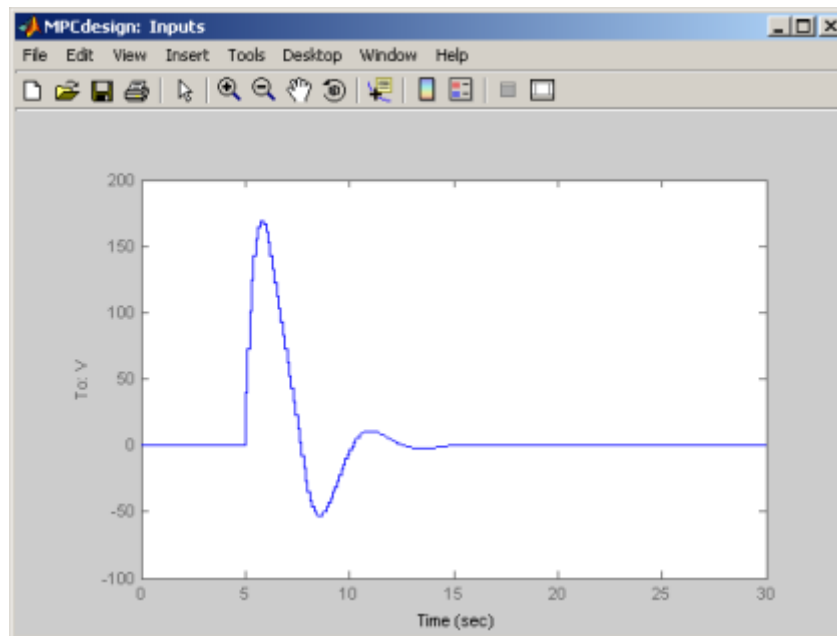
### **Retuning to Achieve a Faster Servo Response**

To obtain a more rapid servo response, navigate to the **MPC1 Weight Tuning** pane (select the **MPC1** node to get the controller design view, then select the **Weight Tuning** tab) and move the slider all the way to the right. Then click on the green arrow in the tool bar. Your results should now resemble Figure 4-9 and Figure 4-10.

The angular position now settles within 10 seconds following the step. The torque approaches its lower limit, but doesn't exceed it (see Figure 4-9) and the applied voltage stays within its limits (See Figure 4-10).



**Figure 4-9: Faster Servo Response**

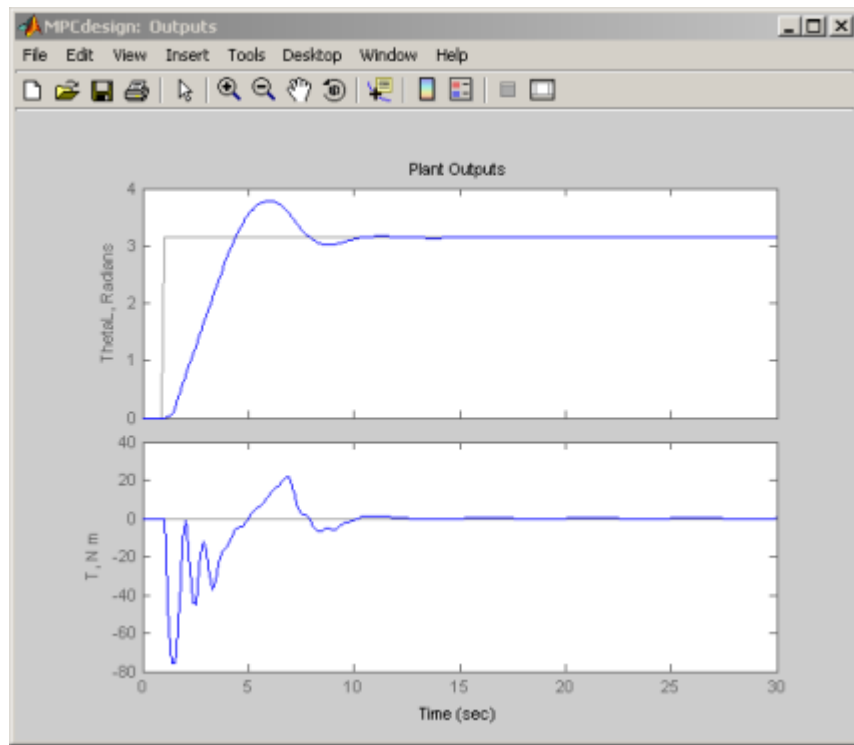


**Figure 4-10: Manipulated Variable Adjustments Corresponding to Figure 4-9**

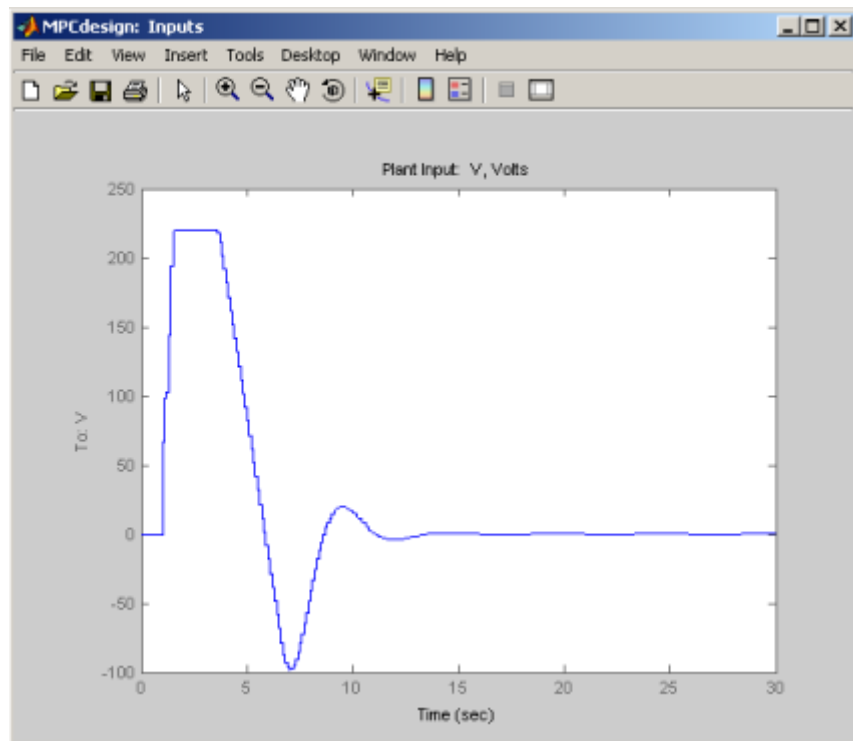
### Modifying the Scenario

Finally, increase the step size to  $\pi$  radians (select the **Scenario1** node and edit the tabular value).

As shown in Figure 4-11 and Figure 4-12, the servo response is essentially as good as before, and we avoid exceeding the torque constraint at  $-78.5$  Nm, even though the applied voltage is saturated for about 2.5 seconds (see Figure 4-12).



**Figure 4-11: Servo Response for Step Increase of  $\pi$  Radians**



**Figure 4-12: Voltage Adjustments Corresponding to Figure 4-11.**

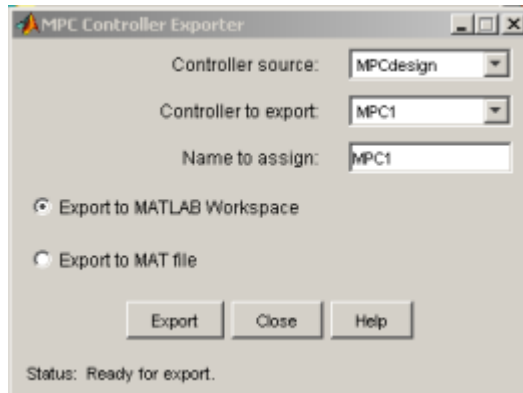
### Saving Your Work

Once you're satisfied with a controller's performance, you can export it to the workspace, for use in a Simulink block diagram or for analysis (or you can save it in a MAT-file).

To export a controller, right-click on its node and select **Export** from the resulting menu (or select the **Controllers** node, select the controller in the list, and click the **Export** button). A dialog like that shown in Figure 4-13 will appear.

The **Controller source** is the design from which you wish to extract a controller. There's only one in this example, but in general you could be working on several simultaneously. The **Controller to export** choice defaults to the controller most recently selected. Again, there's no choice in this case,

but there could be in general. The **Name to assign** edit box allows you to rename the exported controller. (This will not change its in the design tool.)



**Figure 4-13: Exporting a Controller to the Workspace**

---

**Note** When you exit the design tool you will be prompted to save the entire design in a MAT file. This allows you to reload it later using the **File/Load** menu option or the **Load** icon on the tool bar.

---

## Using MPC Toolbox Commands

Once you’ve become familiar with the toolbox, you may find it more convenient to build a controller and run a simulation using commands.

For example, suppose that you’ve already defined the model as discussed in “Defining the Plant Model” on page 4-4. Consider the following command sequence:

```
ManipulatedVariables = struct('Min', -220, 'Max', 220, 'Units',  
    'V');  
OutputVariables(1) = struct('Min', -Inf, 'Max', Inf, 'Units',  
    'rad');  
OutputVariables(2) = struct('Min', -78.5, 'Max', 78.5, 'Units',  
    'Nm');  
Weights = struct('Input', 0, 'InputRate', 0.05, 'Output', [10 0]);
```



```

Model.Plant = sys;
Model.Plant.OutputGroup = {[1], 'Measured' ; [2], 'Unmeasured'};
Ts = 0.1;
PredictionHorizon = 10;
ControlHorizon = 2;

```

This creates several *structure* variables. For example, `ManipulatedVariables` defines the display units and constraints for the applied voltage (the manipulated plant input). `Weights` defines the tuning weights shown in Figure 4-6 (but the numerical values used here provide better performance). `Model` designates the plant model (stored in `sys`, which we defined earlier). The code also sets the `Model.Plant.OutputGroup` property to designate the second output as unmeasured.

### Constructing an MPC Object

Use the `mpc` command to construct an MPC object called `ServoMPC`:

```
ServoMPC = mpc(Model, Ts, PredictionHorizon, ControlHorizon);
```

Like the LTI objects used to define linear, time-invariant dynamic models, an MPC object contains a complete definition of a controller.

### Setting, Getting, and Displaying Object Properties

Once you've constructed an MPC object, you can change its properties as you would for other objects. For example, to change the prediction horizon, you could use one of the following commands:

```
ServoMPC.PredictionHorizon = 12;
```

or

```
set(ServoMPC, 'PredictionHorizon', 12);
```

For a listing of all the object's properties, you could type

```
get(ServoMPC)
```

To access a particular one (e.g., the control horizon), you could type

```
M = get(ServoMPC, 'ControlHorizon');
```

or

```
M = ServoMPC.ControlHorizon;
```

You can also set multiple properties simultaneously.

Set the following properties before continuing with this example:

```
set(ServoMPC, 'Weights', Weights, ...  
    'ManipulatedVariables', ManipulatedVariables, ...  
    'OutputVariables', OutputVariables);
```

Typing the name of an object without a terminating semicolon generates a formatted display of the object's properties. You can achieve the same effect using the display command:

```
display(ServoMPC)
```

### Running a Simulation

The `sim` command performs a linear simulation. For example, the following code sequence defines constant setpoints for the two outputs, then runs a simulation.

```
TimeSteps = round(10/Ts);  
r = [pi 0];  
[y, t, u] = sim(ServoMPC, TimeSteps, r);
```

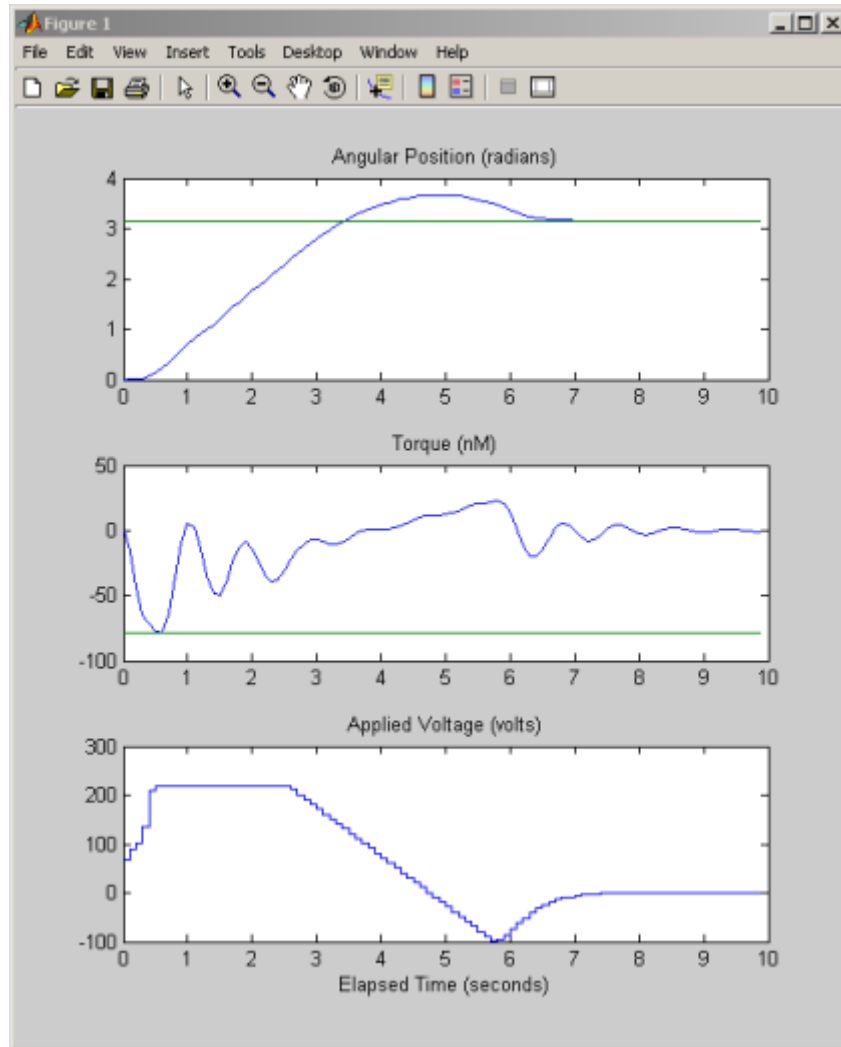
By default, the model used to design the controller (stored in `ServoMPC`) also represents the plant.

The `sim` command saves the output and manipulated variable sequences in variables `y` and `u`. For example,

```
subplot(311)  
plot(t, y(:,1), [0 t(end)], pi*[1 1])  
title('Angular Position (radians)');  
subplot(312)  
plot(t, y(:,2), [0 t(end)], [-78.5 -78.5])  
title('Torque (nM)')  
subplot(313)  
stairs(t, u)  
title('Applied Voltage (volts)')  
xlabel('Elapsed Time (seconds)')
```

produces the custom plot shown in Figure 4-14. The plot includes the angular position's setpoint. The servo response settles within 5 seconds with no overshoot. It also displays the torque's lower bound, which activates after about

0.9 second, but isn't exceeded. The applied voltage saturates between about 0.5 and 2.8 seconds, but the controller performs well despite this.

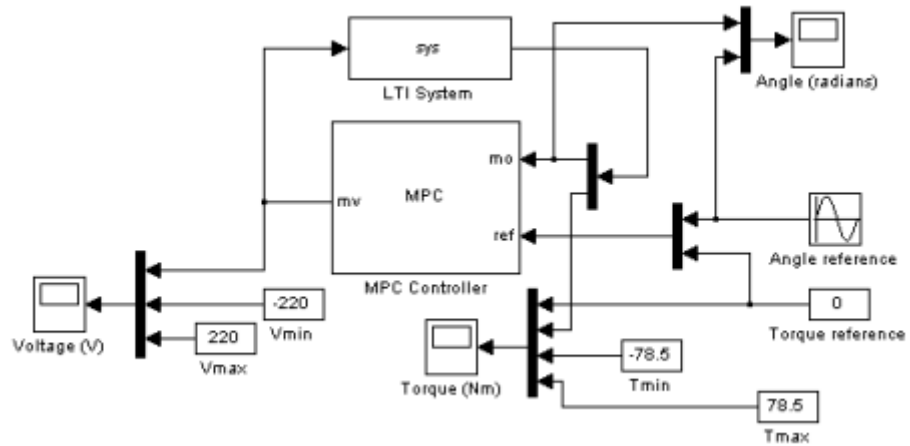


**Figure 4-14: Plotting the Output of the Sim Command**

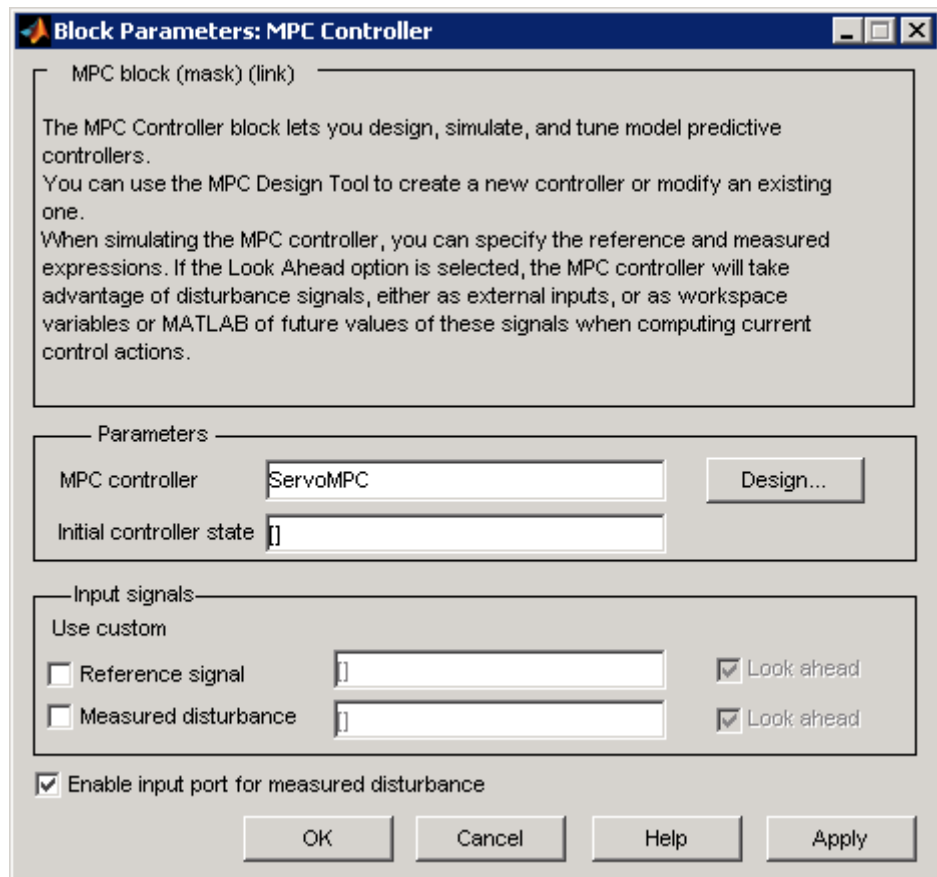
## Using MPC Tools in Simulink

Figure 4-15 is a Simulink block diagram for the servomechanism example. Most of the blocks are from the standard Simulink library. There are two exceptions:

- Servomechanism Model is an LTI System block from the Control System Toolbox library. The LTI model `sys` (which must exist in the workspace) defines its dynamic behavior. To review how to create this model, see “Defining the Plant Model” on page 4-4.
- MPC Controller is from the MPC Blocks library. Figure 4-16 shows the dialog box obtained by double-clicking on this block. You need to supply an MPC object, and `ServoMPC` is being used here. It must be in the Workspace before you run a simulation. The **Design** button opens the design tool, which allows you to create or modify the object. To review how to use commands to create `ServoMPC`, see “Constructing an MPC Object” on page 4-23.



**Figure 4-15: Block Diagram for the Servomechanism Example**



**Figure 4-16: MPC Toolbox Simulink Block Dialog**

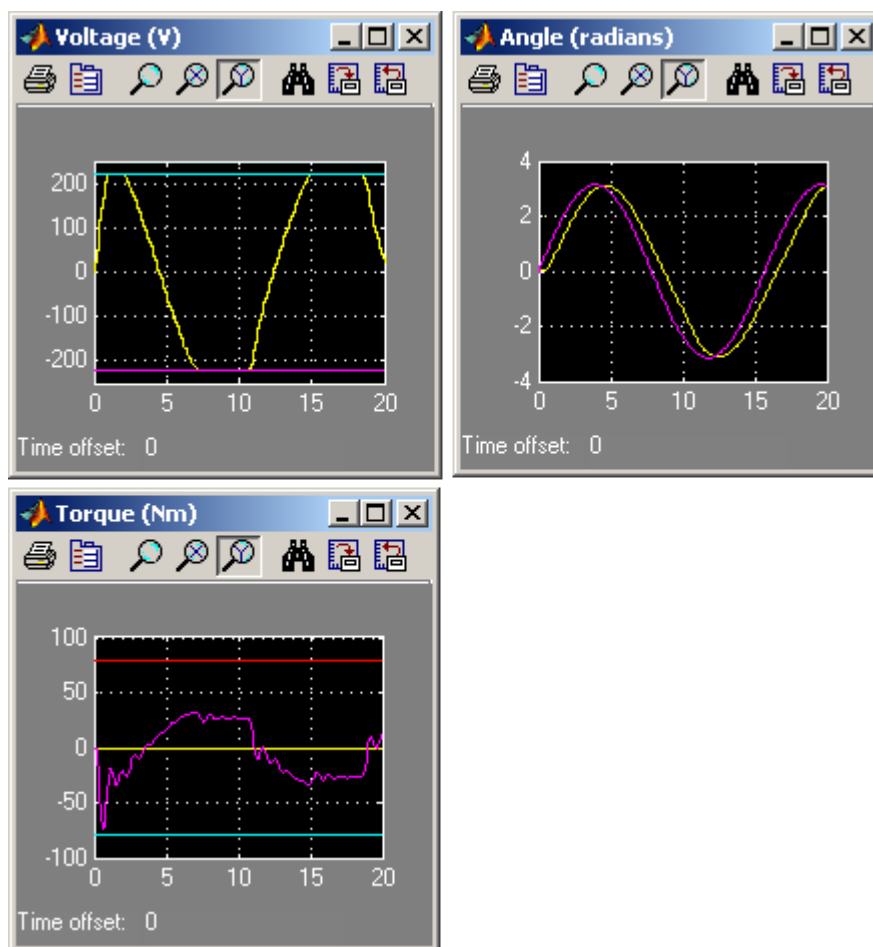
The key features of the diagram are as follows:

- The MPC Controller output is the plant input. The Voltage Scope block plots it (yellow curve). Minimum and maximum voltage values are shown as magenta and cyan curves.
- The plant output is a vector signal. The first element is the measured angular position. The second is the unmeasured torque. A Demux block separates them. The angular position feeds back to the controller and plots

on the Angle scope (yellow curve). The torque plots on the Torque scope (with its lower and upper bounds).

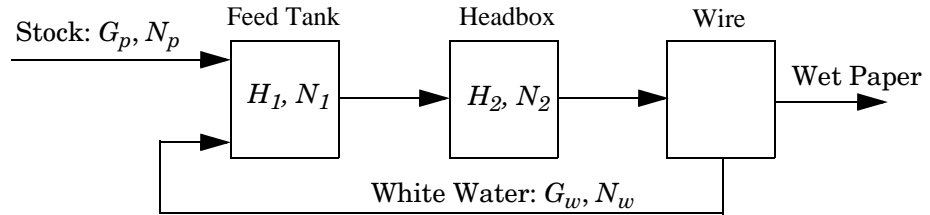
- The position setpoint varies sinusoidally with amplitude  $\pi$  radians and frequency 0.4 rad/s. It also appears on the Angle scope (magenta curve).

Figure 4-17 shows the scope displays for a 20-second simulation. The angular position tracks the sinusoidal setpoint variations quite well, despite saturation of the applied voltage. The setpoint variations are more gradual than the step changes used previously, so the torque stays well within its bounds.



**Figure 4-17: Servomechanism Simulation Scopes**

## Paper Machine Process Control



**Figure 4-18: Schematic of Paper Machine Headbox Elements**

Ying *et al.* [1] studied the control of consistency (percentage pulp fibers in aqueous suspension) and liquid level in a paper machine headbox, a schematic of which is shown in Figure 4-18. The process model is a set of ordinary differential equations (ODEs) in bilinear form. The states are

$$x = [H_1 \ H_2 \ N_1 \ N_2]^T$$

where  $H_1$  is the liquid level in the feed tank,  $H_2$  is the headbox liquid level,  $N_1$  is the feed tank consistency, and  $N_2$  is the headbox consistency. The measured outputs are

$$y = [H_2 \ N_1 \ N_2]^T$$

The primary control objectives are to hold  $H_2$  and  $N_2$  at setpoints. There are two manipulated variables

$$u = [G_p \ G_w]^T$$

where  $G_p$  is the flow rate of stock entering the feed tank, and  $G_w$  is the recycled *white water* flow rate. The consistency of stock entering the feed tank,  $N_p$ , is a measured disturbance.

$$v = N_p$$

The white water consistency is an unmeasured disturbance.



$$d = N_w$$

Variables are normalized. All are zero at the nominal steady state and have comparable numerical ranges. Time units are minutes. The process is open-loop stable.

The `mpcdemos` folder contains a file called `mpc_pmmodel.m`, which implements the nonlinear model equations as a Simulink S-function. The input sequence is  $G_p, G_w, N_p, N_w$ , and the output sequence is  $H_2, N_1, N_2$ .

## Linearizing the Nonlinear Model

The paper machine headbox model is easy to linearize analytically, yielding the following state space matrices:

```
A = [-1.9300      0      0      0
      0.3940    -0.4260      0      0
           0      0    -0.6300      0
      0.8200    -0.7840    0.4130   -0.4260];
B = [1.2740     1.2740      0      0
           0      0      0      0
      1.3400    -0.6500    0.2030    0.4060
           0      0      0      0];
C = [0     1.0000      0      0
      0      0     1.0000      0
      0      0      0     1.0000];
D = zeros(3,4);
```

Use these to create a continuous-time LTI state-space model, as follows:

```
PaperMach = ss(A, B, C, D);
PaperMach.InputName = {'G_p', 'G_w', 'N_p', 'N_w'};
PaperMach.OutputName = {'H_2', 'N_1', 'N_2'};
```

(The last two commands are optional; they improve plot labeling.)

As a quick check of model validity, plot its step responses as follows:

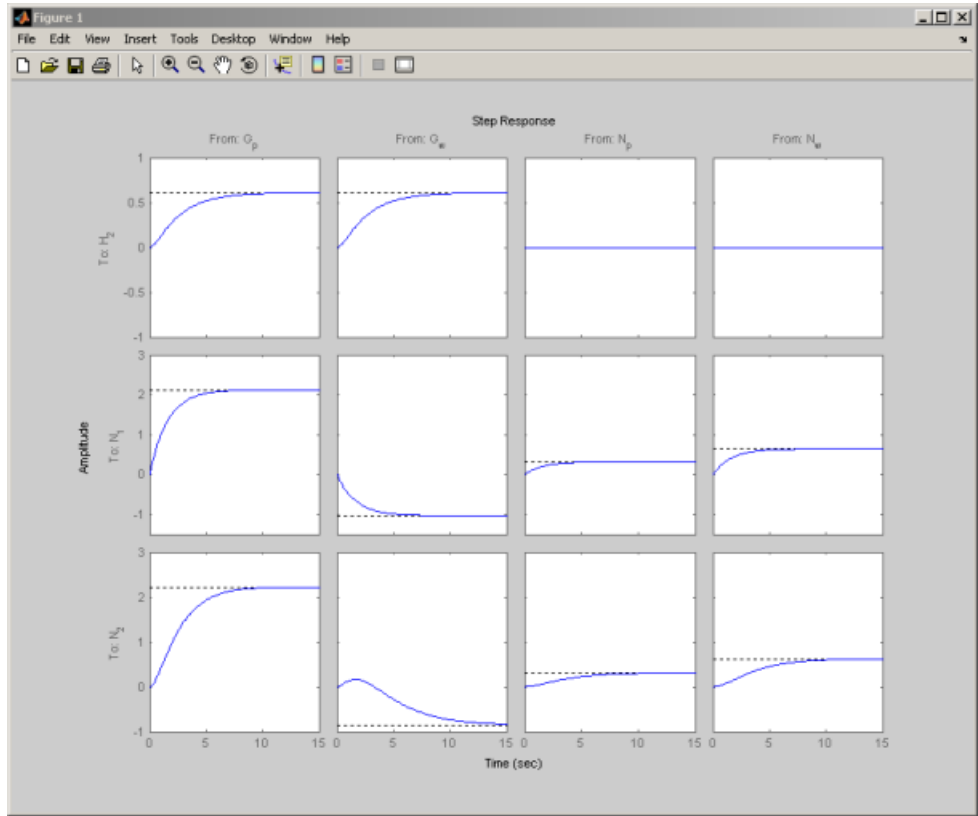
```
step(PaperMach);
```

The results appear in Figure 4-19. Note the following:

- The two manipulated variables affect all three outputs.

- They have essentially identical effects on  $H_2$ .
- The  $G_w \rightarrow N_2$  pairing exhibits an inverse response.

These features make the it difficult to achieve accurate, independent control of  $H_2$  and  $N_2$ .



**Figure 4-19: Linearized Paper Machine Model's Step Responses**

## MPC Design

Type

mpctool

to open the mpc design tool. Import your LTI PaperMach model as described in “Opening MPCTOOL and Importing a Model” on page 4-6.

Next, define signal properties, being sure to designate  $N_p$  and  $N_w$  as measured and unmeasured disturbances, respectively. Your specifications should resemble Figure 4-20.

Input signal properties				
Name	Type	Description	Units	Nominal
G_p	Manipulated	Feed flow rate	kg/h	0.0
G_w	Manipulated	White water flow rate	kg/h	0.0
N_p	Meas. disturb.	Feed consistency	%	0.0
N_w	Unmeas. disturb.	White water consistency	%	0.0

Output signal properties				
Name	Type	Description	Units	Nominal
H_2	Measured	Headbox level	m	0.0
N_1	Measured	Feed tank consistency	%	0.0
N_2	Measured	Head box consistency	%	0.0

**Figure 4-20: Signal Properties for the Paper Machine Application**

### Initial Controller Design

If necessary, review “Specifying Controller Properties” on page 4-10. Then click the **MPC1** node and specify the following controller parameters (leaving others at their default values):

- **Models and Horizons.** Control interval = 2 minutes
- **Constraints.** For both  $G_p$  and  $G_w$ , Minimum = -10, Maximum = 10, Max down rate = -2, Max up rate = 2.

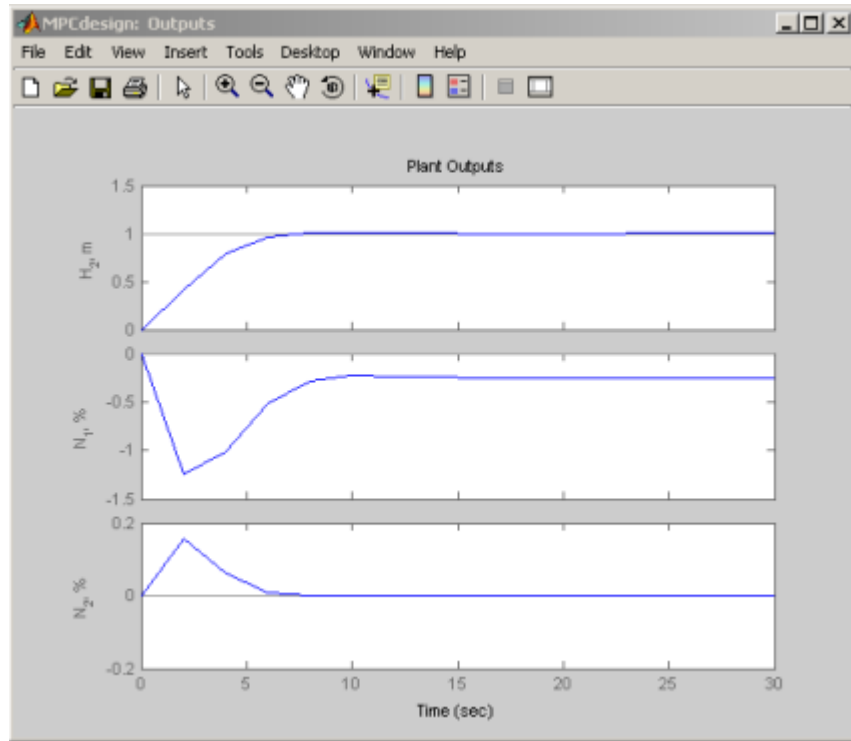
- **Weight Tuning.** For both  $G_p$  and  $G_w$ , Weight = 0, Rate weight = 0.4. For  $N_I$ , Weight = 0. (Other outputs have Weight = 1.)

**Servo Response**

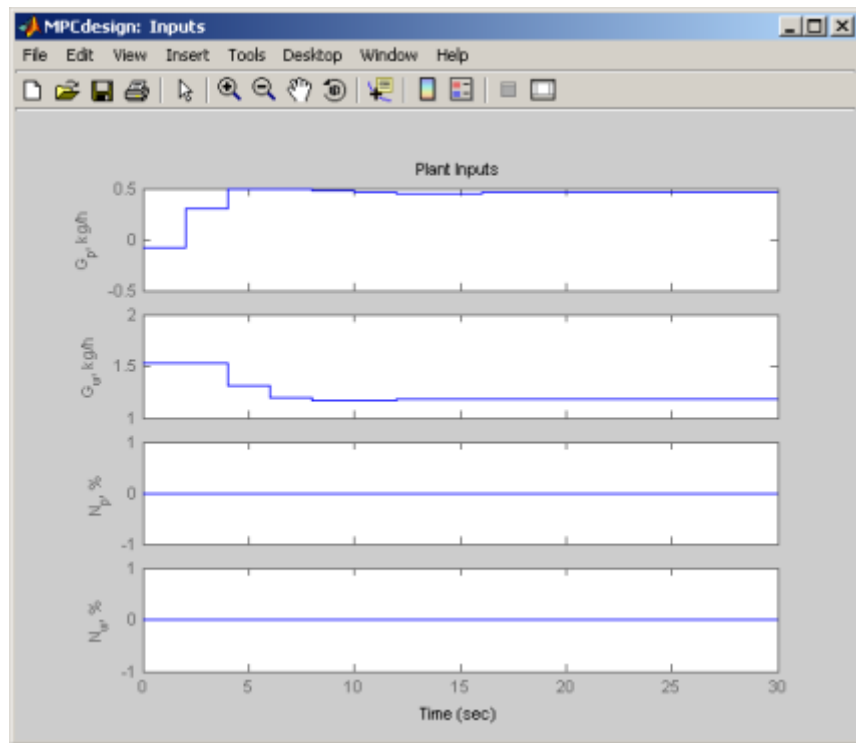
Finally, select the **Scenario1** node and define a servo-response test:

- Duration = 30
- $H_2$  setpoint = 1 (constant)

Simulate the scenario. You should obtain results like those shown in Figure 4-21 and Figure 4-22.



**Figure 4-21: Servo Response for Unit Step in Headbox Level Setpoint**



**Figure 4-22: Manipulated Variable Moves Corresponding to Figure 4-21**

### Weight Tuning

The response time is about 8 minutes. We could reduce this by decreasing the control interval, reducing the rate weight on the manipulated variables, and/or eliminating the up/down rate constraints. The present design uses a conservative control effort, which would usually improve robustness, so we will continue with the current settings.

Note the steady-state error in  $N_I$  (it's about -0.25 units in Figure 4-21). There are only two manipulated variables, so it's impossible to hold three outputs at setpoints. We don't need to hold  $N_I$  so we have set its weight to zero (see controller settings in "Initial Controller Design" on page 4-33). Otherwise, all three outputs would have exhibited steady-state error (try it).

Consistency control is more important than level control. Try decreasing the  $H_2$  weight from 1 to 0.2. You should find that the peak error in  $N_2$  decreases by almost an order of magnitude, but the  $H_2$  response time increases from 8 to about 18 minutes (not shown). Use these modified output weights in subsequent tests.

### Feedforward Control

To configure a test of the controller's feedforward response, define a new scenario by clicking on the **Scenarios** node, clicking the **New** button, and renaming the new scenario **Feedforward** (by editing its name in the tree or the summary list).

In the **Feedforward** scenario, define a step change in the measured disturbance,  $N_p$ , with **Initial value** = 0, **Size** = 1, **Time** = 10. All output setpoints should be zero. Set the **Duration** to 30 time units.

If response plots from the above servo response tests are still open, close them. Simulate the **Feedforward** scenario. You should find that the  $H_2$  and  $N_2$  outputs deviate very little from their setpoints (not shown).

Experiment with the "look ahead" feature. First, observe that in the simulation just completed the manipulated variables didn't begin to move until the disturbance occurred at  $t = 10$  minutes. Return to the **Feedforward** scenario, select the **Look ahead** option for the measured disturbance, and repeat the simulation.

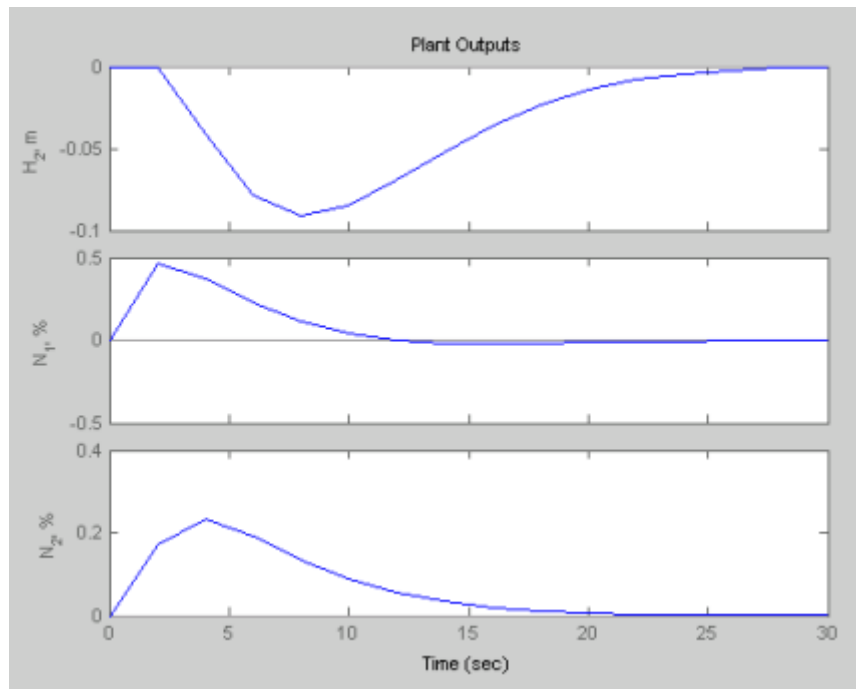
Notice that the manipulated variables begin changing *in advance* of the disturbance. This happens because the look ahead option uses known future values of the disturbance when computing its control action. For example, at time  $t = 0$  the controller is using a prediction horizon of 10 control intervals (20 time units), so it "sees" the impending disturbance at  $t = 10$  and begins to prepare for it. The output setpoint tracking improves slightly, but it was already so good that the improvement is insignificant. Also, it's unlikely that there would be advanced knowledge of a consistency disturbance, so clear the **Look ahead** check box for subsequent simulations.

### Unmeasured Input Disturbance

To test the response to unmeasured disturbances, define another new scenario called **Feedback**. Configure it as for **Feedforward**, but set the measured disturbance,  $N_p$ , to zero (constant), and the unmeasured disturbance,  $N_w$ , to

1.0 (constant). This simulates a sudden, sustained, unmeasured disturbance occurring at time zero.

Running the simulation should yield results like those in Figure 4-23. The two controlled outputs ( $H_2$  and  $N_2$ ) exhibit relatively small deviations from their setpoints (which are zero). The settling time is longer than for the servo response (compare to Figure 4-21) which is typical.



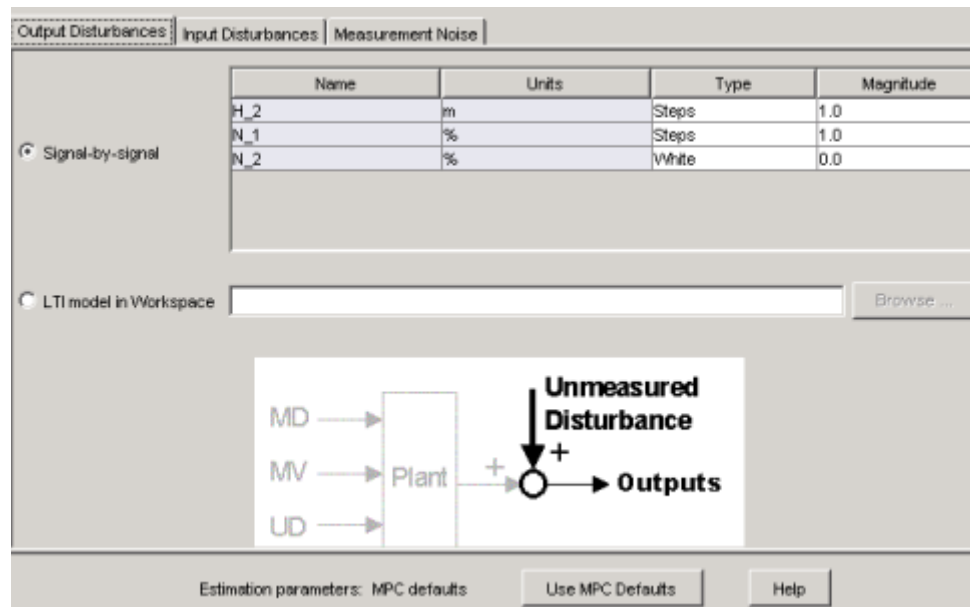
**Figure 4-23: Feedback Scenario: Unmeasured Disturbance Rejection**

One factor limiting performance is the chosen control interval of 2 time units. The controller can't respond to the disturbance until it first appears in the outputs, i.e., at  $t = 2$ . If you wish, experiment with larger and smaller intervals (modify the specification on the controller's **Model and Horizons** tab).

### Effect of Estimator Assumptions

Another factor influencing the response to unmeasured disturbances (and model prediction error) is the estimator configuration. The results shown in Figure 4-23 are for the default configuration.

To view the default assumptions, select the controller node (**MPC1**), and select its **Estimation** tab. The resulting view should be as shown in Figure 4-24. The status message (bottom of figure) indicates that the MPC Toolbox default assumptions are being used.



**Figure 4-24: Default Estimator Assumptions: Output Disturbances.**

Now consider the upper part of the figure. The **Output Disturbances** tab is active, and its **Signal-by-signal** option is selected. According to the tabular data, the controller is assuming independent, step-like disturbances (i.e., integrated white noise) in the first two outputs.

Select the **Input Disturbances** tab. Verify that the controller is also assuming independent step-like disturbances in the unmeasured disturbance input.



Thus, there are a total of three independent, sustained (step-like) disturbances. This allows the controller to eliminate offset in all three measured outputs.

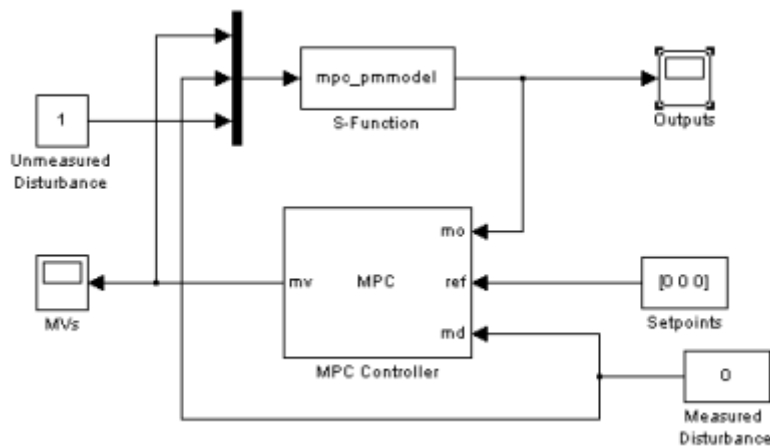
The disturbance magnitudes are unity by default. Making one larger than the rest would signify a more important disturbance at that location.

Select the **Measurement Noise** tab. Verify that white noise (unit magnitude) is being added to each output. The noise magnitude governs how much influence each measurement has on the controller's decisions. For example, if a particular measurement is relatively noisy, the controller will give it less weight, relying instead upon the model predictions of that output. This provides a noise filtering capability.

In the paper machine application, the default disturbance assumptions are reasonable. It is difficult to improve disturbance rejection significantly by modifying them.

## Controlling the Nonlinear Plant in Simulink

It's good practice to run initial tests using the linear plant model as described in "Servo Response" on page 4-34, and "Unmeasured Input Disturbance" on page 4-36. Such tests don't introduce prediction error, and are a useful benchmark for more demanding tests with a nonlinear plant model. The controller's prediction model is linear, so such tests introduce prediction error.



**Figure 4-25: Paper Machine Headbox Control Using MPC Tools in Simulink**

Figure 4-25 is a Simulink diagram in which the MPC Toolbox controller is being used to regulate the nonlinear paper machine headbox model. The block labeled S-Function embodies the nonlinear model, which is coded in an M-file called *mpc\_pmmodel.m*.

As shown in the dialog below, the MPC Controller block references a controller design called MPC1, which was exported to the MATLAB workspace from the design tool. Note also that the measured disturbance inport is enabled, allowing the measured disturbance to be connected as shown in Figure 4-25.

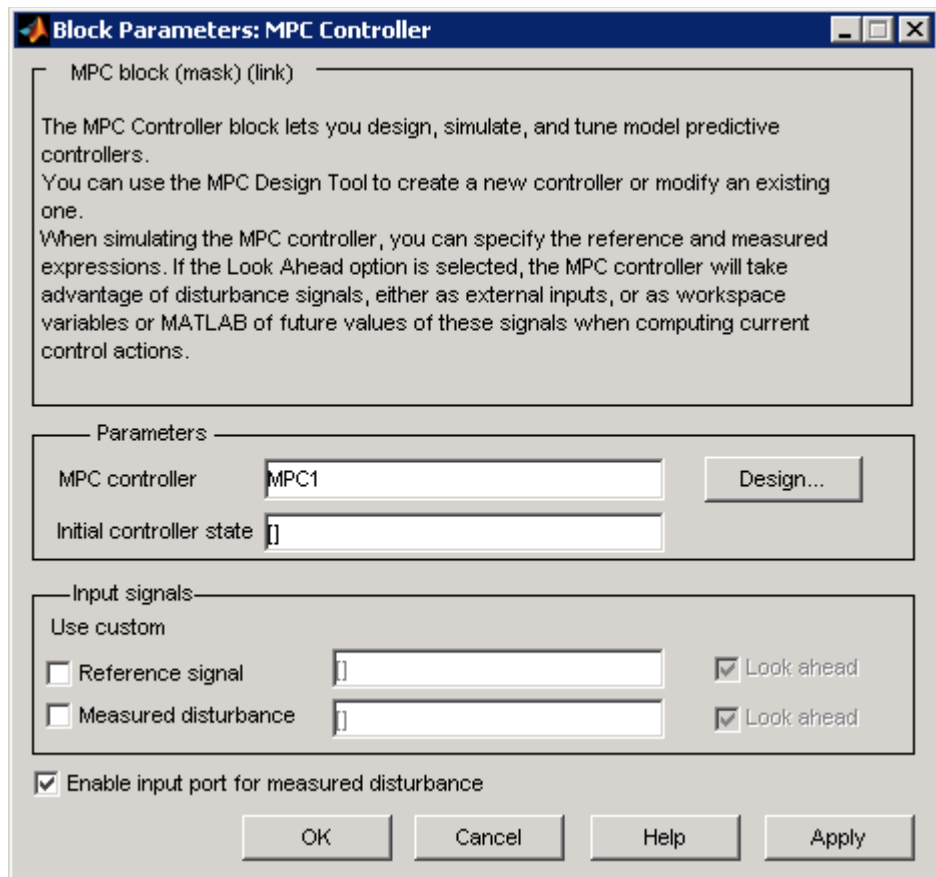
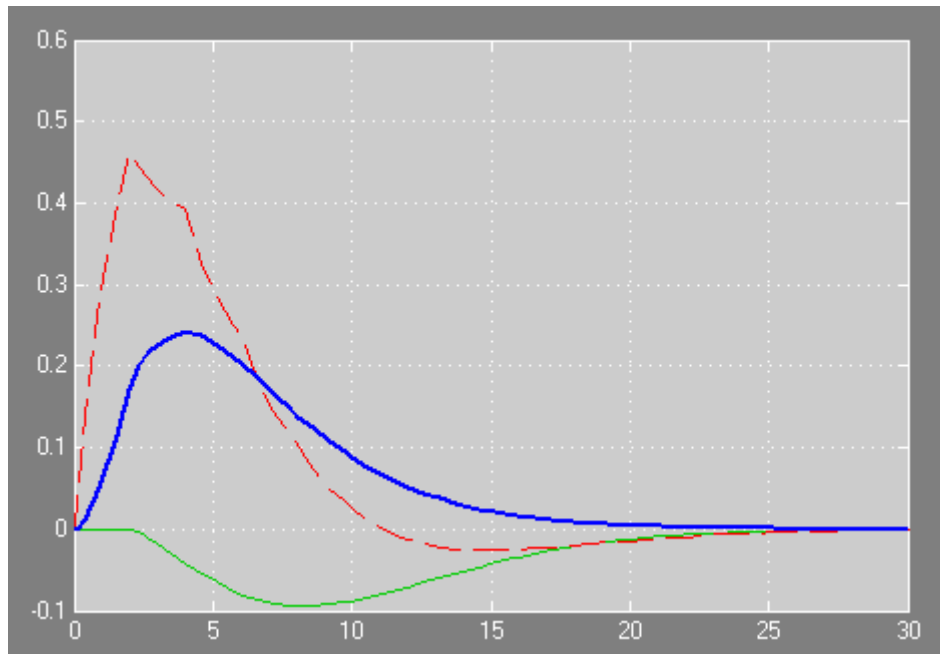


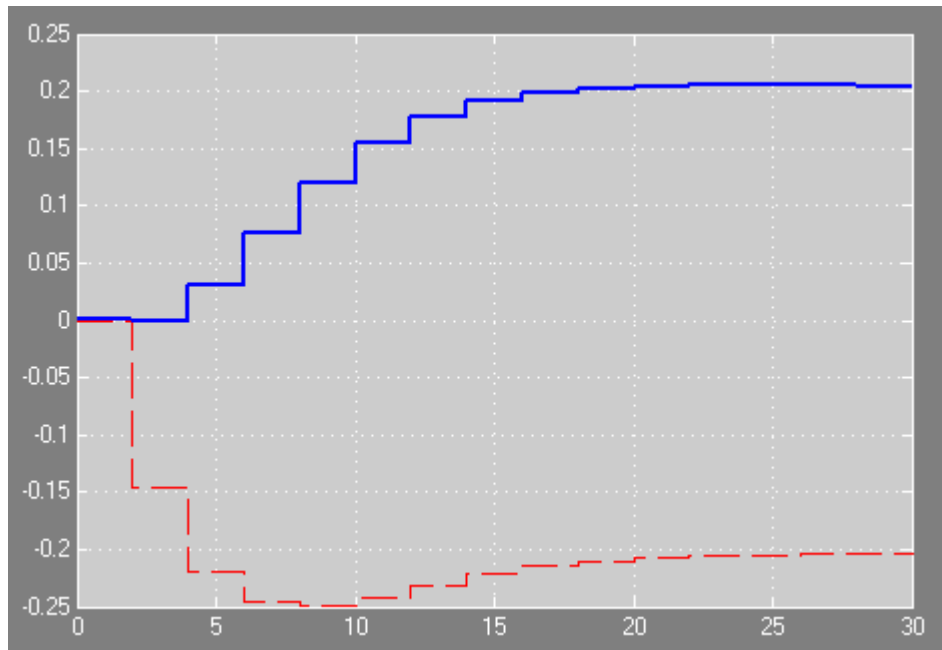
Figure 4-26 shows the scope display from the “Outputs” block for the setup of Figure 4-25, i.e., an unmeasured disturbance. The yellow curve is  $H_2$ , the

magenta is  $N_1$ , and the cyan is  $N_2$ . Comparing to Figure 4-23, the results are almost identical, indicating that the effects of nonlinearity and prediction error were insignificant in this case. Figure 4-27 shows the corresponding manipulated variable moves (from the “MVs” scope in Figure 4-25) which are smooth yet reasonably fast.

As disturbance size increases, nonlinear effects begin to appear. For a disturbance size of 4, the results are still essentially the same as shown in Figure 4-26 and Figure 4-27 (scaled by a factor of 4), but for a disturbance size of 6, the setpoint deviations are relatively larger, and the curve shapes differ (not shown). There are marked qualitative and quantitative differences when the disturbance size is 8. When it is 9, deviations become very large, and the MVs saturate. If such disturbances were likely, the controller would have to be retuned to accommodate them.



**Figure 4-26: Simulink Test: Output Variables**



**Figure 4-27: Simulink Test: Manipulated Variables**

---

## Reference

- [1] Ying, Y., M. Rao, and Y. Sun “Bilinear control strategy for paper making process,” *Chemical Engineering Communications* (1992), Vol. 111, pp. 13-28.



# The Design Tool

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This chapter is the reference manual for the MPC Toolbox design tool (graphical user interface). For example design tool applications, see the MPC Toolbox “Getting Started” manual, or Chapter 4, “Case-Study Examples.” in this document.

Opening the MPC Design Tool (p. 5-2)	How to start the design tool from MATLAB or Simulink
The Menu Bar (p. 5-3)	Describes the main menu options
The Tool Bar (p. 5-6)	Describes the tool bar icons and their use
The Tree View (p. 5-7)	Explains how to navigate among the various design tool views
Importing a Plant Model (p. 5-9)	The plant model import dialog and its options
Importing a Controller (p. 5-15)	The controller import dialog and its options
Exporting a Controller (p. 5-19)	The controller export dialog and its options
Signal Definition View (p. 5-21)	Detailed description of the initial design tool view, which defines the overall controller structure
Plant Models View (p. 5-26)	Lists the plant models available to your design, and allows you to import others
Controllers View (p. 5-29)	Lists the controllers in your design and allows you to copy, export, rename, or delete a controller
Simulation Scenarios List (p. 5-33)	Lists the simulation scenarios in your design
Controller Specifications View (p. 5-36)	Shows how to specify a controller
Simulation Scenario View (p. 5-59)	Shows how to set up a simulation
Response Plots (p. 5-67)	Describes the plots generated in a simulation and their customization

## Opening the MPC Design Tool

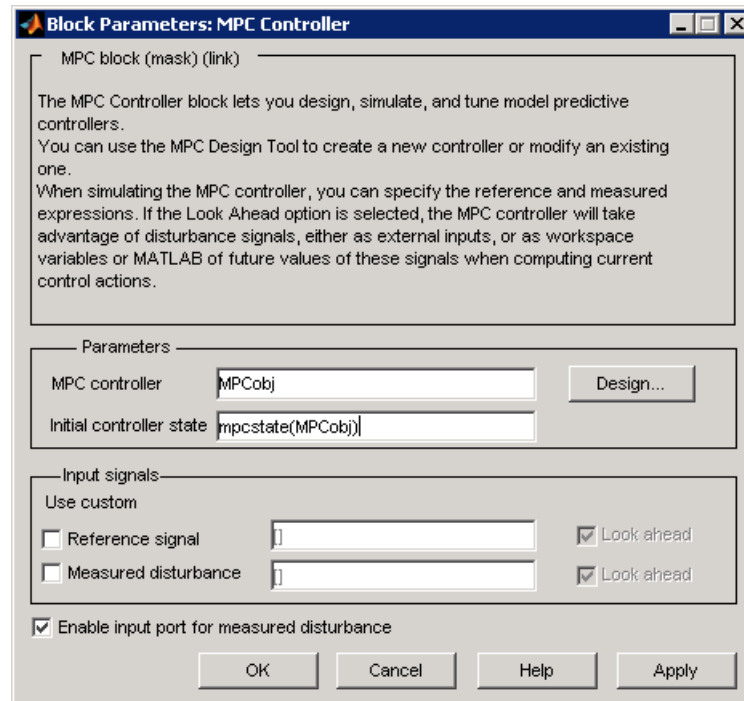
To open the Design Tool in MATLAB, type

```
mpctool
```

The design tool is part of the Control and Estimation Tools Manager. When invoked as shown above, the design tool opens as a new *project* named **MPCdesign**.

If you started the tool previously, the above command makes the tool visible but doesn't open a new project.

Alternatively, if your Simulink model contains an MPC Controller block, you can double-click on the block to obtain its mask (see example below) and click the **Design** button. If the **MPC controller** field is empty, the design tool will initialize a default controller. Otherwise, it will load the specified existing controller object so you can edit its properties.





## The Menu Bar

The design tool's menu bar appears whenever you've selected an MPC Toolbox project or task in the tree (see "The Tree View" on page 5-7). The menu bar's MPC option distinguishes it from other control and estimation tools. See the example below. The following sections describe each menu option.



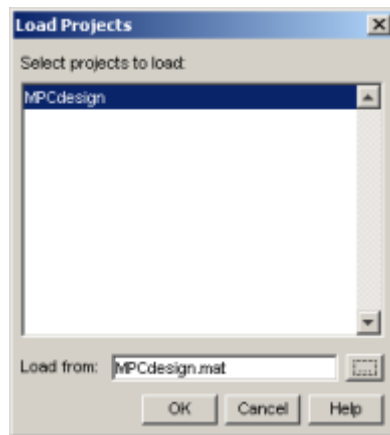
### File Menu

#### New Design

Creates a new (empty) MPC Toolbox design project within the Control and Estimation Tools Manager and assigns it a default name. You can also create a new design using the tool bar (see "The Tool Bar" on page 5-6).

#### Load

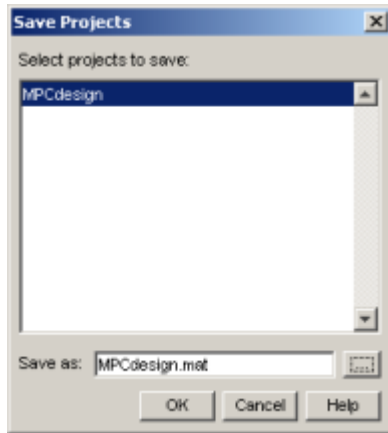
Loads a saved design. A dialog asks you to specify the MAT-file containing the saved design. If the MAT-file contains multiple projects, you must select the one(s) to be loaded (see example below).



You can also load a design using the tool bar (see "The Tool Bar" on page 5-6).

### Save

Saves a design so you can use it later. The data are saved in a MAT-file. A dialog allows you to specify the file name (see below). If you are working on multiple projects, you can select those to be saved.



You can also select the **Save** option using the tool bar (see “The Tool Bar” on page 5-6)

### Close

Closes the design tool. If you’ve modified the design, you’ll be asked whether or not you want to save it before closing.

## MPC Menu

### Import

You have the following options:

- **Plant model** – Import a plant model using the model import dialog (see “Importing a Plant Model” on page 5-9)
- **Controller** – Import a controller using the controller import dialog (see “Importing a Controller” on page 5-15)

**Export**

Export a controller using the export dialog (see “Exporting a Controller” on page 5-19). This option won’t be enabled until your design includes at least one fully specified controller.

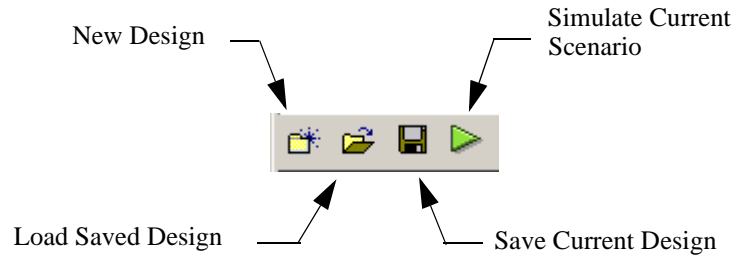
**Simulate**

Simulate the *current scenario*, i.e., the one most recently simulated or selected in the tree (see “The Tree View” on page 5-7). You can select this option from the keyboard by typing Ctrl-R, or using the tool bar icon (see “The Tool Bar” on page 5-6).

The **Simulate** option won’t be enabled until your design includes at least one fully specified simulation scenario.

## The Tool Bar

The tool bar provides quick access to the menu options you'll use most often.



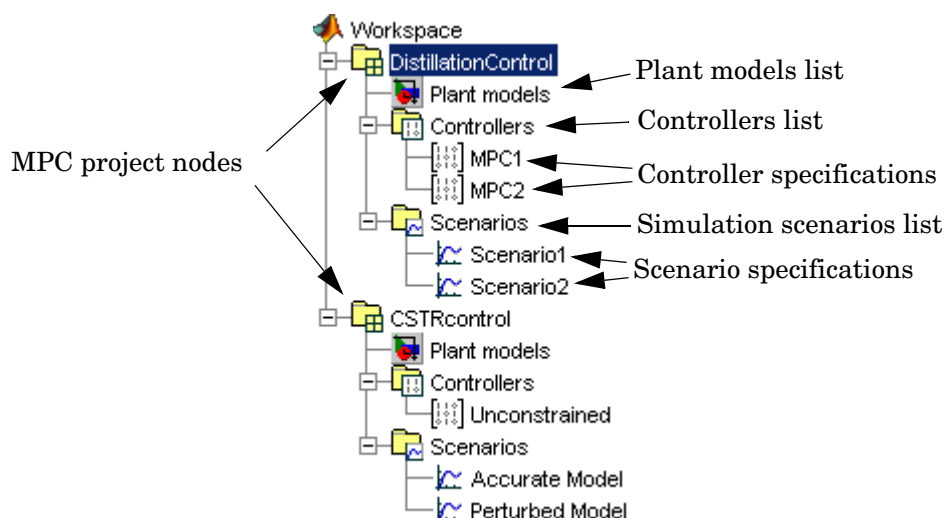
For more information on each option, see the following:

- “New Design” on page 5-3
- “Load” on page 5-3
- “Save” on page 5-4
- “Simulate” on page 5-5

## The Tree View

The tree view appears in a frame on the design tool's left-hand side (see example below). When you select one of the tree's *nodes* (by clicking its name or icon) the larger frame to its right shows a dialog panel that allows you to view and edit the specifications associated with that item.

### Node Types



The above example shows two MPC Toolbox design project nodes, **DistillationControl** and **CSTRcontrol**, and their sub-nodes. For more details on each node type, see the following:

- *MPC design project/task* – see “Signal Definition View” on page 5-21
- *Plant models list* – see “Plant Models View” on page 5-26
- *Controllers list* – see “Controllers View” on page 5-29
- *Controller specifications* – see “Simulation Scenarios List” on page 5-33
- *Scenarios list* – see “Simulation Scenario View” on page 5-59
- *Scenario specifications* – see “Controller Specifications View” on page 5-36

### Renaming a Node

You can rename following node types:

- MPC design project/task
- Controller specifications
- Scenario specifications

To rename a node, do *one* of the following:

- Click on the name, wait for an edit box to appear, type the desired name, and push the Enter key to finalize your choice, OR
- Right-click on the name, select the **Rename** menu option, and enter the desired name in the dialog box, OR
- To rename a controller specification node, select **Controllers** and edit the controller name in the table, OR
- To rename a scenario specification node, select **Scenarios** and edit the scenario name in the table

## Importing a Plant Model

To import a plant model, do *one* of the following:

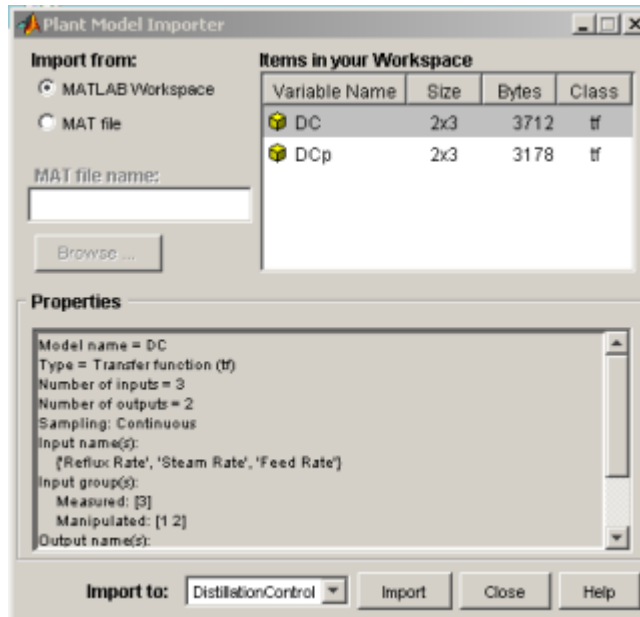
- Select the **MPC/Import/Plant Model** menu option, OR
- Select the MPC project/task node in the tree (see “The Tree View” on page 5-7), and then click the **Import Plant** button, OR
- Right-click the MPC project/task node and select the **Import Plant Model** menu option, OR
- If you’ve already imported a model, select the **Plant models** node, and then click the **Import** button, OR
- If you’ve already imported a model, right-click the **Plant models** node and select the **Import Model** menu option

All of the above open the **Plant Model Importer** dialog, shown below. Within the dialog you can import an LTI model from the workspace or, when you have Simulink Control Design, you can import a linearized plant model from the Simulink model. The following sections describe the dialog options for importing an LTI model from the workspace. For information on importing a linearized plant model, see “Importing a Linearized Plant Model” on page 5-12.

## Import from

Use the radio buttons to set the location from which the model will be imported.

### MATLAB Workspace

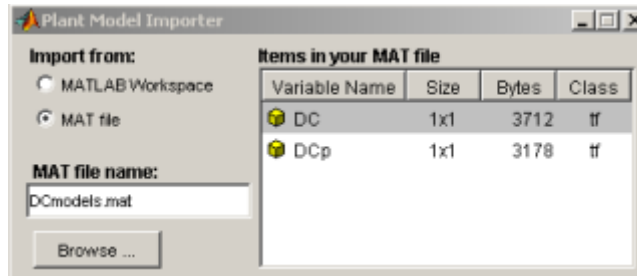


This is the default option and is the case shown in the above example. The **Items in your Workspace** area in dialog's upper-right lists all candidate models in your MATLAB workspace. Select one by clicking on it. The dialog's **Properties** area lists the selected model's properties (the DC model in the above example).



## MAT-File

The upper part of the dialog changes as shown below

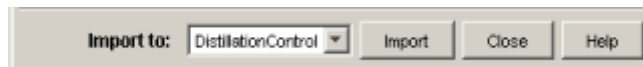


The **MAT file name** edit box becomes active. Type the desired MAT-file name here (if it's not on the MATLAB path, enter the complete path to the file). You can also use the **Browse** button which activates a standard file chooser dialog.

In the above example, file DCmodels.mat contains two models. Their names appear in the **Items in your MAT file** area on the dialog's upper right. As with the workspace option, the selected model's properties appear in the **Properties** area.

## Import to

The combo box at the dialog's bottom allows you to specify the MPC project/task into which the plant model will be imported (see example below). It defaults to the project/task most recently active.



## Buttons

### Import

Select the model you want to import from the **Items** list in the dialog's upper right. Verify that the **Import To** option designates the correct project/task. Click the **Import** button to import the model.

You can select **Plant models** in the tree to verify that the model has been loaded. (see “The Tree View” on page 5-7, and “Plant Models View” on page 5-26).

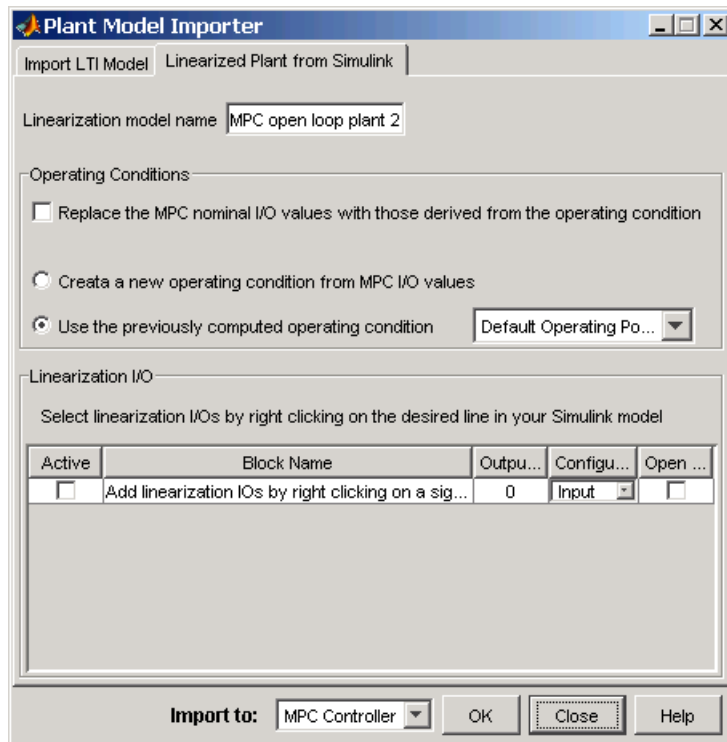
The import dialog remains visible until you close it, allowing you to import additional models.

### Close

Click **Close** to close the dialog window. You can also click the close icon on the window’s title bar.

## Importing a Linearized Plant Model

To import a linearized plant model from the Simulink model, select the **Linearized Plant from Simulink** panel within the **Plant Model Importer**, as shown in the following figure.



## Linearization Process

When you click **OK**, the MPC Toolbox works with Simulink Control Design to create a linearized plant model by automatically performing the following tasks:

- 1 Configures the Control and Estimation Tools Manager.
- 2 Temporarily inserts linearization input and output points in the model at the inputs and outputs of the MPC Controller block.
- 3 When the **Create a new operating condition from MPC I/O values** is selected, the MPC Toolbox temporarily inserts output constraints at the inputs/outputs of the MPC Controller block..
- 4 Finds an equilibrium operating condition based on the constraints or uses the specified operating condition.
- 5 Linearizes the plant model about the operating point.

The linearized plant model is added as a new node under the **Plant Models** node within the Control and Estimation Tools Manager. For more information on the linearization process, refer to the Simulink Control Design documentation.

## Linearization Options

You can also customize the linearization process in several ways before clicking **OK**:

- To specify an alternative name for the linearized plant model, enter the name in the **Linearization model name** edit field.
- To use an alternative operating condition, you can
  - select one from the menu next to **Use the previously computed operating condition**. This list contains all operating conditions that exist within the current project.
  - select **Create a new operating condition from MPC I/O values** to compute an operating condition by optimization, using the nominal plant values as constraints.

- To replace the nominal plant values with the operating point used in the linearization, select the check box next to **Replace the MPC nominal I/O values with those derived from the operating condition.**
- When there are multiple MPC Controller blocks, use the **Import to** menu to select a node within the Control and Estimation Tools Manager to import the plant model to.

In addition, the **Linearization I/O** panel displays the current linearization input and output points in the model. When creating the linearized model, the MPC Toolbox temporarily modifies these input and output points with input and output points suitable for extracting a linearized plant model.

## Importing a Controller

To import a controller, do *one* of the following:

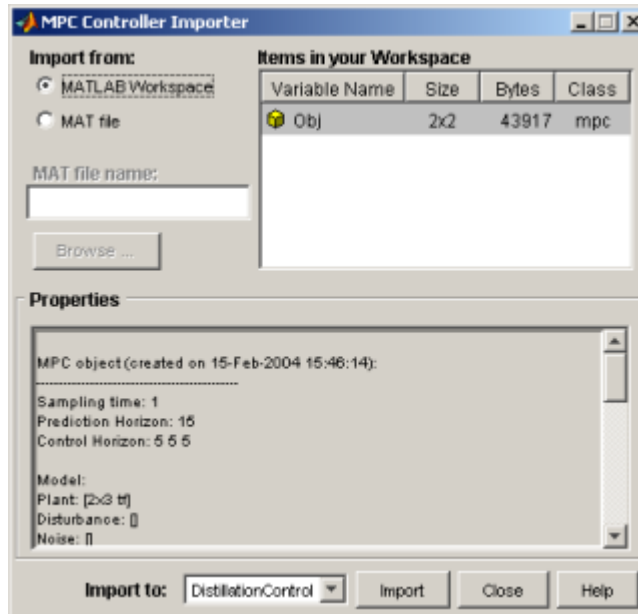
- Select the **MPC/Import/Controller** menu option, OR
- Select the MPC project/task node in the tree (see “The Tree View” on page 5-7), and then click the **Import Controller** button, OR
- Right-click the MPC project/task node and select the **Import Controller** menu option, OR
- If you’ve already designed a controller, select the **Controllers** node, and then click the **Import** button, OR
- If you’ve already designed a controller, right-click the **Controllers** node and select the **Import Controller** menu option

All of the above open the MPC Controller Importer dialog. The following sections describe the dialog’s options.

## Import from

Use the radio buttons to set the location from which the controller will be imported.

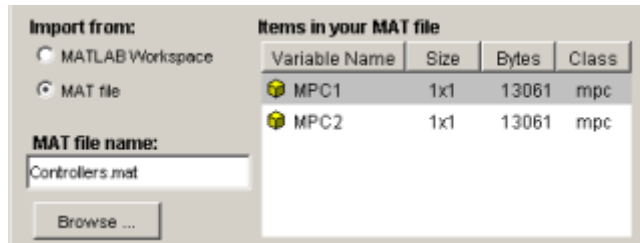
### MATLAB Workspace



This is the default option and is the case shown in the above example. The **Items in your Workspace** area in dialog's upper-right lists all mpc objects in your workspace. Select one by clicking on it. The **Properties** area lists the properties of the selected model (the DC model in the above example).

## MAT-File

The upper part of the dialog changes as shown below

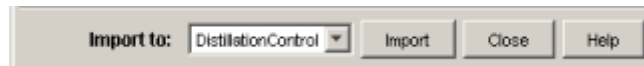


The **MAT file name** edit box becomes active. Type the desired MAT-file name here (if it's not on the MATLAB path, enter the complete path to the file). You can also use the **Browse** button which activates a standard file chooser dialog.

In the above example, file `Controllers.mat` contains two `mpc` objects. Their names appear in the **Items in your MAT file** area on the dialog's upper right.

## Import to

The combo box at the dialog's bottom allows you to specify the MPC project/task into which the controller will be imported (see example below). It defaults to the project/task most recently active.



## Buttons

### Import

Select the controller you want to import from the **Items** list in the dialog's upper right. Verify that the **Import To** option designates the correct project/task. Click the **Import** button to import the controller.

The new controller should appear in the tree as a sub-node of **Controllers**. (see "The Tree View" on page 5-7).

The imported controller contains a plant model, which appears in the **Plant models** list. (see "Plant Models View" on page 5-26).

---

**Note** If the selected controller is incompatible with any others in the designated project, the design tool will not import it.

---

The dialog remains visible until you close it, allowing you to import additional models.

### **Close**

Click **Close** to close the dialog window. You can also click the close icon on the window's title bar.

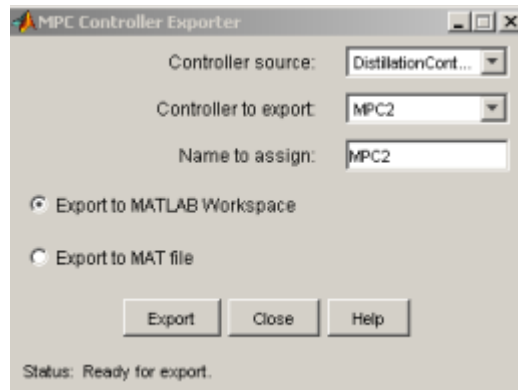


## Exporting a Controller

To export a controller, do *one* of the following:

- Select the **MPC/Export** menu option, OR
- Select **Controllers** in the tree and click its **Export** button, OR
- In the tree, right-click **Controllers** and select the **Export Controller** menu option, OR
- In the tree, right-click the controller you wish to export and select the **Export Controller** menu option

All of the above open the MPC Controller Exporter dialog (see example below).



### Dialog Options

The following sections describe the dialog's options.

#### Controller Source

Use this combo box to select the project/task containing the controller to be exported. It defaults to the project/task most recently active.

#### Controller to Export

Use this combo box to specify the controller to be exported. It defaults to the controller most recently selected in the tree.

### **Name to Assign**

Use this edit box to assign a valid MATLAB variable name (no spaces, etc.). It defaults to a blank-free version of the selected controller's name.

### **Export to Workspace**

Select this radio button if you want the controller to be exported to the MATLAB workspace.

### **Export to MAT File**

Select this radio button if you want the controller to be exported to a MAT file.

## **Buttons**

### **Export**

If you've selected the **to Workspace** option, clicking **Export** causes a new mpc object to be created in your MATLAB workspace. (If one having the assigned name already exists, you'll be asked if you want to overwrite it.) You can use the MATLAB whos command to verify that the controller has been exported.

If you've selected the **to MAT File** option, clicking **Export** opens a standard file chooser that allows you to specify the file.

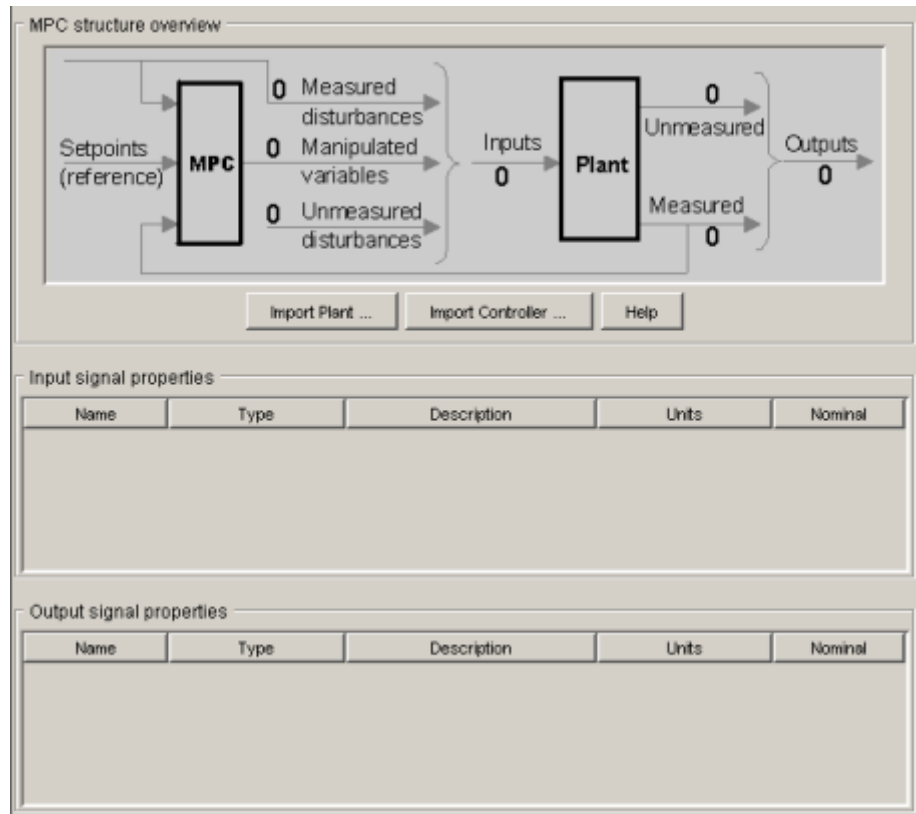
In either case, the dialog window remains visible, allowing you to export additional controllers.

### **Close**

Click **Close** to close the dialog window. You can also click the close icon on the window's title bar.

## Signal Definition View

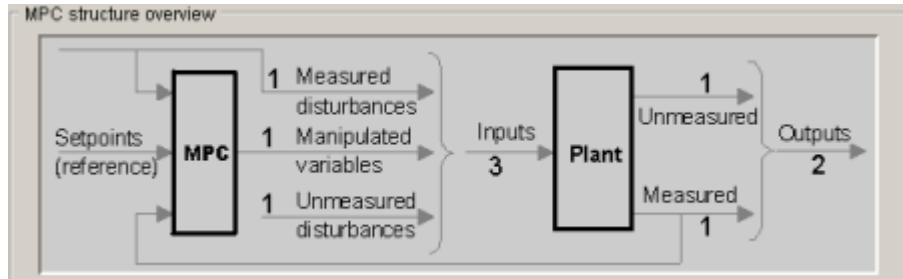
The signal definition view appears whenever you select an MPC Toolbox project/task node in the tree (see “The Tree View” on page 5-7). It is also the view you’ll see when you open the design tool for the first time. An example appears below



The following sections describe the view’s main features.

## MPC Structure Overview

This upper section is a non-editable display of your application’s structure. Once you’ve imported a plant model (or controller), the graphic shows counts for the five possible signal types, as in the example below



The counts will change if you edit the signal types.

## Buttons

### Import Plant

Clicking this opens the Plant Model Importer dialog (see “Importing a Plant Model” on page 5-9).

### Import Controller

Clicking this opens the MPC Controller Importer dialog (see “Importing a Controller” on page 5-15).

---

**Note** You won’t be allowed to proceed with your design until you import a plant model. You can do so indirectly by importing a controller or loading a saved project.

---

## Signal Properties Tables

Two tables display the properties of each signal in your design.

## Input Signal Properties

The plant's input signals appear as table rows (see example below).

Name	Type	Description	Units	Nominal
Reflux Rate	Manipulated	Reflux Flow Rate	moles/min	0.0
Steam Rate	Unmeas. disturb.	Steam Flow Rate	moles/min	0.0
Feed Rate	Meas. disturb.	Feed Flow Rate	moles/min	0.0

The table's columns are editable and have the following significance:

- **Name** – The signal name, an alphanumeric string used to label other tables, graphics, etc. Each name must be unique. The design tool assigns a default name if your imported plant model doesn't specify one.
- **Type** – One of the three valid MPC Toolbox input signal types. The above example shows one of each. To change a signal's type, click on the table cell and select the desired type from the resulting menu. The valid signal types are as follows:
  - Manipulated** – A signal that will be manipulated by the controller, i.e., an actuator (valve, motor, etc.)
  - Measured Disturbance** – An independent input whose value is measured and used as a controller input for *feedforward compensation*
  - Unmeasured Disturbance** – An independent input representing an unknown, unexpected disturbance.
- **Description** – An optional descriptive string.
- **Units** – Optional units (dimensions), a string. Used to label other dialogs, simulation plots, etc.
- **Nominal** – The signal's nominal value. The design tool defaults this to zero. Any value you assign here will be the default initial condition in simulations.

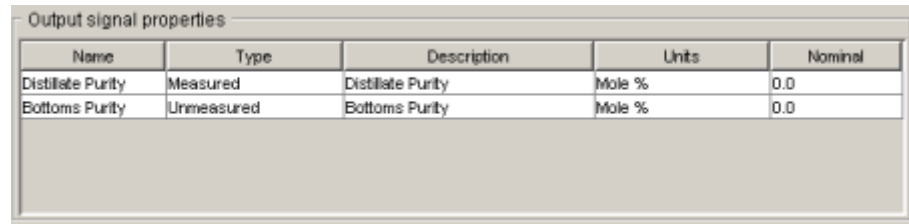
---

**Note** Your design must include at least one *manipulated variable*. The other input signal types need not be included.

---

## Output Signal Properties

The plant's output signals appear as table rows (see example below).



Name	Type	Description	Units	Nominal
Distillate Purity	Measured	Distillate Purity	Mole %	0.0
Bottoms Purity	Unmeasured	Bottoms Purity	Mole %	0.0

The table's columns are editable and have the following significance:

- **Name** – The signal name, an alphanumeric string used to label other tables, graphics, etc. Each name must be unique. The design tool assigns a default name if your imported plant model doesn't specify one.
- **Type** – One of the two valid MPC Toolbox output signal types. The above example shows one of each. To change a signal's type, click on the table cell and select the desired type from the resulting menu. The valid signal types are as follows:
  - Measured** – A signal the controller can use for feedback
  - Unmeasured** – Predicted by the plant model but unmeasured. Can be used as an indicator. Can also be assigned a setpoint or constrained.
- **Description** – An optional descriptive string.
- **Units** – Optional units (dimensions), a string. Used to label other dialogs, simulation plots, etc.
- **Nominal** – The signal's nominal value. The design tool defaults this to zero. Any value you assign here will be the default initial condition in simulations.

---

**Note** Your design must include at least one *measured* output. Inclusion of unmeasured outputs is optional.

---

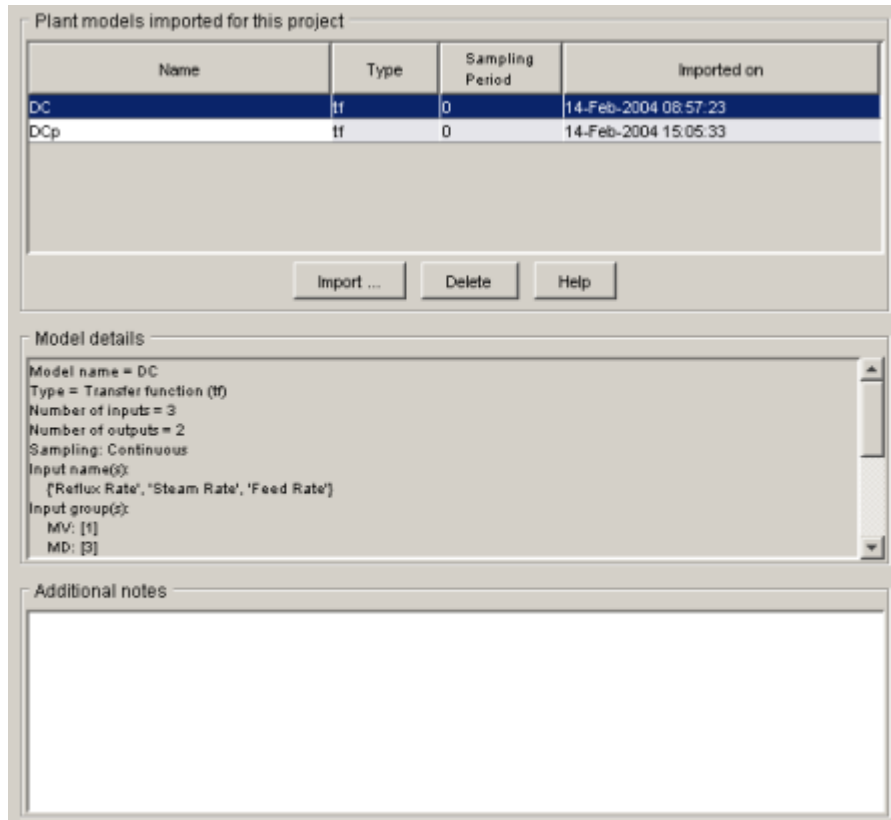
## Right-Click Menu Options

Right-clicking on an MPC project/task node allows you to choose one of the following menu items:

- **Import Plant Model** – Opens the Plant Model Importer dialog (see “Importing a Plant Model” on page 5-9)
- **Import Controller** – Opens the MPC Controller Importer dialog (see “Importing a Controller” on page 5-15)
- **Clear Project** – Erases all plant models, controllers, and scenarios in your design, returning the project to its initial empty state.
- **Delete Project** – Deletes the selected project node.

## Plant Models View

Selecting **Plant models** in the tree causes this view to appear (see example below)

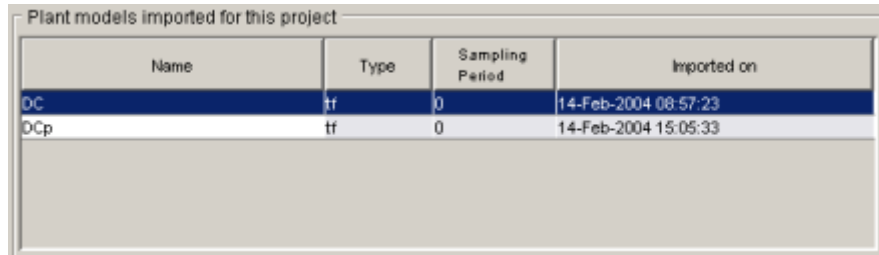


The following sections describe the view's main features.



## Plant Models List

This table lists all the plant models you've imported and/or plant models contained in controllers that you've imported. The example below lists two imported models, DC and DCp.



Name	Type	Sampling Period	Imported on
DC	tf	0	14-Feb-2004 08:57:23
DCp	tf	0	14-Feb-2004 15:05:33

The **Name** field is editable. Each model must have a unique name. The name you assign here will be used within the design tool, but will not alter the original model's name.

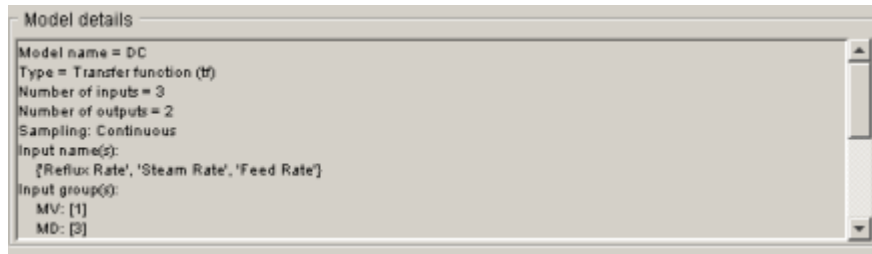
The **Type** field is noneditable and indicates the model's LTI object type (see the Control System Toolbox documentation for a detailed discussion of LTI models).

The **Sampling Period** field is zero for continuous-time models, and a positive real value for discrete-time models.

The **Imported on** field gives the date and time the model was imported into the design tool.

## Model Details

This scrollable viewport shows details of the model currently selected in the plant models list (see "Plant Models List" on page 5-27). An example appears below



## Additional Notes

You can use this editable text area to enter comments, distinguishing model features, etc.

## Buttons

### Import

Opens the Plant Model Importer dialog (see “Importing a Plant Model” on page 5-9).

### Delete

Deletes the selected model. If the model is being used elsewhere (i.e., in a controller or scenario), the first model in the list replaces it (and a warning message appears).

## Right-Click Options

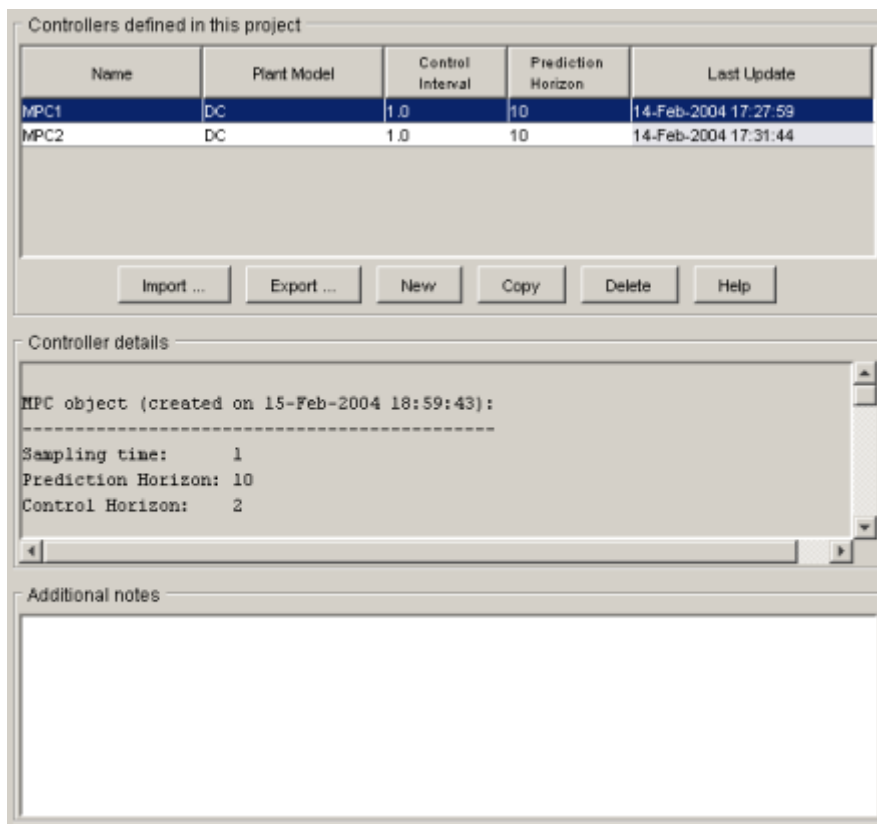
Right-clicking on the **Plant models** node causes the following menu option to appear

### Import Model

Opens the Plant Model Importer dialog (see “Importing a Plant Model” on page 5-9).

## Controllers View

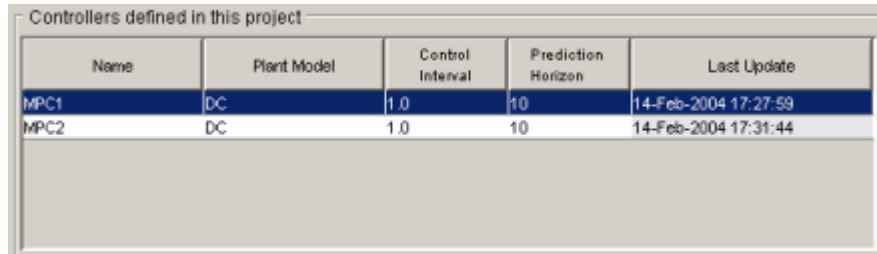
Selecting **Controllers** in the tree causes this view to appear (see example below)



The following sections describe the view's main features.

## Controllers List

This table lists all the controllers in your project. The example below lists two controllers, MPC1 and MPC2.



Name	Plant Model	Control Interval	Prediction Horizon	Last Update
MPC1	DC	1.0	10	14-Feb-2004 17:27:59
MPC2	DC	1.0	10	14-Feb-2004 17:31:44

The **Name** field is editable. The name you assign here must be unique. You will refer to it elsewhere in the design tool, e.g., when you use the controller in a simulation scenario. Each listed controller corresponds to a subnode of **Controllers** (see “The Tree View” on page 5-7). Editing the name in the table will rename the corresponding subnode.

The **Plant Model** field is editable. To change the selection, click on the cell and choose one of your models from the list. (All models appearing in the Plant Models View are valid choices. See “Plant Models View” on page 5-26)

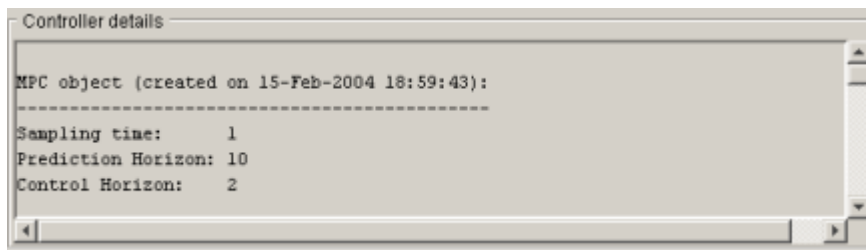
The **Control Interval** field is editable and must be a positive real number. You can also set it in the Controller Specifications view (see “Model and Horizons Tab” on page 5-36 for more details).

The **Prediction Horizon** field is editable and must be a positive, finite integer. You can also set in the Controller Specifications view (see “Model and Horizons Tab” on page 5-36 for more details).

The noneditable **Last Update** field gives the date and time the controller was most recently modified.

## Controller Details

This scrollable viewport shows details of the controller currently selected in the controllers list (see “Controllers List” on page 5-30). An example appears below



---

**Note** This view shows controller details once you have used the controller in a simulation. Prior to that, it is empty.

---

## Additional Notes

You can use this editable text area to enter comments, distinguishing controller features, etc.

## Buttons

### Import

Opens the MPC Controller Importer dialog (see “Importing a Controller” on page 5-15).

### Export

Opens the MPC Controller Exporter dialog (see “Exporting a Controller” on page 5-19).

### New

Creates a new controller specification subnode containing the default MPC Toolbox settings, and assigns it a default name.

### **Copy**

Copies the selected controller, creating a controller specification subnode containing the same controller settings, and assigning it a default name.

### **Delete**

Deletes the selected controller. If the controller is being used elsewhere (i.e., in a simulation scenario), the first controller in the list replaces it (and a warning message appears).

## **Right-Click Options**

Right-clicking on the **Controllers** node causes the following menu options to appear

### **New Controller**

Creates a new controller specification subnode containing the default MPC Toolbox settings, and assigns it a default name.

### **Import Controller**

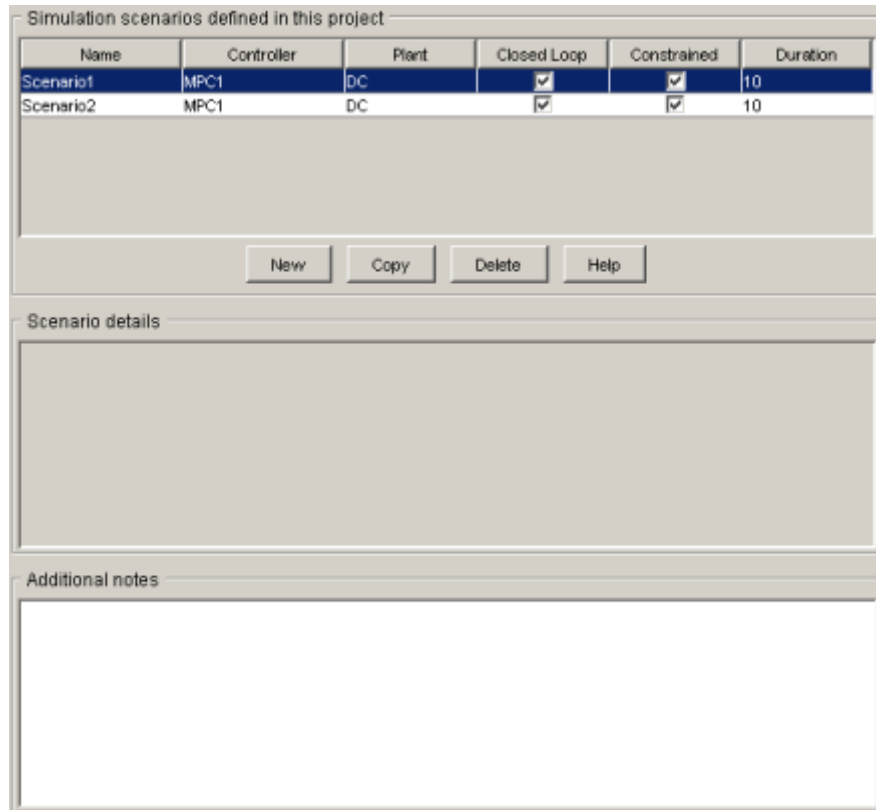
Opens the MPC Controller Importer dialog (see “Importing a Controller” on page 5-15).

### **Export Controller**

Opens the MPC Controller Exporter dialog (see “Exporting a Controller” on page 5-19).

## Simulation Scenarios List

Selecting **Scenarios** in the tree causes this view to appear (see example below)



Simulation scenarios defined in this project

Name	Controller	Plant	Closed Loop	Constrained	Duration
Scenario1	MPC1	DC	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	10
Scenario2	MPC1	DC	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	10

New Copy Delete Help

Scenario details

Additional notes

The following sections describe the view's main features.

## Scenarios List

This table lists all the scenarios in your project. The example below lists two, Scenario1 and Scenario2.

Name	Controller	Plant	Closed Loop	Constrained	Duration
Scenario1	MPC1	DC	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	10
Scenario2	MPC1	DC	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	10

The **Name** field is editable. The assigned name must be unique. Each listed scenario corresponds to a subnode of **Scenarios** (see “The Tree View” on page 5-7). Editing the name in the table will rename the corresponding subnode.

The **Controller** field is editable. To change the selection, click on the cell and choose one of your controllers from the list. (All controllers appearing in the Controllers View are valid choices. See “Controllers View” on page 5-29). You can also set this using the Scenario Specifications view (for more discussion, see “Simulation Scenario View” on page 5-59).

The **Plant** field is editable. To change the selection, click on the cell and choose one of your plant models from the list. (All models appearing in the Plant Models View are valid choices. See “Plant Models View” on page 5-26). You can also set this in the scenario specifications (for more discussion, see “Simulation Scenario View” on page 5-59).

The **Closed Loop** field is an editable checkbox. If unchecked, the simulation will be open loop. You can also set it in the scenario specifications (for more discussion see “Simulation Scenario View” on page 5-59).

The **Constrained** field is an editable checkbox. If unchecked, the simulation will ignore all constraints specified in the controller design. You can also set it in the scenario specifications (for more discussion see “Simulation Scenario View” on page 5-59).

The **Duration** field is editable and must be a positive, finite real number. It sets the simulation duration. You can also set it in the scenario specifications (for more discussion see “Simulation Scenario View” on page 5-59).



## Scenario Details

This area is blank at all times.

## Additional Notes

You can use this editable text area to enter comments, distinguishing scenario features, etc.

## Buttons

### New

Creates a new scenario specification subnode containing the default MPC Toolbox settings, and assigns it a default name.

### Copy

Copies the selected scenario, creating a scenario specification subnode containing the same settings, and assigning it a default name.

### Delete

Deletes the selected scenario.

## Right-Click Options

Right-clicking on the **Scenarios** node causes the following menu option to appear

### New Scenario

Creates a new scenario specification subnode containing the default MPC Toolbox settings, and assigns it a default name.

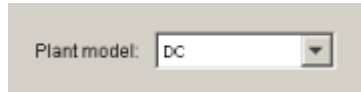
## Controller Specifications View

This view appears whenever you select one of your controller specification nodes (see “The Tree View” on page 5-7). It allows you to specify or review controller settings. It consists of four tabs, each devoted to a particular design aspect. All settings have default values, but these might not be best for your application.

### Model and Horizons Tab

The screenshot shows the 'Model and Horizons' tab of a software interface. At the top, there are four tabs: 'Model and Horizons', 'Constraints', 'Weight Tuning', and 'Estimation (advanced)'. The 'Model and Horizons' tab is active. Below the tabs, there is a 'Plant model:' label followed by a dropdown menu showing 'DC'. Below this, there is a section titled 'Horizons' containing three input fields: 'Control interval (time units):' with the value '1.0', 'Prediction horizon (intervals):' with the value '10', and 'Control horizon (intervals):' with the value '2'. Below the 'Horizons' section, there is a checkbox labeled 'Blocking (advanced)' which is currently unchecked. Below the checkbox, there is a section titled 'Blocking' containing three input fields: 'Blocking allocation within prediction horizon:' with a dropdown menu showing 'Beginning', 'Number of moves computed per step:' with the value '3', and 'Custom move allocation vector:' with the value '[ 2 3 5 ]'.

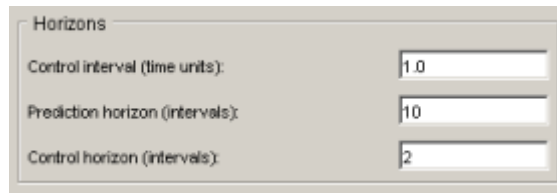
## Plant Model



Plant model: DC

This combo box allows you to specify the plant model the controller uses for its predictions. You can choose any of the plant models you've imported. (See "Importing a Plant Model" on page 5-9.)

## Horizons



Horizons

Control interval (time units):	1.0
Prediction horizon (intervals):	10
Control horizon (intervals):	2

The **Control interval** sets the elapsed time between successive controller moves. It must be a positive, finite real number. The calculations assume a zero-order hold on the manipulated variables (the signals adjusted by the controller). Thus, these signals are constant between moves.

The **Prediction horizon** sets the number of *control intervals* over which the controller predicts its outputs when computing controller moves. It must be a positive, finite integer.

The **Control horizon** sets the number of moves computed. It must be a positive, finite integer, and must not exceed the prediction horizon. If less than the prediction horizon, the final computed move fills the remainder of the prediction horizon.

For more discussion, see "A Typical Sampling Instant" on page 1-5, and "Prediction and Control Horizons" on page 1-8.

## Blocking

Blocking (advanced)

Blocking

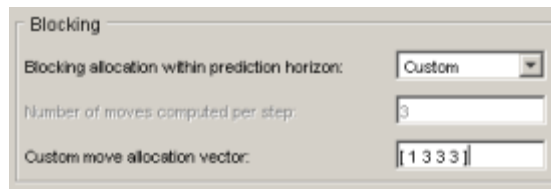
Blocking allocation within prediction horizon: Beginning

Number of moves computed per step: 3

Custom move allocation vector: [ 2 3 5 ]

By default, the **Blocking** option is unchecked (off). When on as shown above, the design tool replaces the **Control horizon** specification (see “Horizons” on page 5-37) with a move pattern determined by the following settings:

- **Blocking allocation within prediction horizon** – choices are
  - Beginning** – successive moves at the beginning of the prediction horizon, each with a duration of one control interval
  - Uniform** – the prediction horizon is divided by the number of moves and rounded to obtain an integer duration, and each computed move has this duration (the last move extends to fill the prediction horizon)
  - End** – successive moves at the end of the prediction horizon, each with a duration of one control interval
  - Custom** – you specify the duration of each computed move
- **Number of moves computed per step** – the number of moves computed when the allocation setting is **Beginning**, **Uniform**, or **End**. Must be a positive integer not exceeding the prediction horizon.
- **Custom move allocation vector** – the duration of each computed move, specified as a row vector. In the example below, there are 4 moves, the first lasting 1 control interval, and the rest lasting 3. The **Number of moves computed per step** setting is disabled (ignored).



Blocking

Blocking allocation within prediction horizon: Custom

Number of moves computed per step: 3

Custom move allocation vector: [1 3 3 3]

The sum of the vector elements should equal the prediction horizon. If not, the last move is extended or truncated automatically.

---

**Note** When **Blocking** is off, the controller uses the **Beginning** allocation with **Number of moves computed per step** equal to the **Control horizon**.

---

For more discussion, see “Blocking” on page 1-14.

## Constraints Tab

This panel allows you to specify *constraints* (bounds) on *manipulated variables* and *outputs*. Constraints can be *hard* or *soft*. By default, all variables are *unconstrained*, as shown in the view below.

Name	Units	Minimum	Maximum	Max down rate	Max up rate
Reflux Rate	moles/min				

Name	Units	Minimum	Maximum
Distillate Purity	Mole %		
Bottoms Purity	Mole %		

Advanced:

**Note** If you specify constraints, manipulated variable constraints are hard by default, whereas output variable constraints are soft by default. You can customize this behavior, as discussed in the following sections. For additional information on constraints, see “Optimization and Constraints” on page 1-10, and “Optimization Problem” on page 2-5.

## Constraints on Manipulated Variables

The example below is for an application with two manipulated variables (MVs), each represented by a table row.

Name	Units	Minimum	Maximum	Max down rate	Max up rate
Reflux Rate	moles/min	0	85	-10	10
Steam Rate	moles/min	0	52		

The **Name** and **Units** columns are noneditable. To change them, use the signal definition view. (See “Signal Definition View” on page 5-21. Any changes there apply to the entire design.)

The remaining table columns are editable. If you leave a cell blank, the controller ignores that constraint. You can achieve the same effect by entering -Inf (for a **Minimum** or **Max down rate**) or Inf (for a **Maximum** or **Max up rate**).

The **Minimum** and **Maximum** values set each MV’s range.

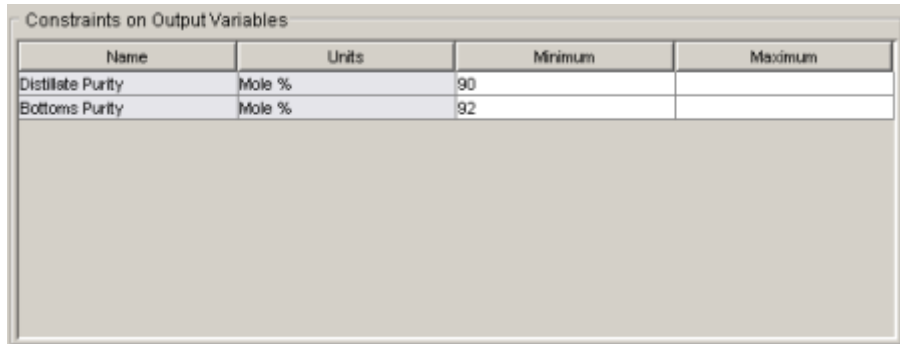
The **Max down rate** and **Max up rate values** set the amount the MV can change *in a single control interval*. The **Max down rate** must be negative or zero. The **Max up rate** must be positive or zero.

Constraint values must be consistent with your nominal values (see “Input Signal Properties” on page 5-23). In other words, each MV’s nominal value must satisfy the constraints.

Constraint values must also be self-consistent. For example, an MV’s lower bound must not exceed its upper bound.

## Constraints on Output Variables

The example below is for an application with two output variables, each represented by a table row.



Name	Units	Minimum	Maximum
Distillate Purity	Mole %	90	
Bottoms Purity	Mole %	92	

The **Name** and **Units** columns are noneditable. To change them, use the signal definition view. (See “Signal Definition View” on page 5-21. Any changes there apply to the entire design.)

The remaining table columns are editable. If you leave a cell blank (as for the **Maximum** column above), the controller ignores that constraint. You can achieve the same effect by entering - Inf (for a **Minimum**) or Inf (for a **Maximum**).

The **Minimum** and **Maximum** values set each output’s range. The controller will attempt to satisfy these constraints at all times.

Constraint values must be consistent with your nominal values (see “Output Signal Properties” on page 5-24). In other words, each output’s nominal value must satisfy the constraints.

Constraint values must also be self-consistent. For example, an output’s lower bound must not exceed its upper bound.

---

**Note** Don’t constrain outputs unless a particular constraint is an essential aspect of your application. It is usually better to define output setpoints (reference values) rather than constraints.

---



## Constraint Softening

A *hard* constraint cannot be violated. Hard constraints are risky, especially for outputs, because the controller will ignore its other objectives in order to satisfy them. The constraints might be impossible to satisfy in certain situations, in which case the controllers calculations are mathematically *infeasible*.

The MPC Toolbox allows you to specify *soft* constraints. These can be violated, but you specify a violation tolerance for each constraint (the *relaxation band*). See the example specifications below.

**Specify relaxation bands**

Input constraints

Name	Units	Minimum	Min band	Maximum	Max band	Max down rate	Max down band	Max up rate	Max up band
Reflux Rate	moles/min	0		85		-10		10	
Steam Rate	moles/min	0	2	52	2				

Output constraints

Name	Units	Minimum	Min Band	Maximum	Max Band
Distillate Purity	Mole %	90	0.5		
Bottoms Purity	Mole %	92	0.5		

Overall constraint softness

Soft constraints Hard constraints

Value:

OK Cancel Help

To open this dialog, click the **Constraint softening** button at the bottom of the **Constraints** tab in the controller specification view (see “Constraints Tab” on page 5-40).

## Input Constraints

An example input constraint specification appears below.

Name	Units	Minimum	Min band	Maximum	Max band	Max down rate	Max down band	Max up rate	Max up band
Reflux Rate	moles/min	0		85		-10		10	
Steam Rate	moles/min	0	2	52	2				

The **Name** and **Units** columns are noneditable. To change them, use the signal definition view. (See “Signal Definition View” on page 5-21. Any changes there apply to the entire design.)

The **Minimum**, **Maximum**, **Max down rate**, and **Max up rate** columns are editable. Their values are the same as on the main **Constraints** tab (see “Constraints on Manipulated Variables” on page 5-41). You can specify them in either location.

The remaining columns specify the *relaxation band* for each constraint. An empty cell is equivalent to a zero, i.e., a hard constraint.

Entries must be zero or positive real numbers. To soften a constraint, increase its relaxation band.

The example above shows a relaxation band of 2 moles/min for the steam flow rate’s lower and upper bounds. The lack of a relaxation band setting for the reflux flow rate’s four constraints means that these will be hard.

---

**Note** The relaxation band is a relative tolerance, not a strict bound. In other words, the actual constraint violation can exceed the relaxation band.

---

## Output Constraints

An example output constraint specification appears below.

Name	Units	Minimum	Min Band	Maximum	Max Band
Distillate Purity	Mole %	90	0.5		
Bottoms Purity	Mole %	92	0.2		

The **Name** and **Units** columns are noneditable. To change them, use the signal definition view. (See “Signal Definition View” on page 5-21. Any changes there apply to the entire design.)

The **Minimum** and **Maximum** columns are editable. Their values are the same as on the main **Constraints** tab (see “Constraints on Output Variables” on page 5-42). You can specify them in either location.

The remaining columns specify the *relaxation band* for each constraint. An empty cell is equivalent to 1.0, i.e., a *soft* constraint.

Entries must be zero or positive real numbers. To soften a constraint, increase its relaxation band.

The example above shows a relaxation band of 0.5 Mole % for the distillate purity lower bound, and a relaxation band of 0.2 Mole % for the bottoms purity lower bound (the harder of the two constraints).

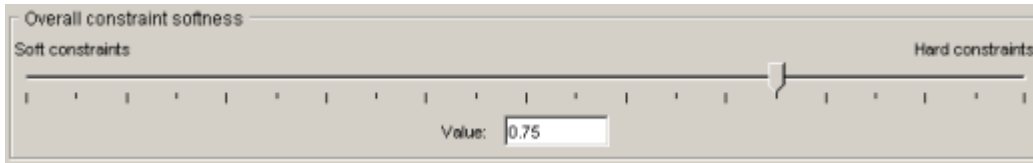
---

**Note** The relaxation band is a relative tolerance, not a strict bound. In other words, the actual constraint violation can exceed the relaxation band.

---

## Overall Constraint Softness

The relaxation band settings allow you to adjust the hardness/softness of each constraint. You can also soften/harden all constraints simultaneously using the slider at the bottom of the dialog panel.



You can move the slider or edit the value in the edit box, which must be between 0 and 1.

### Buttons

**OK** – Closes the constraint softening dialog, implementing changes to the tabular entries or the slider setting.

**Cancel** – Closes the constraint softening dialog without changing anything.

## Weight Tuning Tab

The example below shows the MPC Toolbox default tuning weights for an application with two manipulated variables and two outputs.

Model and Horizons | Constraints | **Weight Tuning** | Estimation (advanced)

Overall

More robust Faster response

Value:

Input weights

Name	Description	Units	Weight	Rate weight
Reflux Rate	Reflux Flow Rate	moles/min	0	0.1
Steam Rate	Steam Flow Rate	moles/min	0	0.1

Output weights

Name	Description	Units	Weight
Distillate Purity	Distillate Purity	Mole %	1.0
Bottoms Purity	Bottoms Purity	Mole %	1.0

The following sections discuss the three panel areas in more detail. For additional information, see “Optimization Problem” on page 2-5.

## Input Weights

Name	Description	Units	Weight	Rate weight
Reflux Rate	Reflux Flow Rate	moles/min	0	0.1
Steam Rate	Steam Flow Rate	moles/min	0	0.1

The **Name**, **Description**, and **Units** columns are noneditable. To change them, use the signal definition view. (See “Signal Definition View” on page 5-21. Any changes there apply to the entire design.)

The **Weight** column sets a penalty on deviations of each manipulated variable (MV) from its *nominal value*. The weight must be zero or a positive real number. The default is zero, meaning that the corresponding MV can vary freely provided that it satisfies its constraints (see “Constraints on Manipulated Variables” on page 5-41).

A large **Weight** discourages the corresponding MV from moving away from its nominal value. This can cause *steady state error* (offset) in the output variables unless you have extra MVs at your disposal.

---

**Note** To set the nominal values, use the signal definition view. (See “Signal Definition View” on page 5-21. Any changes there apply to the entire design.)

---

The **Rate Weight** value sets a penalty on MV *changes*, i.e., on the magnitude of each MV move. Increasing the penalty on a particular MV causes the controller to change it more slowly. The table entries must be zero or positive real numbers. These values have no effect in steady state.

## Output Weights

Name	Description	Units	Weight
Distillate Purity	Distillate Purity	Mole %	1.0
Bottoms Purity	Bottoms Purity	Mole %	1.0

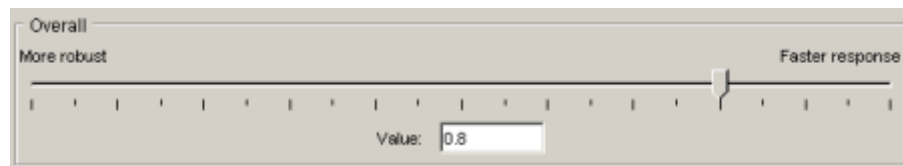
The **Name**, **Description**, and **Units** columns are noneditable. To change them, use the signal definition view. (See “Signal Definition View” on page 5-21. Any changes there apply to the entire design.)

The **Weight** column sets a penalty on deviations of each output variable from its *setpoint* (or *reference*) *value*. The weight must be zero or a positive real number.

A large **Weight** discourages the corresponding output from moving away from its setpoint.

If you don’t want to hold a particular output at a setpoint, set its **Weight** to zero. This may be the case, for example, when an output doesn’t have a target value and is being used as an indicator variable only.

## Overall (Slider Control)



The slider adjusts the weights on all variables simultaneously. Moving the slider to the left increases rate penalties relative to setpoint penalties, which often (but not always!) increases controller robustness. The disadvantage is that disturbance rejection and setpoint tracking become more sluggish.

You can also change the value in the edit box. It must be a real number between 0 and 1. The actual effect is nonlinear. You will generally need to run trials to determine the best setting.

## Estimation Tab

Use these specifications to shape the controller's response to unmeasured disturbances and measurement noise.

The example below shows the MPC Toolbox default settings for an application with two output variables and no unmeasured disturbance inputs.

The screenshot shows the 'Estimation (advanced)' tab in the MPC Toolbox. It features a 'Use MPC defaults' button and a slider for 'Overall estimator gain' set to 0.5. Below this are tabs for 'Output disturbances', 'Input disturbances', and 'Measurement noise'. The 'Output disturbances' tab is active, showing a table of disturbances and a 'Signal-by-signal' radio button selected.

Name	Units	Type	Magnitude
Distillate Purity	Mole %	Steps	1.0
Bottoms Purity	Mole %	Steps	1.0

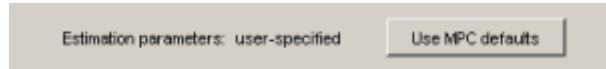
Below the table, there is a radio button for 'LTI model in Workspace' and a 'Browse ...' button. At the bottom, a block diagram shows a 'Plant' block with inputs MD, MV, and UD. The plant output is summed with an 'Unmeasured Disturbance' (indicated by a downward arrow and a plus sign) to produce the 'Outputs'.

The following sections cover each estimation feature in detail. For additional information, see “State Estimation” on page 1-13, and “State Estimation” on page 2-8.



### Button (MPC Default Settings)

If you edit any of the Estimation tab settings, the display near the top will appear as follows



To return the settings to the default state, click the Use MPC defaults button, causing the display to revert to the default condition shown below



### Overall Estimator Gain



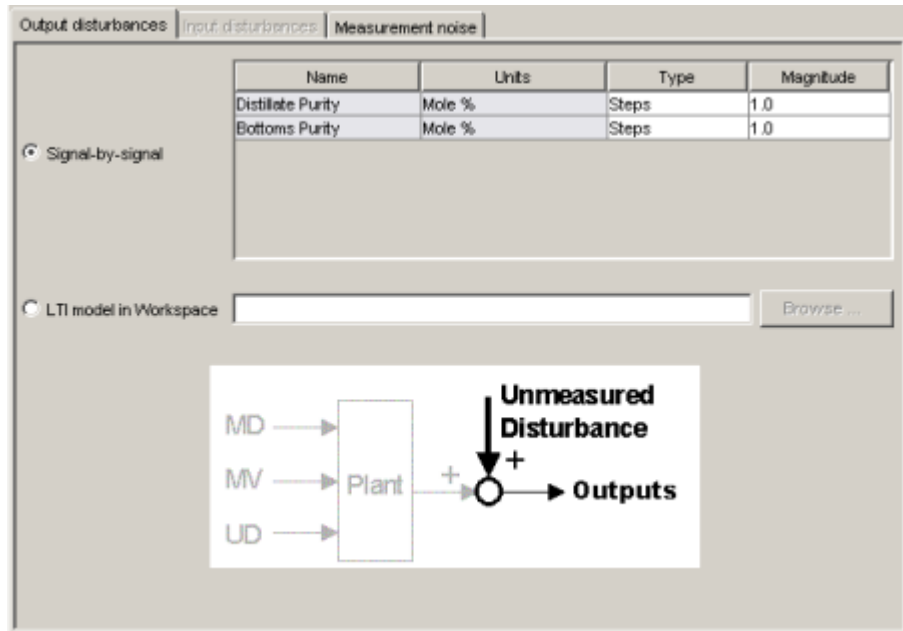
This slider determines the controller's overall disturbance response. As you move the slider to the left, the controller responds less aggressively to unexpected changes in the outputs, i.e., it assumes that such changes are more likely to be caused by measurement noise rather than a *real* disturbance.

You can also change the value in the edit box. It must be between zero and 1. The effect is nonlinear, and you might need to run trial simulations to achieve the desired result.

## Output Disturbances

Use these settings to model unmeasured disturbances adding to the plant outputs.

The example below shows the tab's appearance with the **Signal-by-signal** option selected for an application having two plant outputs.



The graphic shows the disturbance location.

Use the table to specify the disturbance character for each output.

The **Name** and **Units** columns are noneditable. To change them, use the signal definition view. (See “Signal Definition View” on page 5-21. Any changes there apply to the entire design.)

The **Type** column sets the disturbance character. To edit this, click the cell and select from the resulting menu. You have the following options:

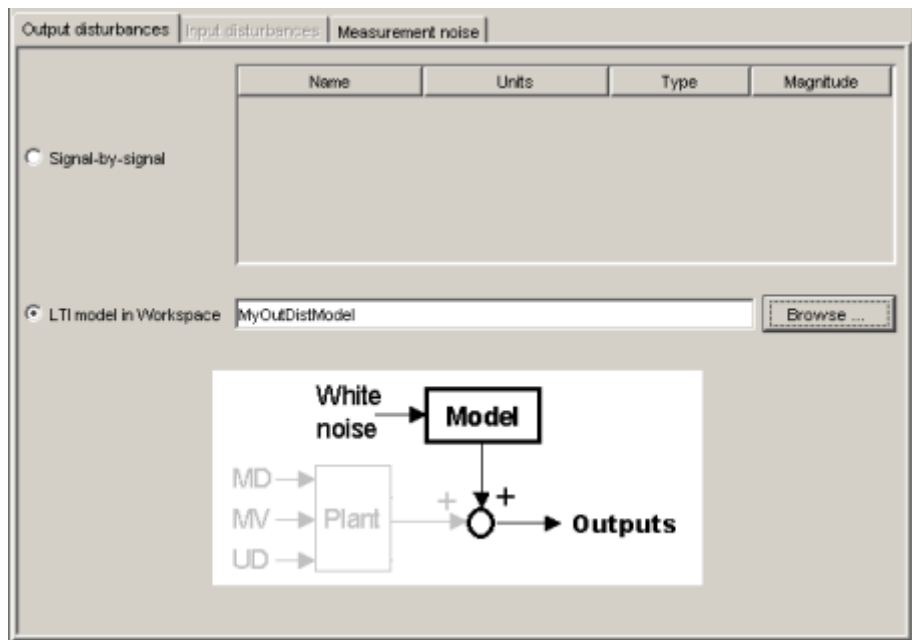
- **Steps** – simulates random step-like disturbances (integrated white noise)
- **Ramps** – simulates a random drifting disturbance (doubly-integrated white noise)

- **White** – white noise

The **Magnitude** column specifies the standard deviation of the white noise assumed to create the disturbance. Set it to zero if you want to turn off a particular disturbance.

For example, if **Type** is **Steps** and **Magnitude** is 2, the disturbance model is integrated white noise, where the white noise has a standard deviation of 2.

If these options are too restrictive, select the **LTI model in Workspace** option. The tab appearance changes to the view shown below



You must specify an LTI output disturbance model residing in your workspace. The **Browse** button opens a dialog listing all LTI models in your workspace, and allows you to choose one. You can also type the model name in the edit box, as shown above.

The model must have the same number of outputs as the plant.

The white noise entering the model is assumed to have unity standard deviation.

## Input Disturbances

Use these settings to model disturbances affecting the plant's unmeasured disturbance inputs.

The example below shows the tab's appearance with the **Signal-by-signal** option selected for a plant having one unmeasured disturbance input. The graphic shows the disturbance location.

The screenshot shows the 'Input disturbances' tab in a software interface. It features a table with the following data:

Name	Units	Type	Magnitude
Feed Rate	moles/min	Steps	1.0

Below the table, the 'Signal-by-signal' radio button is selected. There is also an option for 'LTI model in Workspace' with a 'Browse ...' button. At the bottom, a block diagram shows a 'Plant' block with three inputs: 'MD', 'MV', and 'Unmeasured Disturbance', and two outputs: 'MO' and 'UO'.

Use the table to specify the character of each unmeasured disturbance input.

The **Name** and **Units** columns are noneditable. To change them, use the signal definition view. (See “Signal Definition View” on page 5-21. Any changes there apply to the entire design.)

The **Type** column sets the disturbance character. To edit this, click the cell and select from the resulting menu. You have the following options:

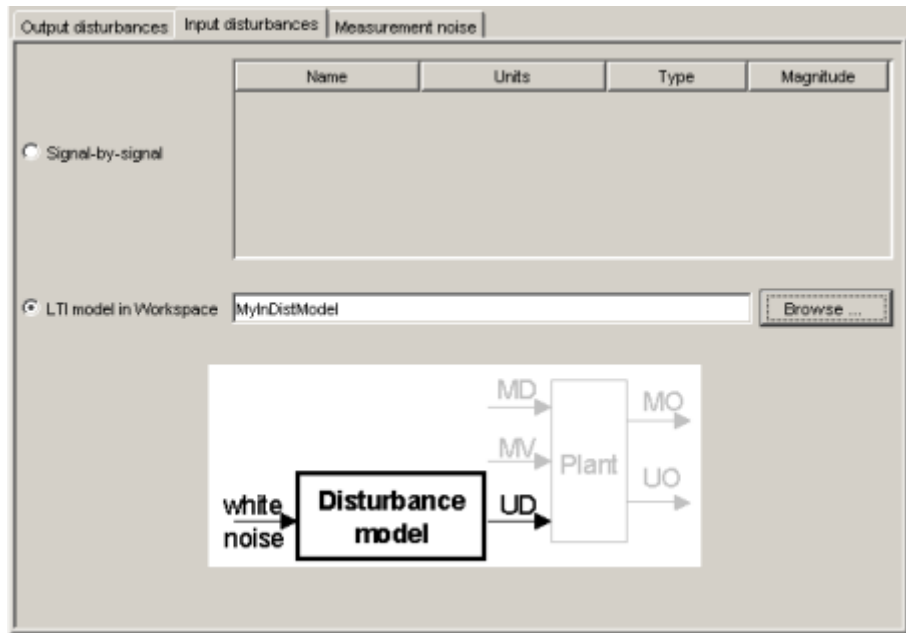
- **Steps** – simulates random step-like disturbances (integrated white noise)
- **Ramps** – simulates a random drifting disturbance (doubly-integrated white noise)

- **White** – white noise

The **Magnitude** column specifies the standard deviation of the white noise assumed to create the disturbance. Set it to zero if you want to turn off a particular disturbance.

For example, if **Type** is **Steps** and **Magnitude** is 2, the disturbance model is integrated white noise, where the white noise has a standard deviation of 2.

If the above options are too restrictive, select the **LTI model in Workspace** option. The tab appearance changes to the view shown below



You must specify an LTI disturbance model residing in your workspace. The **Browse** button opens a dialog listing all LTI models in your workspace, and allows you to choose one. You can also type the model name in the edit box, as shown above.

The number of model outputs must equal the number of plant unmeasured disturbance inputs. The white noise entering the model is assumed to have unity standard deviation.

## Noise

Use these settings to model noise in the plant's measured outputs.

The example below shows the tab's appearance with the **Signal-by-signal** option selected for a plant having two measured outputs. The graphic shows the noise location.

Output disturbances | Input disturbances | **Measurement noise**

Name	Units	Type	Magnitude
Distillate Purity	Mole %	White	1.0
Bottoms Purity	Mole %	White	1.0

Signal-by-signal

LTI model in Workspace

Diagram: A block labeled 'Plant' has three input arrows labeled MD, MV, and UD. It has two output arrows: one labeled 'Measured Outputs' and one labeled 'Unmeasured Outputs'. A 'Measurement noise' input, represented by a downward arrow with a plus sign, enters a summing junction (a circle with a plus sign) that is added to the 'Measured Outputs' signal.

Use the table to specify the character of each noise input.

The **Name** and **Units** columns are noneditable. To change them, use the signal definition view. (See “Signal Definition View” on page 5-21. Any changes there apply to the entire design.)

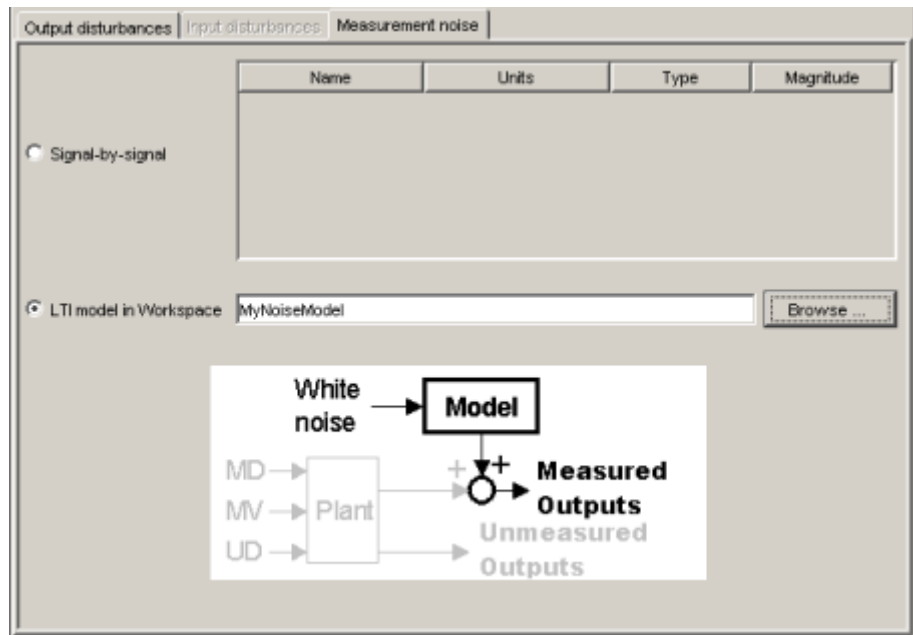
The **Type** column sets the noise character. To edit this, click the cell and select from the resulting menu. You have the following options:

- **White** – white noise
- **Steps** – simulates random step-like disturbances (integrated white noise)

The **Magnitude** column specifies the standard deviation of the white noise assumed to create the noise. Set it to zero if you want to specify that an output is noise-free.

For example, if **Type** is **Steps** and **Magnitude** is 2, the noise model is integrated white noise, where the white noise has a standard deviation of 2.

If the above options are too restrictive, select the **LTI model in Workspace** option. The tab appearance changes as follows



You must specify an LTI model residing in your workspace. The **Browse** button opens a dialog listing all LTI models in your workspace, and allows you to choose one. You can also type the model name in the edit box, as shown above.

The number of noise model outputs must equal the number of plant measured outputs.

The white noise entering the model is assumed to have unity standard deviation.

## **Right-Click Menus**

### **Copy Controller**

Creates a new controller having the same settings and a default name.

### **Delete Controller**

Deletes the controller. If the controller is being used in a simulation scenario, the design tool replaces it with the first controller in your list, and displays a warning message.

### **Rename Controller**

Opens a dialog allowing you to rename the controller.

---

**Note** Each controller in a design project/task must have a unique name.

---

### **Export Controller**

Opens the MPC Controller Exporter dialog (see “Exporting a Controller” on page 5-19).



## Simulation Scenario View

This view appears whenever you select one of your scenario specification nodes (see “The Tree View” on page 5-7). It allows you to specify simulation settings and independent variables. All have default values, but you will want to change at least some of them (otherwise all independent variables will be constant). Defaults for a plant with three inputs and two outputs appears below.

**Simulation settings**

Controller:       Close loops:

Plant:       Enforce constraints:

Duration:       Control interval: 1

---

**Setpoints**

Name	Units	Type	Initial value	Size	Time	Period	Look ahead
Distillate Purity	Mole %	Constant	0.0				<input type="checkbox"/>
Bottoms Purity	Mole %	Constant	0.0				<input type="checkbox"/>

---

**Measured disturbances**

Name	Units	Type	Initial value	Size	Time	Period	Look ahead
Steam Rate	moles/min	Constant	0.0				<input type="checkbox"/>

---

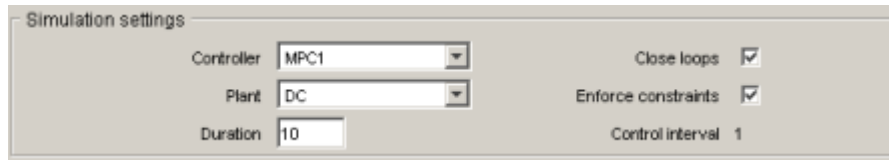
**Unmeasured disturbances**

Name	Units	Type	Initial value	Size	Time	Period
Feed Rate	moles/min	Constant	0.0			
Distillate Purity	Mole %	Constant	0.0			
Reflux Rate	moles/min	Constant	0.0			

If your application omits measured disturbance inputs, the middle table won't appear.

The following sections describe each of the dialog panel's features.

## Simulation Settings



Simulation settings

Controller: MPC1

Plant: DC

Duration: 10

Close loops:

Enforce constraints:

Control interval: 1

Use this section to set the following:

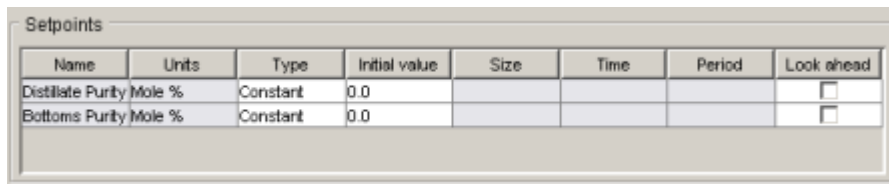
- **Controller** – select one of your controllers
- **Plant** – select the plant model that will act as the “real” plant in the simulation, i.e., it need not be the same as that used for controller predictions.
- **Duration** – the simulation duration in time units
- **Close loops** – if unchecked, the simulation will be open-loop
- **Enforce Constraints** – if unchecked, all controller constraints will be ignored

The **Control interval** field is display-only, and reflects the setting in your **Controller** selection. You can change it there if necessary (see “Model and Horizons Tab” on page 5-36).

## Setpoints

**Note** Setpoint specifications affect *closed-loop* simulations only.

Use this table to specify the setpoint for each output. In the example below, which is for an application having two plant outputs, both setpoints would be constant at 0.0.



Name	Units	Type	Initial value	Size	Time	Period	Look ahead
Distillate Purity Mole %		Constant	0.0				<input type="checkbox"/>
Bottoms Purity Mole %		Constant	0.0				<input type="checkbox"/>

The **Name** and **Units** columns are display-only. To change them, use the signal definition view. (See “Signal Definition View” on page 5-21. Any changes apply to the entire design.)

The **Type** column specifies the setpoint variation. To change this, click on the cell and select a choice from the resulting menu.

The significance of the **Initial value**, **Size**, **Time**, and **Period** columns depends on the **Type**. If a cell is gray (noneditable), it doesn’t apply to the **Type** you’ve chosen.

For details on the signal types, see “Signal Type Settings” on page 5-64.

If the **Look ahead** option is checked (i.e., on), the controller will use future values of the setpoints in its calculations. This improves setpoint tracking, but knowledge of future setpoint changes is unusual in practice.

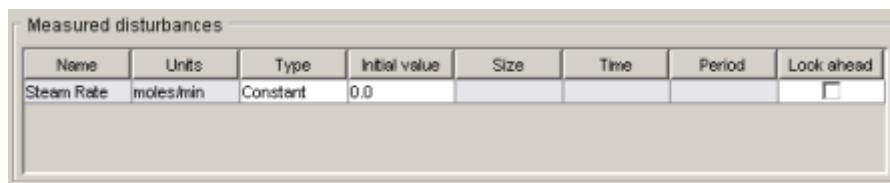
---

**Note** In the current implementation, checking or unchecking the **Look ahead** option for one output will set the others to the same state. The MPC Toolbox code does not allow you to **Look ahead** for some outputs but not for others.

---

## Measured Disturbances

Use this table to specify the variation of each measured disturbance. In the example below, which is for an application having a single measured disturbance, the “Steam Rate” input would be constant at 0.0.



Name	Units	Type	Initial value	Size	Time	Period	Look ahead
Steam Rate	moles/min	Constant	0.0				<input type="checkbox"/>

The **Name** and **Units** columns are display-only. To change them, use the signal definition view. (See “Signal Definition View” on page 5-21. Any changes apply to the entire design.)

The **Type** column specifies the disturbance variation. To change this, click on the cell and select a choice from the resulting menu.

The significance of the **Initial value**, **Size**, **Time**, and **Period** columns depends on the **Type**. If a cell is gray (noneditable), it doesn't apply to the **Type** you've chosen.

For details on the signal types, see "Signal Type Settings" on page 5-64.

If the **Look ahead** option is checked (i.e., on), the controller will use future values of the measured disturbance(s) in its calculations. This improves disturbance rejection, but knowledge of future disturbances is unusual in practice. *It has no effect in an open-loop simulation.*

---

**Note** In the current implementation, checking or unchecking the **Look ahead** option for one input will set the others to the same state. The MPC Toolbox code does not allow you to **Look ahead** for some inputs but not for others.

---

## Unmeasured Disturbances

Use this table to specify the variation of each measured unmeasured disturbance. In the example below, all would be constant at 0.0.

Name	Units	Type	Initial value	Size	Time	Period
Feed Rate	moles/min	Constant	0.0			
Distillate Purity	Mole %	Constant	0.0			
Reflux Rate	moles/min	Constant	0.0			

### Unmeasured Disturbance Locations

You can cause unmeasured disturbances to occur in any of the following locations:

- The plant's unmeasured disturbance (UD) inputs (if any)
- The plant's measured outputs (MO)
- The plant's manipulated variable (MV) inputs

All of the above will appear as rows in the table. In the case of a measured output or manipulated variable, the disturbance is an additive bias.

The **Name** and **Units** columns are display-only. To change them, use the signal definition view. (See “Signal Definition View” on page 5-21. Any changes apply to the entire design.)

The **Type** column specifies the disturbance variation. To change this, click on the cell and select a choice from the resulting menu.

The significance of the **Initial value**, **Size**, **Time**, and **Period** columns depends on the **Type**. If a cell is gray (noneditable), it doesn’t apply to the **Type** you’ve chosen.

For details on the signal types, see “Signal Type Settings” on page 5-64.

### Open-Loop Simulations

For open-loop simulations, you can vary the MV unmeasured disturbance to simulate the plant’s response to a particular MV. The MV signal coming from the controller stays at its nominal value, and the MV unmeasured disturbance adds to it.

For example, suppose Reflux Rate is an MV, and the corresponding row in the table below represents an unmeasured disturbance in this MV.

Name	Units	Type	Initial value	Size	Time	Period
Feed Rate	moles/min	Constant	0.0			
Distillate Purity	Mole %	Constant	0.0			
Reflux Rate	moles/min	Constant	0.0			

You could set it to a constant value of 1 to simulate the plant’s open-loop unit-step response to the Reflux Rate input. (In a closed-loop simulation, controller adjustments would also contribute, changing the response.)

Similarly, an unmeasured disturbance in an MO adds to the output signal coming from the plant. If there are no changes at the plant input, the plant outputs are constant, and you see only the change due to the disturbance. This allows you to check the disturbance character before running a closed-loop simulation.

## Signal Type Settings

The table below is an example that uses each of the six available signal types. The cells with white backgrounds are the entries you must supply. All have defaults.

Unmeasured disturbances						
Name	Units	Type	Initial value	Size	Time	Period
Out1		Constant	-2			
Out2		Step	3	2	10	
Out3		Ramp	1	0.5	5	
In1		Sine	-1	3	2	0.1
In2		Pulse	4	-3	7	2
In3		Gaussian	-3	0.7	5	

### Constant

The signal value equals the specified **Initial value** for the entire simulation.

$$y = y_0 \text{ for } t \geq 0$$

### Step

Prior to **Time**, the signal = **Initial value**. At **Time**, the signal changes step-wise by **Size** units. Its value thereafter = **Initial value** + **Size**.

$$y = y_0 \text{ for } 0 \leq t < t_0 \text{ where } y_0 = \text{Initial value, } t_0 = \text{Time}$$

$$y = y_0 + M \text{ for } t \geq t_0 \text{ where } M = \text{Size}$$

### Ramp

Prior to **Time**, the signal = **Initial value**. At **Time**, the signal begins to vary linearly with slope **Size**.

$$y = y_0 \text{ for } 0 \leq t < t_0 \text{ where } y_0 = \text{Initial value, } t_0 = \text{Time}$$

$$y = y_0 + M(t - t_0) \text{ for } t \geq t_0 \text{ where } M = \text{Size}$$

### Sine

Prior to **Time**, the signal = **Initial value**. At **Time**, the signal begins to vary sinusoidally with amplitude **Size** and period **Period**.

$y = y_0$  for  $0 \leq t < t_0$  where  $y_0 = \mathbf{Initial\ value}$ ,  $t_0 = \mathbf{Time}$

$y = y_0 + M \sin[\omega(t - t_0)]$  for  $t \geq t_0$  where  $M = \mathbf{Size}$ ,  $\omega = 2\pi/\mathbf{Period}$

### Pulse

Prior to **Time**, the signal = **Initial value**. At **Time**, a square pulse of duration **Period** and magnitude **Size** occurs.

$y = y_0$  for  $0 \leq t < t_0$  where  $y_0 = \mathbf{Initial\ value}$ ,  $t_0 = \mathbf{Time}$

$y = y_0 + M$  for  $t_0 \leq t < t_0 + T$  where  $M = \mathbf{Size}$ ,  $T = \mathbf{Period}$

$y = y_0$  for  $t \geq t_0 + T$

### Gaussian

Prior to **Time**, the signal = **Initial value**. At **Time**, the signal begins to vary randomly about **Initial value** with standard deviation **Size**.

$y = y_0$  for  $0 \leq t < t_0$  where  $y_0 = \mathbf{Initial\ value}$ ,  $t_0 = \mathbf{Time}$

$y = y_0 + M \text{randn}$  for  $t \geq t_0$  where  $M = \mathbf{Size}$

randn is MATLAB's random-normal function, which generates random numbers having zero mean and unit variance.

## Simulation Button

Click the **Simulate** button to simulate the scenario. You can also type `ctrl-R`, use the tool bar icon (see "The Tool Bar" on page 5-6), or use the **MPC/Simulate** menu option (see "The Menu Bar" on page 5-3).

## Right-Click Menus

### Copy Scenario

Creates a new simulation scenario having the same settings and a default name.

**Delete Scenario**

Deletes the scenario.

**Rename Scenario**

Opens a dialog allowing you to rename the scenario.

---

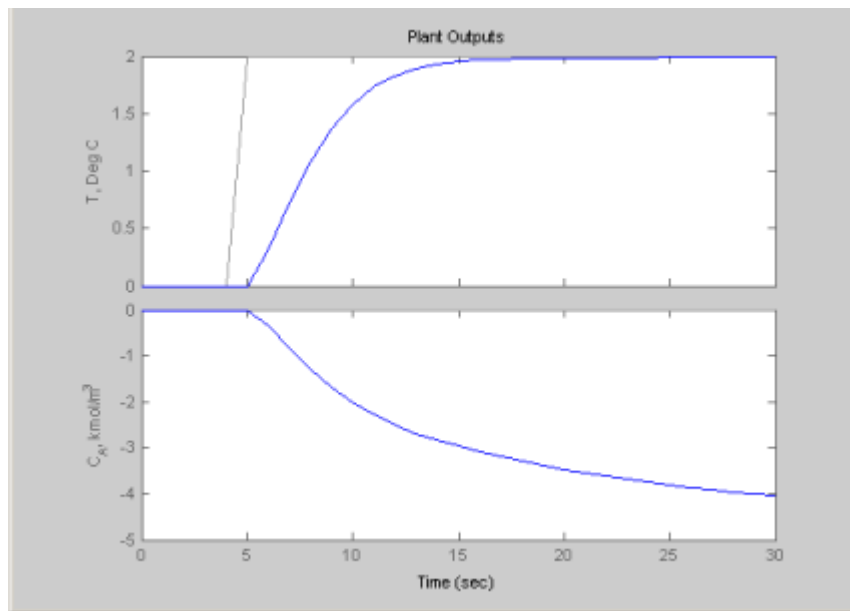
**Note** Each scenario in a design project/task must have a unique name.

---



## Response Plots

Each time you simulate a scenario, the design tool plots the corresponding plant input and output responses. The graphic below shows such a *response plot* for a plant having two outputs (the corresponding input response plot is not shown).



By default, each plant signal plots in its own graph area (as shown above). If the simulation is closed loop, each output signal plot include the corresponding setpoint.

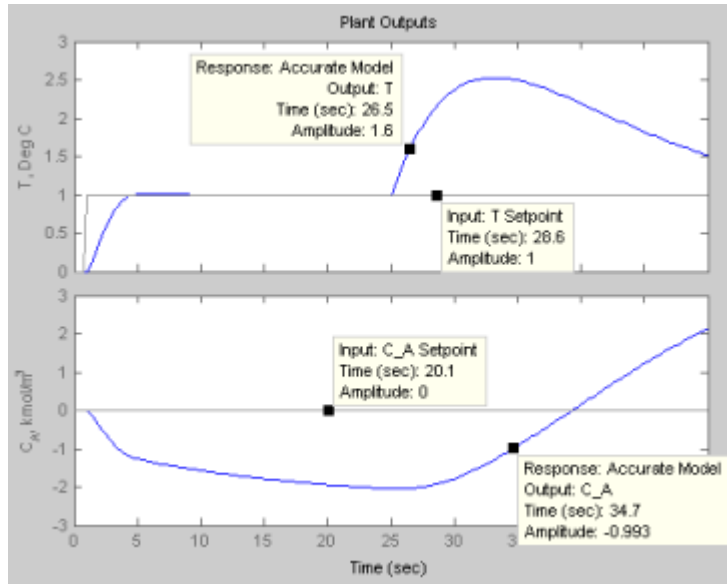
The following sections describe response plot customization options.

### Data Markers

You can use data markers to label a curve or to display numerical details.

## Adding a Data Marker

To add a data marker, click on the desired curve at the location you want to mark. The following graph shows a marker added to each output response and its corresponding setpoint.



## Data Marker Contents

Each data marker provides information about the selected point, as follows:

- **Response** – the *scenario* that generated the curve
- **Time** – the time value at the data marker location
- **Amplitude** – the signal value at the data marker location
- **Output** – the plant variable name (plant outputs only)
- **Input** – [\*\*\* this needs to be fixed \*\*\*]

## Changing a Data Marker's Alignment

To relocate the data marker's label (without moving the marker), right-click on the marker, and select one of the four **Alignment** menu options. The above example shows three of the possible four alignment options.

### Relocating a Data Marker

To move a marker, left-click on it (holding down the mouse key) and drag it along its curve to the desired location.

### Deleting Data Markers

To delete all data markers in a plot, click in the plot's white space.

To delete a single data marker, right-click on it and select the **Delete** option.

### Right-Click Options

Right-click on a data marker to use one of the following options:

- **Alignment** – relocate the marker's label
- **Font Size** – change the label's font size
- **Movable** – on/off option that makes the marker movable or fixed
- **Delete** – deletes the selected marker
- **Interpolation** – Interpolate linearly between the curve's data points, or locate at the nearest data point
- **Track Mode** – Changes the way the marker responds when you drag it

### Displaying Multiple Scenarios

By default the response plots include all the scenarios you've simulated. The example below shows a response plot for a plant with two outputs. The data markers indicate the two scenarios being plotted: "Accurate Model" and "Perturbed Model". Both scenarios use the same setpoints (not marked – the lighter solid lines).

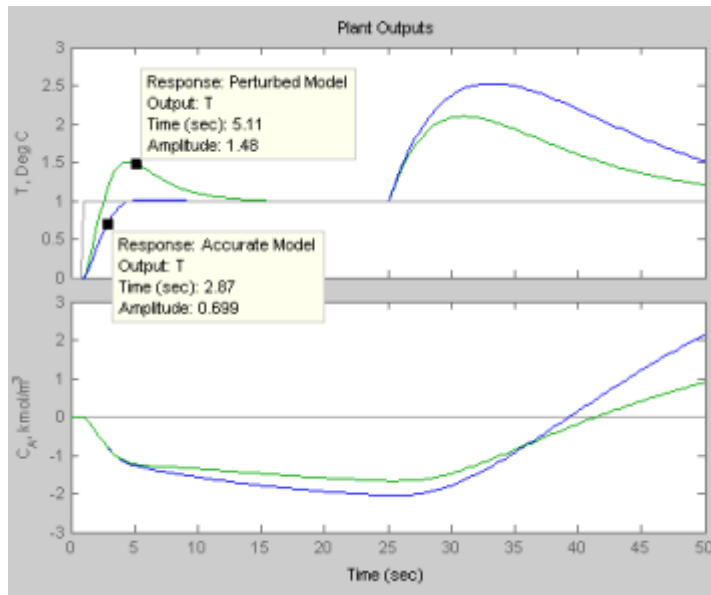
### Viewing Selected Scenarios

If your plots are too cluttered, you can hide selected scenarios. To do so, right-click in the plot's white space, choose **Responses** from the resulting menu, then toggle responses (i.e., scenarios) on or off using the submenu.

---

**Note** This selection affects all variables being plotted.

---



### Revising a Scenario

If you modify and recalculate a scenario, its data are replotted, replacing the original curves.

### Viewing Selected Variables

By default, the design tool plots all plant inputs in a single window, and plots all plant outputs in another. If your application involves many signals, the plots of each may be too small to view comfortably.

Therefore, you can control the variables being plotted. To do so, right-click in a plot's white space and choose **I/O Selector** from the resulting menu. A dialog box appears, on which you can opt to show or hide each variable.

### Grouping Variables in a Single Plot

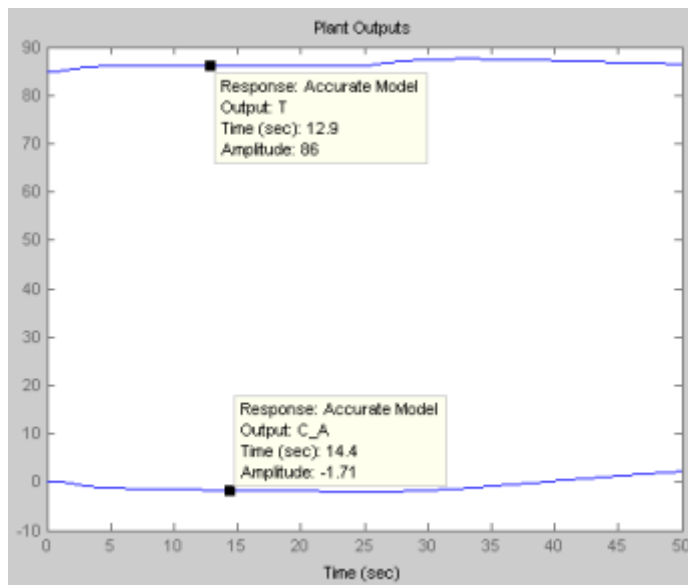
By default, each variable appears in its own plot area. You can instead choose to display variables together in a single plot. To do so, right-click in a plot's white space select **I/O Grouping**, and then select **All**.

To return to the default mode, use the **I/O Grouping: None** option.

## Normalizing Response Amplitudes

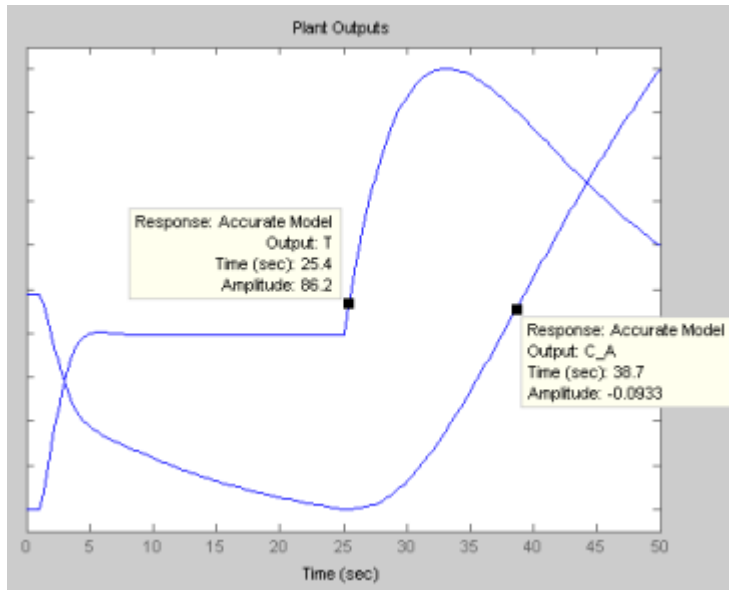
When you're using the **I/O Grouping: All** option, you might find that the variables have very different scales, making it very difficult to view them together. You can choose to *normalize* the curves, so that each expands or contracts to fill the available plot area.

For example, the plot below shows two plant outputs together (**I/O Grouping: All** option). The outputs have very different magnitudes, so together they plot as nearly straight lines at the extremes of the y-axis scale.



The plot below shows the normalized version, which displays each curve's variations clearly.

The y-axis scale is no longer meaningful, however. If you want to know a normalized signal's amplitude, use a data marker (see "Adding a Data Marker" on page 5-68). Note that the two data markers on the plot below are at the same normalized y-axis location, but correspond to very different amplitudes in the original (unnormalized) coordinates.



# Function Reference

---

- Functions — Categorical List (p. 6-2)    A list of available functions, sorted by category
- Functions — Alphabetical List (p. 6-5)    A list of available functions, sorted alphabetically

## Functions – Categorical List

### MPC Controller

Function Name	Description
d2d	Change MPC controller's sampling time
display	Display properties of MPC controller
get	Access/query property values
mpc	Create MPC controller
set	Set/modify MPC controller properties
setmpcsignals	Set signal types in MPC plant model
getname	Get I/O signal names in MPC prediction model
setname	Set I/O signal names in MPC prediction model
getmpcdata	Get privateMPC data structure
setmpcdata	Get privateMPC data structure

### MPC Controller Characteristics

Function Name	Description
compare	Compare two MPC objects
isempty	Test true for empty MPC controller
mpcprops	Provide help on MPC controller's properties
mpchelp	MPC property and function help
mpcverbosity	Change the level of verbosity of the MPC Toolbox
pack	Reduce size of MPC object in memory
size	Display model output/input/disturbance dimensions



## Linear Behavior of MPC Controller

Function Name	Description
<code>cloffset</code>	Compute MPC closed-loop DC gain from output disturbances to measured outputs assuming constraints are inactive at steady state
<code>ss</code>	Convert unconstrained MPC controller to state-space linear form
<code>tf</code>	Convert unconstrained MPC controller to linear transfer function
<code>zpk</code>	Convert unconstrained MPC controller to zero/pole/gain form

## MPC State

Function Name	Description
<code>mpcstate</code>	Define state for MPC controller
<code>trim</code>	Compute the steady-state value of MPC controller state for given inputs and outputs values.
<code>get</code>	Access/query MPC state properties
<code>set</code>	Set/modify MPC state properties

## MPC Computation and Simulation

Function Name	Description
<code>mpcmove</code>	Compute the MPC control action
<code>sim</code>	Simulate closed-loop/open-loop response to arbitrary reference and disturbance signals
<code>mpcsimopt</code>	Specify MPC simulation options
<code>plot</code>	Plot responses generated by MPC simulations

## State Estimation

<b>Function Name</b>	<b>Description</b>
getestim	Extract model and gain used for observer design
setestim	Modify an MPC object's linear state estimator
getindist	Retrieves the unmeasured input disturbance model
setindist	Modify the unmeasured input disturbance model
getoutdist	Retrieve unmeasured output disturbance model
setoutdist	Modify the unmeasured output disturbance model

## Quadratic Programming

<b>Function Name</b>	<b>Description</b>
qpdantz	Solve a convex quadratic program using Dantzig-Wolfe's algorithm
qpsolver	QP solver

## **Functions — Alphabetical List**

This section contains function reference pages listed alphabetically.

# cloffset

## Purpose

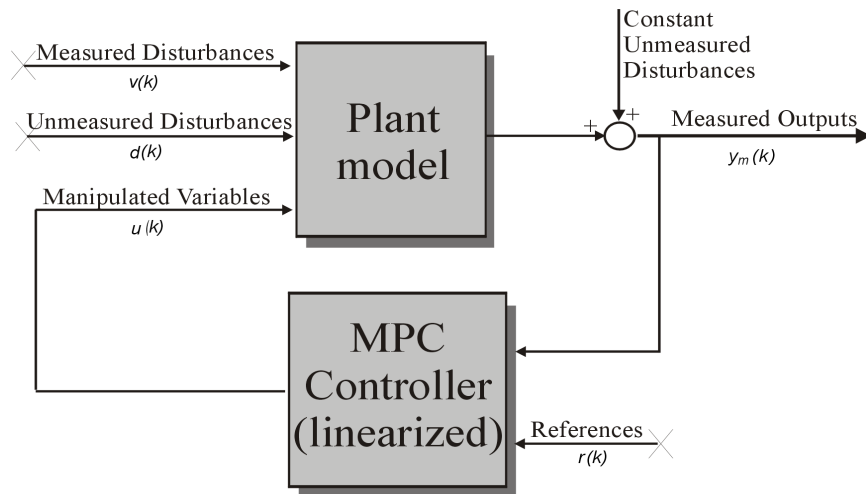
Compute MPC closed-loop DC gain from output disturbances to measured outputs assuming constraints are inactive at steady state

## Syntax

`DCgain=cloffset(MPCobj)`

## Description

The `cloff` function computes the DC-gain from output disturbances to measured outputs, assuming constraints are not active, based on the feedback connection between `Model.Plant` and the linearized MPC controller, as depicted below.



### Computing the Effect of Output Disturbances

By superposition of effects, the gain is computed by zeroing references, measured disturbances, and unmeasured input disturbances.

`DCgain=cloffset(MPCobj)` returns an  $n_{ym}$ -by- $n_{ym}$  DC gain matrix `DCgain`, where  $n_{ym}$  is the number of measured plant outputs. `MPCobj` is the MPC object specifying the controller for which the closed-loop gain is calculated.

`DCgain(i, j)` represents the gain from an additive (constant) disturbance on output  $j$  to measured output  $i$ . If row  $i$  contains all zeros, there will be no steady-state offset on output  $i$ .

**Examples** See `misocloffset.m` in `mpcdemos`

**See Also** `mpc`, `ss`

# compare

---

**Purpose** Compare two MPC objects

**Syntax** `yesno=compare(MPC1, MPC2)`

**Description** The compare function compares the contents of two MPC objects MPC1, MPC2. If the design specifications (models, weights, horizons, etc.) are identical, then yesno is equal to 1.

---

**Note** compare may return yesno=1 even if the two objects are not identical. For instance, MPC1 may have been initialized while MPC2 may have not, so that they may have different sizes in memory. In any case, if yesno=1 the behavior of the two controllers will be identical.

---

**See Also** `mpc`, `pack`

<b>Purpose</b>	Change MPC controller's sampling time
<b>Syntax</b>	<code>MPCobj=d2d(MPCobj,ts)</code>
<b>Description</b>	The <code>d2d</code> function changes the sampling time of the MPC controller <code>MPCobj</code> to <code>ts</code> . All models are sampled or resampled as soon as the QP matrices must be computed, e.g., when <code>sim</code> or <code>mpcmove</code> are used.
<b>See Also</b>	<code>mpc</code> , <code>set</code>

# get

---

**Purpose** Access/query MPC property values

**Syntax** `Value = get(MPCObj, 'PropertyName')`  
`get(MPCObj)`  
`Struct = get(MPCObj)`

**Description** `Value = get(MPCObj, 'PropertyName')` returns the current value of the property `PropertyName` of the MPC controller `MPCObj`. The string `'PropertyName'` can be the full property name (for example, `'UserData'`) or any unambiguous case-insensitive abbreviation (for example, `'user'`). You can specify any generic MPC property.

`Struct = get(MPCObj)` converts the MPC controller `MPCObj` into a standard MATLAB structure with the property names as field names and the property values as field values.

`get(MPCObj)` without a left-side argument displays all properties of `MPCObj` and their values.

**Remark** An alternative to the syntax

```
Value = get(MPCObj, 'PropertyName')
```

is the structure-like referencing

```
Value = MPCObj.PropertyName
```

For example,

```
MPCObj.Ts  
MPCObj.p
```

return the values of the sampling time and prediction horizon of the MPC controller `MPCObj`.

**See Also** `mpc`, `set`



**Purpose** Extract model and gain used for observer design

**Syntax**

```
M=getestim(MPCobj)
[M,A,Cm]=getestim(MPCobj)
[M,A,Cm,Bu,Bv,Dvm]=getestim(MPCobj)
[M,model,Index]=getestim(MPCobj,'sys')
```

**Description** `M=getestim(MPCobj)` extracts the estimator gain  $M$  used by the MPC controller `MPCobj` for observer design. The observer is based on the models specified in `MPCobj.Model.Plant`, in `MPCobj.Model.Disturbance`, by the output disturbance model (default is integrated white noise, see “Output Disturbance Model” on page 2-9), and by `MPCobj.Model.Noise`.

The state estimator is based on the linear model (cf. “State Estimation” on page 2-8)

$$x(k+1) = Ax(k) + B_u u(k) + B_v v(k)$$

$$y_m(k) = C_m x(k) + D_{vm} v(k)$$

where  $v(k)$  are the measured disturbances,  $u(k)$  are the manipulated plant inputs,  $y_m(k)$  are the measured plant outputs, and  $x(k)$  is the overall state vector collecting states of plant, unmeasured disturbance, and measurement noise models.

The estimator used in the MPC Toolbox is described in “State Estimation” on page 2-8. The estimator’s equations are

**Predicted Output Computation:**

$$\hat{y}_m(k|k-1) = C_m \hat{x}(k|k-1) + D_{vm} v(k)$$

**Measurement Update:**

$$\hat{x}(k|k) = \hat{x}(k|k-1) + M(y_m(k) - \hat{y}_m(k|k-1))$$

**Time Update:**

$$\hat{x}(k+1|k) = A\hat{x}(k|k) + B_u u(k) + B_v v(k)$$

By combining these three equations, the overall state observer is

$$\hat{x}(k+1|k) = (A - LC_m)\hat{x}(k|k) + Ly_m(k)B_u u(k) + (B_v - LD_{vm})v(k)$$

where  $L=AM$ .

`[M,A,Cm]=getestim(MPCobj)` also returns matrices  $A, C_m$  used for observer design. This includes plant model, disturbance model, noise model, offsets. The extended state is

$x$ =[plant states; disturbance models states; noise model states]

`[M,A,Cm,Bu,Bv,Dvm]=getestim(MPCobj)` retrieves the whole linear system used for observer design.

`[M,model,Index]=getestim(MPCobj, 'sys')` retrieves the overall model used for observer design (specified in the `Model` field of the MPC object) as an LTI state-space object, and optionally a structure `Index` summarizing I/O signal types.

The extended input vector of model `model` is

$u$ =[manipulated vars;measured disturbances; 1; noise exciting disturbance model;noise exciting noise model]

Model `model` has an extra measured disturbance input  $v=1$  used for handling possible nonequilibrium nominal values (see “Offsets” on page 2-4).

Input, output, and state names and input/output groups are defined for model `model`.

The structure `Index` has the fields detailed in the following table.

Field Name	Description
ManipulatedVariables	Indices of manipulated variables within input vector
MeasuredDisturbances	Indices of measured disturbances within input vector (not including offset=1)
Offset	Index of offset=1
WhiteNoise	Indices of white noise signals within input vector

---

Field Name	Description
MeasuredOutputs	Indices of measured outputs within output vector
UnmeasuredOutputs	Indices of unmeasured outputs within output vector

The model returned by `getestim` does not include the additional white noise added on manipulated variables and measured disturbances to ease the solvability of the Kalman filter design, as described in Equation 2-6 on page 2-10.

**See Also**

`setestim`, `mpc`, `mpcstate`

# getindist

---

**Purpose** Retrieves the unmeasured input disturbance model

**Syntax** `model=getindist(MPCobj)`

**Description** `model=getindist(MPCobj)` retrieves the linear discrete-time transfer function used to model unmeasured input disturbances in the MPC setup described by the MPC object `MPCobj`. Model `model` is an LTI object with as many outputs as the number of unmeasured input disturbances, and as many inputs as the number of white noise signals driving the input disturbance model.

See Figure 2-2, Model Used for State Estimation, on page 2-8 for details about the overall model used in the MPC algorithm for state estimation purposes.

**See Also** `mpc`, `setindist`, `setestim`, `getestim`, `getoutdist`

**Purpose** Get private MPC data structure

**Syntax** `mpcdata=getmpcdata(MPCobj)`

**Description** `mpcdata=getmpcdata(MPCobj)` returns the private field `MPCData` of the MPC object `MPCobj`. Here, all internal QP matrices, models, estimator gains are stored at initialization of the object. You can manually change the private data structure using the `setmpcdata` command, although you may only need this for very advanced use of the MPC Toolbox.

---

**Note** Changes to the data structure may easily lead to unpredictable results.

---

**See Also** `setmpcdata`, `set`, `get`

# getname

---

**Purpose** Get I/O signal names in MPC prediction model

**Syntax**  
`name=getname(MPCobj, 'input', I)`  
`name=getname(MPCobj, 'output', I)`

**Description**  
`name=getname(MPCobj, 'input', I)` returns the name of the I-th input signal in variable `name`. This is equivalent to `name=MPCobj.Model.Plant.InputName{I}`. The name property is equal to the contents of the corresponding `Name` field of `MPCobj.DisturbanceVariables` or `MPCobj.ManipulatedVariables`.

`name=getname(MPCobj, 'output', I)` returns the name of the I-th output signal in variable `name`. This is equivalent to `name=MPCobj.Model.Plant.OutputName{I}`. The name property is equal to the contents of the corresponding `Name` field of `MPCobj.OutputVariables`.

**See Also** `setname`, `mpc`, `set`

**Purpose** Retrieve unmeasured output disturbance model

**Syntax** `outdist=getoutdist(MPCobj)`  
`[outdist,channels]=getoutdist(MPCobj)`

**Description** `outdist=getoutdist(MPCobj)` retrieves the linear discrete-time transfer function used to model output disturbances in the MPC setup described by the MPC object `MPCobj`. Model `outdist` is an LTI object with as many outputs as the number of measured + unmeasured outputs, and as many inputs as the number of white noise signals driving the output disturbance model.

See Figure 2-2, Model Used for State Estimation, on page 2-8 for details about the overall model used in the MPC algorithm for state estimation purposes.

`[outdist,channels]=getoutdist(MPCobj)` also returns the output channels where integrated white noise was added as an output disturbance model. This is only meaningful when the default output disturbance model is used, namely when `MPCobj.OutputVariables(i).Integrators` is empty for all channels `i`. The array `channels` is empty for user-provided output disturbance models.

**See Also** `mpc`, `setoutdist`, `setestim`, `getestim`, `getindist`

**Purpose** Create MPC controller

**Syntax**

```
MPCobj=mpc(plant)
MPCobj=mpc(plant,ts)
MPCobj=mpc(plant,ts,p,m)
MPCobj=mpc(plant,ts,p,m,weights)
MPCobj=mpc(plant,ts,p,m,weights,MV,OV,DV)
MPCobj=mpc(models,ts,p,m,weights,MV,OV,DV)
MPCobj=mpc
```

**Description** `MPCobj=mpc(plant)` creates a MPC controller based on the discrete-time model `plant`. The model can be specified either as an LTI object, or as an object in the System Identification Toolbox's format (IDMODEL object), see [Using Identified Models](#) (p. 2-19).

`MPCobj=mpc(plant,ts)` also specifies the sampling time `ts` for the MPC controller. A continuous-time plant is discretized with sampling time `ts`. A discrete-time plant is resampled if its sampling time is different than the controller's sampling time `ts`. If `plant` is a discrete-time model with unspecified sampling time, namely `plant.ts=-1`, then the MPC Toolbox assumes that the plant is sampled with the controller's sampling time `ts`.

`MPCobj=mpc(plant,ts,p,m)` also specifies prediction horizon `p` and control horizon `m`.

`MPCobj=mpc(plant,ts,p,m,weights)` also specifies the structure weights of input, input increments, and output weights (see "Weights" on page 8-7).

`MPCobj=mpc(plant,ts,p,m,weights,MV,OV,DV)` also specifies limits on manipulated variables (MV) and output variables (OV), as well as equal concern relaxation values, units, etc. Names and units of input disturbances can be also specified in the optional input DV. The fields of structures MV, OV, and DV are described in "ManipulatedVariables" on page 8-3, in "OutputVariables" on page 8-5, and in "DisturbanceVariables" on page 8-6, respectively).

`MPCobj=mpc(models,ts,p,m,weights,MV,OV,DV)` where `model` is a structure containing models for plant, unmeasured disturbances, measured disturbances, and nominal linearization values, as described in "Model" on page 8-8.

`MPCobj=mpc` returns an empty MPC object.



---

**Note** Other MPC properties are specified by using `set(MPCobj,Property1,Value1,Property2,Value2,...)` or `MPCobj.Property=Value`.

---

## Examples

Define an MPC controller based on the transfer function model  $s+1/(s^2+2s)$ , with sampling time  $T_s=0.1$  s, and satisfying the input constraint  $-1 \leq u \leq 1$ :

```
Ts=.1;    %Sampling time
MV=struct('Min',-1,'Max',1);
p=20;
m=3;

mpc1=mpc(tf([1 1],[1 2 0]),Ts,p,m,[],MV);
```

## See Also

`set`, `get`

# mpchelp

---

**Purpose** MPC property and function help

**Syntax**

```
mpchelp
mpchelp name
out=mpchelp(`name`)
mpchelp(MPCobj)
mpchelp(MPCobj, 'name');
out=mpchelp(MPCobj, 'name');
```

**Description**

`mpchelp` provides a complete listing of Model Predictive Control Toolbox.

`mpchelp name` provides on-line help for the function or property name.

`out=mpchelp(`name`)` returns the help text in string, `out`.

`mpchelp(obj)` displays a complete listing of functions and properties for the MPC object, `obj`, along with the on-line help for the object's constructor.

`mpchelp(obj, 'name')` displays the help for function or property, `name`, for the MPC object, `obj`.

`out=mpchelp(obj, 'name')` returns the help text in string, `out`.

**Examples** To get help on the MPC method “getoutdist”, you can type

```
mpchelp getoutdist
```

**See Also** `mpcprops`

**Purpose** Compute the MPC control action

**Syntax** `u=mpcmove(MPCobj,x,ym,r,v)`  
`[u,Info]=mpcmove(MPCobj,x,ym,r,v)`

**Description** `u=mpcmove(MPCobj,x,ym,r,v)` computes the current input move  $u(k)$ , given the current estimated extended state  $x(k)$ , the vector of measured outputs  $y_m(k)$ , the reference vector  $r(k)$ , and the measured disturbance vector  $v(k)$ , by solving the quadratic programming problem based on the parameters contained in the MPC controller `MPCobj`.

`x` is an `mpcstate` object. It is updated by `mpcmove` through the internal state observer based on the extended prediction model (see `getestim` for details). A default initial state `x` for the first call at time  $k=0$  can be simply defined as

`x=mpcstate(MPCobj)`

`[u,Info]=mpcmove(MPCobj,x,ym,r,v)` also returns the structure `Info` containing details about the optimal control calculations. `Info` has the fields listed below.

Field Name	Description
<code>Uopt</code>	Optimal input trajectory over the prediction horizon, returned as a $p$ -by- $n_u$ dimensional array.
<code>Yopt</code>	Optimal output sequence over the prediction horizon, returned as a $p$ -by- $n_y$ dimensional array
<code>Xopt</code>	Optimal state sequence over the prediction horizon, returned as a $p$ -by- $n_x$ dimensional array, where $n_x$ =total number of states of the extended state vector
<code>Topt</code>	Prediction time vector $(0:p-1)'$

Field Name	Description
Slack	Value of the ECR slack variable $\epsilon$ at optimum
Iterations	Number of iterations needed by the QP solver
QPCode	Exit code of the QP solver

To plot the optimal input trajectory, type

```
plot(Topt,Uopt)
```

The optimal output and state trajectories can be plotted similarly. The input, output, and state sequences  $U_{opt}$ ,  $Y_{opt}$ ,  $X_{opt}$ ,  $T_{opt}$  correspond to the predicted open-loop optimal control trajectories solving the optimization problem described in “Optimization Problem” on page 2-5. The optimal trajectories might also help understand the closed-loop behavior. For instance, constraints that are active in the open-loop optimal trajectory only at late steps of the prediction horizon might not be active at all in the closed-loop MPC trajectories. The sequence of optimal manipulated variable increments can be retrieved from `MPCobj.MPCData.MPCstruct.optimalseq`.

`QPCode` returns either 'feasible', 'infeasible' or 'unreliable' (the latter occurs when the QP solver terminates because the maximum number of iterations `MPCobj.Optimizer.MaxIter` is exceeded; see `qp_dantzs` on page 6-33). When `QPCode='infeasible'`, then  $u$  is obtained by shifting the previous optimal sequence of manipulated variable rates (stored in `MPCobj.MPCData.MPCstruct.optimalseq` inside the MPC object `MPCobj`), and summing the first entry of this sequence to the previous vector of manipulated moves. You may set up different backup strategies for handling infeasible situations by discarding  $u$  and replacing it with a different emergency decision-variable vector.

$r/v$  can be either a sample (no future reference/disturbance known in advance) or a sequence of samples (when a preview / look-ahead / anticipative effect is desired). In the latter case, they must be an array with as many rows as  $p$  and as many columns as the number of outputs/measured disturbances, respectively. If the number of rows is smaller than  $p$ , the last sample is extended constantly over the horizon, to obtain the correct size.

The default for  $y$  and  $r$  is `MPCobj.Model.Nominal.Y`. The default for  $v$  is obtained from `MPCobj.Model.Nominal.U`. The default for  $x$  is `mpcstate(MPCobj,MPCobj.Model.Nominal.X,0,0,U0)` where  $U0$  are the entries from `MPCobj.Model.Nominal.U` corresponding to manipulated variables.

To bypass the MPC Controller block's internal estimator and use your own state observer to update the MPC state yourself, you can for instance use the syntax

```

xp=x.plant; xd=x.dist; xn=x.noise;      % Save current state
u=mpcmove(MPCobj,x,ym,r,v);            % x will be updated
% Now call to your state update function:
[xp,xd,xn]=my_estimator(xp,xd,xn,ym); % States get updated
x.plant=xp;x.dist=xd;x.noise=xn;

```

## Examples

Model predictive control of a multi-input single-output system (see the demo `MISO.M`). The system has three inputs (one manipulated variable, one measured disturbance, one unmeasured disturbance) and one output.

```

% Open-loop system parameters

% True plant and true initial state
sys=ss(tf({1,1,1},{[1 .5 1],[1 1],[.7 .5 1]}));
x0=[0 0 0 0 0]';

% MPC object setup

Ts=.2;          % sampling time

% Define type of input signals
model.InputGroup=struct('Manipulated',1,'Measured',2,'Unmeasured',3);

% Define constraints on manipulated variable
MV=struct('Min',0,'Max',1);

Model=[]; % Reset structure Model
Model.Plant=sys;

```

```
% Integrator driven by white noise with variance=1000
Model.Disturbance=tf(sqrt(1000),[1 0]);

p=[];          % Prediction horizon (take default one)
m=3;          % Control horizon
weights=[];   % Default value for weights

MPCobj=mpc(Model,Ts,p,m,weights,MV);

% Simulate closed loop system using MPCMOVE

Tstop=30;     %Simulation time

xmpc=mpcstate(MPCobj); % Initial state of MPC controller
x=x0;         % Initial state of Plant
r=1;         % Output reference trajectory

% State-space matrices of Plant model
[A,B,C,D]=ssdata(c2d(sys,Ts));

YY=[];XX=[];RR=[];
for t=0:round(Tstop/Ts)-1,
    XX=[XX,x];

    % Define measured disturbance signal
    v=0;
    if t*Ts>=10, v=1; end

    % Define unmeasured disturbance signal
    d=0;
    if t*Ts>=20, d=-0.5; end

    % Plant equations: output update
    % (note: no feedthrough from MV to Y, D(:,1)=0)
    y=C*x+D(:,2)*v+D(:,3)*d;
    YY=[YY,y];

    % Compute MPC law
    u=mpcmove(MPCobj,xmpc,y,r,v);
```

```
        % Plant equations: state update
        x=A*x+B(:,1)*u+B(:,2)*v+B(:,3)*d;
    end

    % Plot results
    plot(0:Ts:Tstop-Ts,YY);grid
```

**See Also**

`mpc`, `mpcstate`, `sim`, `setestim`, `getestim`

# mpcprops

---

<b>Purpose</b>	Provide help on MPC controller's properties.
<b>Syntax</b>	mpcprops
<b>Description</b>	mpcprops displays details on the generic properties of MPC controllers. It provides a complete list of all the fields of MPC objects with a brief description of each field and the corresponding default values.
<b>See Also</b>	get, set, mpchelp



<b>Purpose</b>	Specify MPC simulation options
<b>Syntax</b>	<code>SimOptions=mpcsimopt(mpcobj)</code>
<b>Description</b>	<p>The purpose of <code>mpcsimopt</code> is to create an object <code>SimOptions</code> of class <code>@mpcsimopt</code> for specifying additional parameters for simulation with <code>sim</code>.</p> <p><code>SimOptions=mpcsimopt(mpcobj)</code> creates an empty object <code>SimOptions</code> which is compatible with the MPC object <code>mpcobj</code>. The fields of the object <code>SimOptions</code> and their description are reported in Table 8-12, MPC Simulation Options Properties, on page 8-14.</p>
<b>Examples</b>	<p>We want to simulate the MPC control of a multi-input multi-output (MIMO) system under predicted / actual plant model mismatch (<code>demo simmismatch.m</code>). The system has two manipulated variables, two unmeasured disturbances, and two measured outputs.</p> <pre> % Open-loop system parameters p1 = tf(1,[1 2 1])*[1 1; 0 1]; plant = ss([p1 p1]);  % Define I/O types plant=setmpcsignals(plant,'MV',[1 2],'UD',[3 4]);  % Define I/O names (optional) set(plant,'InputName',{'mv1','mv2','umd3','umd4'});  % Model for unmeasured input disturbances distModel = eye(2,2)*ss(-.5,1,1,0);  % Create MPC object mpcobj = mpc(plant,1,40,2); mpcobj.Model.Disturbance = distModel;  % Closed-loop MPC simulation with model mismatch and unforeseen % unmeasured disturbance inputs  % Define plant model generating the data p2 = tf(1.5,[0.1 1 2 1])*[1 1; 0 1]; psim = ss([p2 p2 tf(1,[1 1])*[0;1]]); </pre>

# mpcsimopt

---

```
psim=setmpcsignals(psim,'MV',[1 2],'UD',[3 4 5]);

% Closed-loop simulation
dist=ones(1,3); % Unmeasured disturbance trajectory
refs=[1 2];    % Output reference trajectory
Tf=100; % Total number of simulation steps

options=mpcsimopt(mpcobj);
options.unmeas=dist;
options.model=psim;

sim(mpcobj,Tf,refs,options);
```

## See Also

[sim](#)

---

<b>Purpose</b>	Define MPC controller state
<b>Syntax</b>	<pre>xmpc=mpcstate(MPCobj, xp, xd, xn, u) xmpc=mpcstate(MPCobj)</pre>
<b>Description</b>	<p><code>xmpc=mpcstate(MPCobj, xp, xd, xn, u)</code> defines an <code>mpcstate</code> object for state estimation and optimization in an MPC control algorithm based on the MPC object <code>MPCobj</code>. The state of an MPC controller contains the estimates of the states <math>x(k)</math>, <math>x_d(k)</math>, <math>x_m(k)</math>, where <math>x(k)</math> is the state of the plant model, <math>x_d(k)</math> is the overall state of the input and output disturbance model, <math>x_m(k)</math> is the state of the measurement noise model, and the value of the last vector <math>u(k-1)</math> of manipulated variables. The overall state is updated from the measured output <math>y_m(k)</math> by a linear state observer (see “State Observer” on page 2-9)</p> <p><code>xmpc=mpcstate(MPCobj)</code> returns a default extended initial state that is compatible with the MPC controller <code>MPCobj</code>. Such a default state has plant state and previous input initialized at nominal values, and the states of the disturbance and noise models at zero.</p> <p>Note that <code>mpcstate</code> objects are updated by <code>mpcmove</code> through the internal state observer based on the extended prediction model.</p>
<b>See Also</b>	<code>getoutdist</code> , <code>setoutdist</code> , <code>setindist</code> , <code>getestim</code> , <code>setestim</code> , <code>ss</code> , <code>mpcmove</code>

# mpcverbosity

---

**Purpose** Change the level of verbosity of the MPC Toolbox

**Syntax** `mpcverbosity on`  
`mpcverbosity off`  
`mpcverbosity`

**Description** `mpcverbosity on` enables messages displaying default operations taken by the MPC Toolbox during the creation and manipulation of MPC objects.

`mpcverbosity off` turns messages off.

`mpcverbosity` just shows the verbosity status.

By default, messages are turned on.

See also “Construction and Initialization” on page 8-12.

**See Also** `mpc`

**Purpose** Reduce size of MPC object in memory

**Syntax** `pack(MPCobj)`

**Description** `pack(MPCobj)` cleans up information build at initialization and stored in the `MPCData` field of the MPC object `MPCobj`. This reduces the amount of bytes in memory required to store the MPC object. For MPC objects based on large prediction models it is recommended to pack the object before saving the object to file, in order to minimize the size of the file.

**See Also** `mpc`, `getmpcdata`, `setmpcdata`, `compare`

# plot

---

**Purpose** Plot responses generated by MPC simulations

**Syntax** `plot(MPCobj,t,y,r,u,v,d)`

**Description** `plot(MPCobj,t,y,r,u,v,d)` plots the results of a simulation based on the MPC object `MPCobj`. `t` is a vector of length `Nt` of time values, `y` is a matrix of output responses of size `[Nt,Ny]` where `Ny` is the number of outputs, `r` is a matrix of setpoints and has the same size as `y`, `u` is a matrix of manipulated variable inputs of size `[Nt,Nu]` where `Nu` is the number of manipulated variables, `v` is a matrix of measured disturbance inputs of size `[Nt,Nv]` where `Nv` is the number of measured disturbance inputs, and `d` is a matrix of unmeasured disturbance inputs of size `[Nt,Nd]` where `Nd` is the number of unmeasured disturbances input.

**See Also** `sim`, `mpc`

**Purpose** Solve a convex quadratic program using Dantzig-Wolfe's algorithm

**Syntax** `[xopt,lambda,how]=qpdantz(H,f,A,b,xmin)`  
`[xopt,lambda,how]=qpdantz(H,f,A,b,xmin,maxiter)`

**Description** `[xopt,lambda,how]=qpdantz(H,f,A,b,xmin)` solves the convex quadratic program

$$\min \quad \frac{1}{2}x^T Hx + f^T x$$

subject to  $Ax \leq b, x \geq x_{min}$

using Dantzig-Wolfe's active set method [2]. The Hessian matrix H should be positive definite. By default, `xmin=1e-5`. Vector `xopt` is the optimizer. Vector `lambda` contains the optimal dual variables (Lagrange multipliers).

The exit flag `how` is either 'feasible', 'infeasible' or 'unreliable'. The latter occurs when the solver terminates because the maximum number `maxiter` of allowed iterations was exceeded.

The solver is implemented in `qp solver.d11`. Dantzig-Wolfe's algorithm uses the direction of the largest gradient, and the optimum is usually found after about  $n+q$  iterations, where  $n=\dim(x)$  is the number of optimization variables, and  $q=\dim(b)$  is the number of constraints. More than  $3(n+q)$  iterations are rarely required (see Chapter 7.3 of [3]).

**Examples** Solve a random QP problem using `quadprog` from the Optimization Toolbox and `qpdantz`.

```
n=50;      % Number of vars

H=rand(n,n);H=H'*H;H=(H+H')/2;
f=rand(n,1);
A=[eye(n);-eye(n)];
b=[rand(n,1);rand(n,1)];

x1=quadprog(H,f,A,b);
[x2,how]=qpdantz(H,f,A,b,-100*ones(n,1));
```

## References

[2] Fletcher, R. *Practical Methods of Optimization*, John Wiley & Sons, Chichester, UK, 1987.

[3] Dantzig, G.B. *Linear Programming and Extensions*, Princeton University Press, Princeton, 1963.



---

<b>Purpose</b>	Set or modify MPC object properties
<b>Syntax</b>	<pre>set(sys, 'Property', Value) set(sys, 'Property1', Value1, 'Property2', Value2, ...) set(sys, 'Property') set(sys)</pre>
<b>Description</b>	<p>The set function is used to set or modify the properties of an MPC controller (see “MPC Controller Object” on page 8-2 for background on MPC properties). Like its Handle Graphics counterpart, set uses property name/property value pairs to update property values.</p> <p>set(MPCobj, 'Property', Value) assigns the value Value to the property of the MPC controller MPCobj specified by the string 'Property'. This string can be the full property name (for example, 'UserData') or any unambiguous case-insensitive abbreviation (for example, 'user').</p> <p>set(MPCobj, 'Property1', Value1, 'Property2', Value2, ...) sets multiple property values with a single statement. Each property name/property value pair updates one particular property.</p> <p>set(MPCobj, 'Property') displays admissible values for the property specified by 'Property'. See “MPC Controller Object” on page 8-2 for an overview of legitimate MPC property values.</p> <p>set(sys) displays all assignable properties of sys and their admissible values.</p>
<b>See Also</b>	mpc, get

# setestim

---

**Purpose** Modify an MPC object's linear state estimator

**Syntax** `setestim(MPCobj,M)`  
`setestim(MPCobj,'default')`

**Description** The `setestim` function modifies the linear estimator gain of an MPC object. The state estimator is based on the linear model (cf. “State Estimation” on page 2-8)

$$x(k+1) = Ax(k) + B_u u(k) + B_v v(k)$$

$$y_m(k) = C_m x(k) + D_{vm} v(k)$$

where  $v(k)$  are the measured disturbances,  $u(k)$  are the manipulated plant inputs,  $y_m(k)$  are the measured plant outputs, and  $x(k)$  is the overall state vector collecting states of plant, unmeasured disturbance, and measurement noise models. The order of the states in  $x$  is the following: plant states; disturbance models states; noise model states].

`setestim(MPCobj,M)`, where `MPCobj` is an MPC object, changes the default Kalman estimator gain stored in `MPCobj` to that specified by matrix `M`.

`setestim(MPCobj,'default')` restores the default Kalman gain.

The estimator used in the MPC Toolbox is described in “State Estimation” on page 2-8. The estimator’s equations are

### Predicted Output Computation:

$$\hat{y}_m(k|k-1) = C_m \hat{x}(k|k-1) + D_{vm} v(k)$$

### Measurement Update:

$$\hat{x}(k|k) = \hat{x}(k|k-1) + M(y_m(k) - \hat{y}_m(k|k-1))$$

### Time Update:

$$\hat{x}(k+1|k) = A\hat{x}(k|k) + B_u u(k) + B_v v(k)$$

By combining these three equations, the overall state observer is

$$\hat{x}(k+1|k) = (A - LC_m)\hat{x}(k|k) + Ly_m(k) + B_u u(k) + (B_v - LD_{vm})v(k)$$

where  $L=AM$ .

---

**Note** The estimator gain  $M$  has the same meaning as the gain  $M$  in function `DKALMAN` of the Control Systems Toolbox.

---

Matrices  $A$ ,  $B_u$ ,  $B_v$ ,  $C_m$ ,  $D_{vm}$  can be retrieved using `getestim` as follows:

```
[M,A,Cm,Bu,Bv,Dvm]=getestim(MPCobj)
```

As an alternative they can be retrieved from the internal structure `MPCobj.MPCData.MPCstruct` under the fields `A`, `Bu`, `Bv`, `Cm`, `Dvm` (see `getmpcdata` on page 6-15).

## Examples

To design an estimator by pole placement, you can use the commands

```
[M,A,Cm]=getestim(MPCobj);
L=place(A',Cm',observer_poles)';
M=A\L;
setestim(MPCobj,M);
```

assuming that the linear system  $AM=L$  is solvable.

---

**Note** The pair  $(A,C_m)$  describing the overall state-space realization of the combination of plant and disturbance models must be observable for the state estimation design to succeed. Observability is checked in the MPC Toolbox at two levels: (1) observability of the plant model is checked *at construction* of the MPC object, provided that the model of the plant is given in state-space form; (2) observability of the overall extended model is checked *at initialization* of the MPC object, after all models have been converted to discrete-time, delay-free, state-space form and combined together (see the note on page 2-11)

---

## See Also

`getestim`, `mpc`, `mpcstate`

# setindist

---

**Purpose** Modify the unmeasured input disturbance model

**Syntax** `setindist(MPCobj, 'integrators')`  
`setindist(MPCobj, 'model', model)`

**Description** `setindist(MPCobj, 'integrators')` imposes the default disturbance model for unmeasured inputs, that is for each unmeasured input disturbance channel, an integrator is added unless there is a violation of observability, otherwise the input is treated as white noise with unit variance (this is equivalent to `MPCobj.Model.Disturbance=[]`)  
`setindist(MPCobj, 'model', model)` sets the input disturbance model to `model` (this is equivalent to `MPCobj.Model.Disturbance=model`).

**See Also** `mpc`, `getindist`, `setestim`, `getestim`, `setoutdist`

**Purpose** Set private MPC data structure

**Syntax** `setmpcdata(MPCObj,mpcdata)`

**Description** `setmpcdata(MPCObj,mpcdata)` changes the private field `MPCData` of the MPC object `MPCObj`, where all internal QP matrices, models, estimator gains are stored at initialization of the object. You may only need this for very advanced use of the MPC Toolbox.

---

**Note** Changes to the data structure may easily lead to unpredictable results.

---

**See Also** `getmpcdata`, `set`, `get`, `pack`

# setmpcsignals

---

**Purpose** Set signal types in MPC plant model

**Syntax** `P=setmpcsignals(P,SignalType1,Channels1,SignalType2,Channels2,...)`

**Description** The purpose of `setmpcsignals` is to set I/O channels of the MPC plant model `P`. `P` must be an LTI object. Valid signal types, their abbreviations, and the channel type they refer to are listed below.

Signal Type	Abbreviation	Channel
Manipulated	MV	Input
MeasuredDisturbances	MD	Input
UnmeasuredDisturbances	UD	Input
MeasuredOutputs	MO	Output
UnmeasuredOutputs	UO	Output

Unambiguous abbreviations of signal types are also accepted.

`P=setmpcsignals(P)` sets channel assignments to default, namely all inputs are manipulated variables (MVs), all outputs are measured outputs (MOs). More generally, input signals that are not explicitly assigned are assumed to be MVs, while unassigned output signals are considered as MOs.

**Examples** We want to define an MPC object based on the LTI discrete-time plant model `sys` with four inputs and three outputs. The first and second input are measured disturbances, the third input is an unmeasured disturbance, the fourth input is a manipulated variable (default), the second output is an unmeasured, all other outputs are measured

```
sys=setmpcsignals(sys,'MD',[1 2],'UD',[3],'UO',[2]);  
mpc1=mpc(sys);
```

---

**Note** When using `setmpcsignals` to modify an existing MPC object, be sure that the fields `Weights`, `MV`, `OV`, `DV`, `Model.Noise`, and `Model.Disturbance` are consistent with the new I/O signal types.

---

## See Also

`mpc`, `set`

# setname

---

**Purpose** Set I/O signal names in MPC prediction model

**Syntax**

```
setname(MPCobj, 'input', I, name)
setname(MPCobj, 'output', I, name)
```

**Description**

`setname(MPCobj, 'input', I, name)` changes the name of the I-th input signal to `name`. This is equivalent to `MPCobj.Model.Plant.InputName{I}=name`. Note that `setname` also updates the read-only `Name` fields of `MPCobj.DisturbanceVariables` and `MPCobj.ManipulatedVariables`.

`setname(MPCobj, 'output', I, name)` changes the name of the I-th output signal to `name`. This is equivalent to `MPCobj.Model.Plant.OutputName{I}=name`. Note that `setname` also updates the read-only `Name` field of `MPCobj.OutputVariables`.

---

**Note** The `Name` properties of `ManipulatedVariables`, `OutputVariables`, and `DisturbanceVariables` are read-only. You must use `setname` to assign signal names, or equivalently modify the `Model.Plant.InputName` and `Model.Plant.OutputName` properties of the MPC object.

---

**See Also** `getname`, `mpc`, `set`



<b>Purpose</b>	Modify the unmeasured output disturbance model
<b>Syntax</b>	<pre>setoutdist(MPCobj, 'integrators') setoutdist(MPCobj, 'remove', channels) setoutdist(MPCobj, 'model', model)</pre>
<b>Description</b>	<p><code>setoutdist(MPCobj, 'integrators')</code> specifies the default method output disturbance model, based on the specs stored in <code>MPCobj.OutputVariables.Integrator</code> and <code>MPCobj.Weights.OutputVariables</code>. Output integrators are added according to the following rule:</p> <ol style="list-style-type: none"><li>1 Outputs are ordered by decreasing output weight (in case of time-varying weights, the sum of the absolute values over time is considered for each output channel. In case of equal output weight, the order within the output vector is followed);</li><li>2 By following such order, an output integrator is added per measured outputs, unless (a) there is a violation of observability; (b) The corresponding value in <code>MPCobj.OutputVariables.Integrator</code> is zero; (c) the corresponding weight is zero. A warning message is given when an integrator is added on an unmeasured output channel.</li></ol> <p><code>setoutdist(MPCobj, 'remove', channels)</code> removes integrators from the output channels specified in vector <code>channels</code>. This corresponds to setting <code>MPCobj.OutputVariables(channels).Integrator=0</code>. The default for <code>channels</code> is <code>(1:ny)</code>, where <code>ny</code> is the total number of outputs, that is, all output integrators are removed.</p> <p><code>setoutdist(MPCobj, 'model', model)</code> replaces the array of output integrators designed by default according to <code>MPCobj.OutputVariables.Integrator</code> with the LTI model <code>model</code>. The model must have <code>ny</code> outputs. If no <code>model</code> is specified, then the default model based on the specs stored in <code>MPCobj.OutputVariables.Integrator</code> and <code>MPCobj.Weights.OutputVariables</code> is used (same as <code>setoutdist(MPCobj, 'integrators')</code>).</p>
<b>See Also</b>	<code>mpc</code> , <code>getestim</code> , <code>setestim</code> , <code>setoutdist</code> , <code>setindist</code>

# sim

---

## Purpose

Simulate closed-loop/open-loop response to arbitrary reference and disturbance signals

## Syntax

```
sim(MPCobj,T,r)
```

```
sim(MPCobj,T,r,v)
```

```
sim(MPCobj,T,r,SimOptions) or sim(MPCobj,T,r,v,SimOptions)
```

```
[y,t,u,xp,xmpc,SimOptions]=sim(MPCobj,T,...)
```

## Description

The purpose of `sim` is to simulate the MPC controller in closed-loop with a linear time-invariant model, which, by default, is the plant model contained in `MPCobj.Model.Plant`. As an alternative `sim` can simulate the open-loop behavior of the model of the plant, or the closed-loop behavior in the presence of a model mismatch between the prediction plant model and the model of the process generating the output data.

`sim(MPCobj,T,r)` simulates the closed-loop system formed by the plant model specified in `MPCobj.Model.Plant` and by the MPC controller specified by the MPC object `MPCobj`, and plots the simulation results. `T` is the number of simulation steps. `r` is the reference signal array with as many columns as the number of output variables.

`sim(MPCobj,T,r,v)` also specifies the measured disturbance signal `v`, that has as many columns as the number of measured disturbances.

---

**Note** The last sample of `r/v` is extended constantly over the simulation horizon, to obtain the correct size.

---

`sim(MPCobj,T,r,SimOptions)` or `sim(MPCobj,T,r,v,SimOptions)` specifies the simulation options object `SimOptions`, such as initial states, input/output noise and unmeasured disturbances, plant mismatch, etc. See `mpcsimopt` on page 6-27 for details.

Without output arguments, `sim` automatically plots input and output trajectories.

`[y,t,u,xp,xmpc,SimOptions]=sim(MPCobj,T,...)` instead of plotting closed-loop trajectories returns the sequence of plant outputs `y`, the time sequence `t` (equally spaced by `MPCobj.Ts`), the sequence `u` of manipulated

variables generated by the MPC controller, the sequence  $x_p$  of states of the model of the plant used for simulation, the sequence  $x_{mpc}$  of states of the MPC controller (provided by the state observer), and the options object `SimOptions` used for the simulation.

The descriptions of the input arguments and their default values are shown in the table below.

Input Argument	Description	Default
<code>MPCobj</code>	MPC object specifying the parameters of the MPC control law	None
<code>T</code>	Number of simulation steps	Largest row-size of $r, v, d, n$
$r$	Reference signal	<code>MPCobj.Model.Nominal.Y</code>
$v$	Measured disturbance signal	Entries from <code>MPCobj.Model.Nominal.U</code>
<code>SimOptions</code>	Object of class <code>@mpcsimopt</code> containing the simulation parameters (See )	[ ]

$r$  is an array with as many columns as outputs,  $v$  is an array with as many columns as measured disturbances. The last sample of  $r/v/d/n$  is extended constantly over the horizon, to obtain the correct size.

The output arguments of `sim` are detailed below.

Output Argument	Description
$y$	Sequence of controlled plant outputs (without noise added on measured ones)
$t$	Time sequence (equally spaced by <code>MPCobj.Ts</code> )

Output Argument	Description
u	Sequence of manipulated variables generated by MPC
xp	Sequence of states of plant model (from Model or SimOptions.Model)
xmpc	Sequence of states of MPC controller (estimates of the extended state) This is a structure with the same fields as the mpcstate object.

## Examples

We want to simulate the MPC control of a multi-input single-output system (the same model as in demo misosim.m). The system has one manipulated variable, one measured disturbance, one unmeasured disturbance, and one output.

```
%Plant model and initial state
sys=ss(tf({1,1,1},{[1 .5 1],[1 1],[.7 .5 1]}));

% MPC object setup
Ts=.2; % sampling time
sysd=c2d(sys,Ts); % prediction model

% Define type of input signals
sysd=setmpcsignals(model,'MV',1,'MD',2,'UD',3);

MPCobj=mpc(sysd); % Default weights and horizons

% Define constraints on manipulated variable
MPCobj.MV=struct('Min',0,'Max',1);

Tstop=30; % Simulation time

Tf=round(Tstop/Ts); % Number of simulation steps
r=ones(Tf,1); % Reference trajectory
v=[zeros(Tf/3,1);ones(2*Tf/3,1)]; % Measured dist. trajectory
sim(MPCobj,Tf,r,v);
```

## See Also

mpcsimopt, mpc, mpcmove

---

<b>Purpose</b>	Display model output/input/disturbance dimensions
<b>Syntax</b>	<code>sizes=size(MPCobj)</code>
<b>Description</b>	<code>sizes=size(MPCobj)</code> returns the row vector <code>sizes = [n<sub>ym</sub> n<sub>u</sub> n<sub>yu</sub> n<sub>v</sub> n<sub>d</sub>]</code> associated with the MPC object <code>MPCobj</code> , where $n_{ym}$ is the number of measured controlled outputs, $n_u$ is the number of manipulated inputs, $n_{yu}$ is the number of unmeasured controlled outputs, $n_v$ is the number of measured disturbances, and $n_d$ is the number of unmeasured disturbances.  <code>size(MPCobj)</code> by itself makes a nice display.
<b>See Also</b>	<code>mpc</code> , <code>set</code>

**Purpose** Convert unconstrained MPC controller to state-space linear form

**Syntax**

```
sys=ss(MPCobj)
[sys,Br,Dr,Bv,Dv,Boff,Doff,But,Dut]=ss(MPCobj)
[sys,Br,Dr,Bv,Dv,Boff,Doff,But,Dut]=ss(MPCobj,ref_preview,md_preview,name_flag)
```

**Description** The ss utility returns the linear controller sys as an LTI system in ss form corresponding to the MPC controller MPCobj when the constraints are not active. The purpose is to use the linear equivalent control in the Control System Toolbox for sensitivity analysis and other linear analysis.

sys=ss(MPCobj) returns the linear discrete-time dynamic controller sys

$$x(k+1) = Ax(k) + By_m(k)$$

$$u(k) = Cx(k) + Dy_m(k)$$

where  $y_m$  is the vector of measured outputs of the plant, and  $u$  is the vector of manipulated variables. The sampling time of controller sys is MPCobj.Ts.

[sys,Br,Dr,Bv,Dv,Boff,Doff,But,Dut]=ss(MPCobj) returns the linearized MPC controller in its full version, that has the following structure

$$x(k+1) = Ax(k) + By_m(k) + B_r r(k) + B_v v(k) + B_{ut} u_{target}(k) + B_{off}$$

$$u(k) = Cx(k) + Dy_m(k) + D_r r(k) + D_v v(k) + D_{ut} u_{target}(k) + D_{off}$$

---

**Note** vector  $x$  includes the states of the observer (plant+disturbance+noise model states) and the previous manipulated variable  $u(k-1)$ .

---

In the general case of nonzero offsets,  $y_m$  (as well as  $r$ ,  $v$ ,  $u_{target}$ ) must be interpreted as the difference between the vector and the corresponding offset. Vectors  $B_{off}$ ,  $D_{off}$  are constant terms due to nonzero offsets, in particular they are nonzero if and only if MPCobj.Model.Nominal.DX is nonzero (continuous-time prediction models), or MPCobj.Model.Nominal.Dx-MPCobj.Model.Nominal.X is nonzero

(discrete-time prediction models). Note that when `Nominal.X` is an equilibrium state,  $B_{\text{off}}$ ,  $D_{\text{off}}$  are zero.

Only the following fields of `MPCobj` are used when computing the state-space model: `Model`, `PredictionHorizon`, `ControlHorizon`, `Ts`, `Weights`.

`[sys, ...]=ss(MPCobj, ref_preview, md_preview, name_flag)` allows you to specify if the MPC controller has preview actions on the reference and measured disturbance signals. If the flag `ref_preview='on'`, then matrices  $B_r$  and  $D_r$  multiply the whole reference sequence:

$$x(k+1) = Ax(k) + By_m(k) + B_r[r(k);r(k+1);...;r(k+p-1)] + \dots$$

$$u(k) = Cx(k) + Dy_m(k) + D_r[r(k);r(k+1);...;r(k+p-1)] + \dots$$

Similarly if the flag `md_preview='on'`, then matrices  $B_v$  and  $D_v$  multiply the whole measured disturbance sequence:

$$x(k+1) = Ax(k) + \dots + B_v[v(k);v(k+1);...;v(k+p)] + \dots$$

$$u(k) = Cx(k) + \dots + D_v[v(k);v(k+1);...;v(k+p)] + \dots$$

The optional input argument `name_flag='names'` adds state, input, and output names to the created LTI object.

## Examples

To get the transfer function `LTIcon` from  $(y_m, r)$  to  $u$ ,

```
[sys, Br, Dr]=ss(MPCobj);
set(sys, 'B', [sys.B, Br], 'D', [sys.D, Dr]);
```

## See Also

`mpc`, `set`, `tf`, `zpk`

# tf

---

**Purpose** Convert unconstrained MPC controller to linear transfer function

**Syntax** `sys=tf(MPCobj)`

**Description** The `tf` function computes the transfer function of the linear controller `ss(MPCobj)` as an LTI system in `tf` form corresponding to the MPC controller when the constraints are not active. The purpose is to use the linear equivalent control in the Control Systems Toolbox for sensitivity and other linear analysis.

**See Also** `ss`, `zpk`



---

<b>Purpose</b>	Compute the steady-state value of the MPC controller state for given inputs and outputs values
<b>Syntax</b>	<code>x=trim(MPCobj,y,u)</code>
<b>Description</b>	The <code>trim</code> function finds a steady-state value for the plant state vector such that $x=Ax+Bu$ , $y=Cx+Du$ , or the best approximation of such an $x$ in a least squares sense, sets noise and disturbance model states at zero, and forms the extended state vector.
<b>See Also</b>	<code>mpc</code> , <code>mpcstate</code>

# zpk

---

**Purpose** Convert unconstrained MPC controller to zero/pole/gain form

**Syntax** `sys=zpk(MPCobj)`

**Description** The `zpk` function computes the zero-pole-gain form of the linear controller `ss(MPCobj)` as an LTI system in `zpk` form corresponding to the MPC controller when the constraints are not active. The purpose is to use the linear equivalent control in the Control Systems Toolbox for sensitivity and other linear analysis.

**See Also** `ss`, `tf`

# Block Reference

---

Blocks — Alphabetical List (p. -2)

A list of available blocks, sorted alphabetically

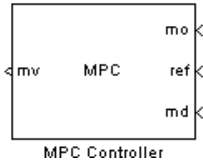
## **Blocks – Alphabetical List**

This section contains function reference pages listed alphabetically.

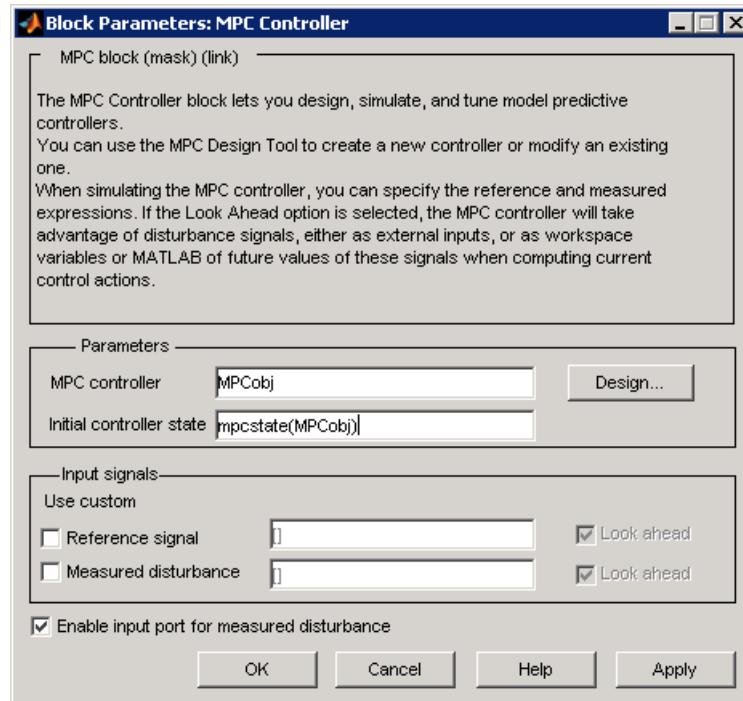
**Purpose** Compute the MPC control law

**Library** MPC Simulink Library

**Description** The MPC Controller Block receives the current measured output, reference signal, and measured disturbance signal, and outputs the optimal manipulated variables by solving a quadratic program. The block is based on an MPC object, which provides performance and constraint specifications, as well as the sampling time of the block.



## Dialog Box



**Figure 7-1: MPC Controller Block Mask**

# MPC Controller Block

---

## **MPC controller**

MPC controller object, defining prediction model, weights, constraints, sampling time, etc.

## **Initial controller state**

Initial state of the MPC controller. This must be a valid `mpcstate` object.

## **Reference signal**

Choose whether the reference signal is loaded from the workspace or received from the block input port. If the signal is received from the workspace, the checkbox **Look Ahead** is enabled, and anticipative action can be selected (see “Look Ahead and Signals from the Workspace” at page 3-4)

## **Measured disturbance**

Choose whether the disturbance signal is loaded from the workspace or received from the block input port. If the signal is received from the workspace, the checkbox **Look Ahead** is enabled, and anticipative action can be selected (see “Look Ahead and Signals from the Workspace” at page 3-4)

The mask requires that you specify a valid MPC controller object. There are two ways of providing an MPC controller object:

- 1** Load an existing MPC object from the workspace, or
- 2** Push the **Design** button to open the MPC Design Tool and design the MPC controller object there. Closed-loop simulations can be run while the MPC controller is edited in the MPC Design Tool. In this case, the controller parameters used for simulating the Simulink diagram are those specified in the MPC Design Tool, so that the parameters of the controller can be more easily tuned.

In the latter case, the designed controller must be exported as an MPC object to the workspace when the Tool is closed, so that the new changes can be still used for simulation.

When no MPC controller is specified in the edit box, the **Design** button will attempt at constructing a default MPC controller by automatically getting a linearized model from the Simulink diagram.

The checkbox **Enable input port for measured disturbance** is used to resize the block. If the checkbox is not checked, the block has two input signal, namely measured outputs and references. When the checkbox is checked, the block has measured disturbances has third input signal.

## See Also

`mpc`, `mpcstate`

# MPC Controller Block

---



# Object Reference

---

This chapter provides reference material for the objects used with the command-line functions. Descriptions of the object properties and fields are given in the following sections.

MPC Controller Object (p. 8-2)	Description of the MPC object containing the parameters defining the MPC control law (prediction horizon, weights, constraints, etc.).
MPC State Object (p. 8-13)	Description of the MPC object containing the state of an MPC controller.
MPC Simulation Options Object (p. 8-14)	Description of the MPC object containing options for simulating MPC controllers.

## MPC Controller Object

All the parameters defining the MPC control law (prediction horizon, weights, constraints, etc.) are stored in an MPC object, whose properties are listed in Table 8-1.

**Table 8-1: MPC Controller Object**

Property	Description
ManipulatedVariables (or MV or Manipulated or Input)	Input and input-rate upper and lower bounds, ECR values, names, units, and input target
OutputVariables (or OV or Controlled or Output)	Output upper and lower bounds, ECR values, names, units
DisturbanceVariables (or DV or Disturbance)	Disturbance names and units
Weights	Weights defining the performance function
Model	Plant, input disturbance, and output noise models, and nominal conditions.
Ts	Controller's sampling time
Optimizer	Parameters for the QP solver
PredictionHorizon	Prediction horizon
ControlHorizon	Number of free control moves or vector of blocking moves
History	Creation time
Notes	User notes (text)
UserData	Any additional data

**Table 8-1: MPC Controller Object**

Property	Description
MPCData (private)	Matrices for the QP problem and other accessorial data
Version (private)	MPC Toolbox version number

### ManipulatedVariables

`ManipulatedVariables` (or `MV` or `Manipulated` or `Input`) is an  $n_u$ -dimensional array of structures ( $n_u$  = number of manipulated variables), one per manipulated variable. Each structure has the fields described in Table 8-2, where  $p$  denotes the prediction horizon.

**Table 8-2: Structure ManipulatedVariables**

Field Name	Content	Default
Min	1 to $p$ dimensional vector of lower constraints on a manipulated variable $u$	- Inf
Max	1 to $p$ dimensional vector of upper constraints on a manipulated variable $u$	Inf
MinECR	1 to $p$ dimensional vector describing the equal concern for the relaxation of the lower constraints on $u$	0
MaxECR	1 to $p$ dimensional vector describing the equal concern for the relaxation of the upper constraints on $u$	0
Target	1 to $p$ dimensional vector of target values for the input variable $u$	0
RateMin	1 to $p$ dimensional vector of lower constraints on the rate of a manipulated variable $u$	- Inf if problem is unconstrained, otherwise -10

**Table 8-2: Structure ManipulatedVariables**

Field Name	Content	Default
RateMax	1 to $p$ dimensional vector of upper constraints on the rate of a manipulated variable $u$	Inf
RateMinECR	1 to $p$ dimensional vector describing the equal concern for the relaxation of the lower constraints on the rate of $u$	0
RateMaxECR	1 to $p$ dimensional vector describing the equal concern for the relaxation of the upper constraints on the rate of $u$	0
Name	Name of input signal. This is inherited from InputName of the LTI plant model	InputName of LTI plant model
Units	String specifying the measurement units for the manipulated variable	' '

---

**Note** Rates refer to the difference  $\Delta u(k)=u(k)-u(k-1)$ . Constraints and weights based on derivatives  $du/dt$  of continuous-time input signals must be properly reformulated for the discrete-time difference  $\Delta u(k)$ , using the approximation  $du/dt \cong \Delta u(k)/T_s$ .

---

## OutputVariables

OutputVariables (or OV or Controlled or Output) is an  $n_y$ -dimensional array of structures ( $n_y$  = number of outputs), one per output signal. Each structure has the fields described in Table 8-3, where  $p$  denotes the prediction horizon.

**Table 8-3: Structure** OutputVariables

Field Name	Content	Default
Min	1 to $p$ dimensional vector of lower constraints on an output $y$	- Inf
Max	1 to $p$ dimensional vector of upper constraints on an output $y$	Inf
MinECR	1 to $p$ dimensional vector describing the equal concern for the relaxation of the lower constraints on an output $y$	1
MaxECR	1 to $p$ dimensional vector describing the equal concern for the relaxation of the upper constraints on an output $y$	1
Name	Name of output signal. This is inherited from OutputName of the LTI plant model	OutputName of LTI plant model
Units	String specifying the measurement units for the measured output	''
Integrator	Magnitude of integrated white noise on the output channel (0=no integrator)	[ ]

In order to reject constant disturbances due for instance to gain nonlinearities, the default output disturbance model used in the MPC Toolbox is a collection of integrators driven by white noise on measured outputs (see “Output Disturbance Model” on page 2-9). Output integrators are added according to the following rule:

- 1 Measured outputs are ordered by decreasing output weight (in case of time-varying weights, the sum of the absolute values over time is considered

for each output channel, and in case of equal output weight, the order within the output vector is followed)

- 2 By following such order, an output integrator is added per measured outputs, unless there is a violation of observability, or the corresponding weight is zero, or the user forces it by zeroing the corresponding value in `OutputVariables.Integrators`).

By default, `OutputVariables.Integrators` is empty on all outputs. This enforces the default action of the MPC Toolbox, namely add integrators on measured outputs, do not add integrators on unmeasured outputs. By setting the entry of `OutputVariables(i).Integrators` to zero, no attempt will be made to add integrated white noise on the *i*-th output. On the contrary, by setting the entry of `OutputVariables(i).Integrators` to one, an attempt will be made to add integrated white noise on the *i*-th output (see `getoutdist` on page 6-17)

### DisturbanceVariables

`DisturbanceVariables` (or DV or Disturbance) is an  $(n_v+n_d)$ -dimensional array of structures ( $n_v$  = number of measured input disturbances,  $n_d$  = number of unmeasured input disturbances), one per input disturbance. Each structure has the fields described in Table 8-4.

**Table 8-4: Structure DisturbanceVariables**

Field Name	Content	Default
Name	Name of input signal. This is inherited from <code>InputName</code> of the LTI plant model	<code>InputName</code> of LTI plant model
Units	String specifying the measurement units for the manipulated variable	''

The order of the disturbance signals within the array `DisturbanceVariables` is the following: the first  $n_v$  entries relate to measured input disturbances, the last  $n_d$  entries relate to unmeasured input disturbances.

---

**Note** The Name properties of ManipulatedVariables, OutputVariables, and DisturbanceVariables are read-only. You can set signal names in the Model.Plant.InputName and Model.Plant.OutputName properties of the MPC object, for instance by using the method setname.

---

## Weights

Weights is the structure defining the weighting matrices. Unlike the InputSpecs and OutputSpecs that are arrays of structures, weights is a single structure, whose fields are described in Table 8-5, where  $p$  denotes the prediction horizon,  $n_u$  the number of manipulated variables,  $n_y$  the number of output variables.

**Table 8-5: Structure** Weights

Field Name	Content	Default
ManipulatedVariables (or MV or Manipulated or Input)	$n_u$ -by-(1 to $p$ ) dimensional array of input weights	zeros(nu, 1)
ManipulatedVariablesRate (or MVRate or ManipulatedRate or InputRate)	$n_u$ -by-(1 to $p$ ) dimensional array of input-rate weights	0.1*ones(nu, 1)
OutputVariables (or OV or Controlled or Output)	$n_y$ -by-(1 to $p$ ) dimensional array of output weights	1 (The default for output weights is the following: if $n_u \geq n_y$ , all outputs are weighted with unit weight; if $n_u < n_y$ , $n_u$ outputs are weighted with unit weight (with a preference on measured outputs), while the remaining outputs are not weighted.)
ECR	Weight on the slack variable $\epsilon$ used for softening the constraints	1e5*(max weight)

`ManipulatedVariables`, `ManipulatedVariablesRate`, and `OutputVariables` are arrays with as many columns as inputs or outputs. If weights are time invariant, then `ManipulatedVariables`, `ManipulatedVariablesRate`, and `OutputVariables` are row vectors, while for time-varying weights, they are an array with up to  $p$  rows. The last row is repeated by default in case the matrix has a number of rows smaller than the prediction horizon  $p$ .

The default ECR weight is  $10^5$  times the largest weight specified in `ManipulatedVariables`, `ManipulatedVariablesRate`, and `OutputVariables`.

---

**Note** All weights must be greater than or equal to zero. If all weights on manipulated variable increments are strictly positive, the resulting QP problem is always strictly convex. If some of those weights are zero, the Hessian matrix of the QP problem may become only positive semidefinite. In order to keep the QP problem always strictly convex, if the condition number of the Hessian matrix  $K_{\Delta U}$  is larger than  $10^{12}$ , the quantity  $10 \cdot \sqrt{\text{eps}}$  is added on each diagonal term. This may only occur when all input rates are not weighted ( $W^{\Delta u} = 0$ ) (see note on page 2-16)

---

## Model

The property `Model` specifies plant, input disturbance, and output noise models, and nominal conditions, according to the model setup described in Figure 2-2. It is specified through a structure containing the fields reported in Table 8-6.

**Table 8-6: Structure Model Describing the Models Used by MPC**

Field Name	Content	Default
Plant	LTI model (or IDMODEL) of the plant	No default
Disturbance	LTI model describing color of input disturbances	An integrator on each Unmeasured input channel



**Table 8-6: Structure Model Describing the Models Used by MPC**

Field Name	Content	Default
Noise	LTI model describing color of plant output measurement noise	Unit white noise on each measured output = identity static gain
Nominal	Structure containing the state, input, and output values where Model.Plant is linearized	See Table 8-9

**Note** Direct feedthrough from manipulated variables to measured outputs in Model.Plant is not allowed. See note on page 2-3.

The type of input and output signals is assigned either through the InputGroup and OutputGroup properties of Model.Plant, or, more conveniently, through function setmpcsignals, according to the nomenclature described in Table 8-7 and Table 8-8.

**Table 8-7: Input Groups in Plant Model**

Name	Value
ManipulatedVariables (or MV or Manipulated or Input)	Indices of manipulated variables
MeasuredDisturbances (or MD or Measured)	Indices of measured disturbances
UnmeasuredDisturbances (or UD or Unmeasured)	Indices of unmeasured disturbances

**Table 8-8: Output Groups in Plant Model**

Name	Value
MeasuredOutputs (or MO or Measured)	Indices of measured outputs
UnmeasuredOutputs (or UO or Unmeasured)	Indices of unmeasured outputs

By default, all inputs are manipulated variables, and all outputs are measured.

**Note** With this current release, the InputGroup and OutputGroup properties of LTI objects are defined as structures, rather than cell arrays (see the Control System Toolbox documentation for more details).

The structure Nominal contains the nominal values for states, inputs, outputs and state derivatives/differences at the operating point where Model.Plant was linearized. The fields are reported in Table 8-9 (see “Offsets” on page 2-4).

**Table 8-9: Nominal Values at Operating Point**

Field	Description	Default
X	Plant state at operating point	0
U	Plant input at operating point, including manipulated variables, measured and unmeasured disturbances	0
Y	Plant output at operating point	0
DX	For continuous-time models, DX is the state derivative at operating point: $DX=f(X,U)$ . For discrete-time models, $DX=x(k+1)-x(k)=f(X,U)-X$ .	0

**Ts**

Sampling time of the MPC controller. By default, if `Model.Plant` is a discrete-time model, `Ts=Model.Plant.ts`. For continuous-time plant models, you must specify a sampling time for the MPC controller.

**Optimizer**

Parameters for the QP optimization. `Optimizer` is a structure with the fields reported in Table 8-10.

**Table 8-10: Optimizer Properties**

Field	Description	Default
<code>MaxIter</code>	Maximum number of iterations allowed in the QP solver	200
<code>Trace</code>	On/off	'off'
<code>Solver</code>	QP solver used (only 'ActiveSet')	'ActiveSet'
<code>MinOutputECR</code>	Minimum positive value allowed for <code>OutputMinECR</code> and <code>OutputMaxECR</code>	1e-10

`MinOutputECR` is a positive scalar used to specify the minimum allowed ECR for output constraints. If values smaller than `MinOutputECR` are provided in the `OutputVariables` property of the MPC objects a warning message is issued and the value is raised to `MinOutputECR`.

**PredictionHorizon**

`PredictionHorizon` is an integer value expressing the number  $p$  of sampling steps of prediction.

**ControlHorizon**

`ControlHorizon` is either a number of free control moves, or a vector of blocking moves (see “Optimization Variables” on page 2-13).

**History**

`History` stores the time the MPC controller was created.

### Notes

`Notes` stores user's notes as a cell array of strings.

### UserData

Any additional data stored within the MPC controller object

### MPCData

`MPCData` is a private property of the MPC object used for storing intermediate operations, QP matrices, internal flags, etc. See `getmpcdata` on page 6-15 and `setmpcdata` on page 6-39.

### Version

`Version` is a private property indicating the MPC Toolbox version number.

## Construction and Initialization

An MPC object is built in two steps. The first step happens *at construction* of the object when the object constructor `mpc` is invoked, or properties are changed by a `set` command. At this first stage, only basic consistency checks are performed, such as dimensions of signals, weights, constraints, etc. The second step happens *at initialization* of the object, namely when the object is used for the first time by methods such as `mpcmove` and `sim`, that require the full computation of the QP matrices and the estimator gain. At this second stage, further checks are performed, such as a test of observability of the overall extended model.

Informative messages are displayed in the command window in both phases, you can turn them on or off using the `mpcverbosity` command.

## MPC State Object

The `mpcstate` object type contains the state of an MPC controller. Its properties are listed in Table 8-11.

**Table 8-11: MPC State Object Properties**

Property	Description
Plant	Array of plant states. Values are absolute, i.e., they include possible state offsets (cf. <code>Model.Nominal.X</code> )
Disturbance	Array of states of unmeasured disturbance models. This contains the states of the input disturbance model and, appended below, the states of the unmeasured output disturbances model
Noise	Array of states of measurement noise model
LastInput	Array of previous manipulated variables $u(k-1)$ . Values are absolute, i.e., they include possible input offsets (cf. <code>Model.Nominal.U</code> ).

The command

```
mpcstate(mpcobj)
```

returns a zero extended initial state compatible with the MPC object `mpcobj`, and with `mpcobj.Plant` and `mpcobj.LastInput` initialized at the nominal values specified in `mpcobj.Model.Nominal`.

## MPC Simulation Options Object

The `mpcsimopt` object type contains various simulation options for simulating an MPC controller with the command `sim`. Its properties are listed in Table 8-12.

**Table 8-12: MPC Simulation Options Properties**

Property	Description
<code>PlantInitialState</code>	Initial state vector of plant model generating the data
<code>ControllerInitialState</code>	Initial condition of the MPC controller. This must be a valid <code>@mpcstate</code> object
<code>UnmeasuredDisturbance</code>	Unmeasured disturbance signal entering the plant
<code>InputNoise</code>	Noise on manipulated variables
<code>OutputNoise</code>	Noise on measured outputs
<code>RefLookAhead</code>	Preview on reference signal ('on' or 'off')
<code>MDLookAhead</code>	Preview on measured disturbance signal ('on' or 'off')
<code>Constraints</code>	Use MPC constraints ('on' or 'off')
<code>Model</code>	Model used in simulation for generating the data.
<code>StatusBar</code>	Display wait bar ('on' or 'off')
<code>MVSignal</code>	Sequence of manipulated variables (with offsets) for open-loop simulation (no MPC action)
<code>OpenLoop</code>	Performs open-loop simulation

The command

```
SimOptions=mpcsimopt(mpcobj)
```

returns an empty `@mpcsimopt` object. You must use `set / get` to change simulation options.

`UnmeasuredDisturbance` is an array with as many columns as unmeasured disturbances, `InputNoise` and `MVSignal` are arrays with as many columns as manipulated variables, `OutputNoise` is an array with as many columns as measured outputs. The last sample of the array is extended constantly over the horizon to obtain the correct size.

---

**Note** Nonzero values of `ControllerInitialState.LastMove` are only meaningful if there are constraints on the increments of the manipulated variables.

---

The property `Model` is useful for simulating the MPC controller under model mismatch. The `LTI` object specified in `Model` can be either a replacement for `Model.Plant`, or a structure with fields `Plant`, `Nominal`. By default, `Model` is equal to `MPCobj.Model` (no model mismatch). If `Model` is specified, then `PlantInitialState` refers to the initial state of `Model.Plant` and is defaulted to `Model.Nominal.x`.

If `Model.Nominal` is empty, `Model.Nominal.U` and `Model.Nominal.Y` are inherited from `MPCobj.Model.Nominal`. `Model.Nominal.X/DX` is only inherited if both plants are state-space objects with the same state dimension.





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